

3º ENCONTRO NACIONAL DE PESQUISA-PROJETO-PRODUÇÃO EM CONCRETO PRÉ - MOLDADO

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Produção
Projeto
Pesquisa CPM



08 - 09 de julho de 2013

São Carlos / SP

POLITECNICO DI MILANO

3º Encontro Nacional de Pesquisa-Projeto-Produção em Concreto Pré-Moldado

ELEMENTOS PRÉ-MOLDADOS DE PEQUENAS ESPESSURAS PARA COBERTURAS: EXPERIÊNCIA ACUMULADA EM MAIS DE 20 ANOS

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*Department of Civil and Environmental Engineering
Politecnico di Milano*



The Politecnico di Milano net





Pier Luigi Nervi

Architecture as challenge



✓ A long history ... **Ferrocement**



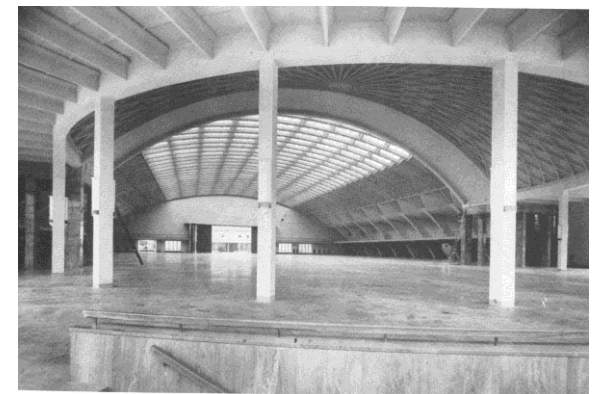
“We wondered if, increasing significantly the diffusion of the steel and its percentage (i.e. reinforcement ratio), it could not be possible to create a new material characterized by a higher strength and especially a larger elasticity and elongation ...”.

Pier Luigi Nervi, 1940

$t = 38 \text{ mm!}$



Vault span 94 m!



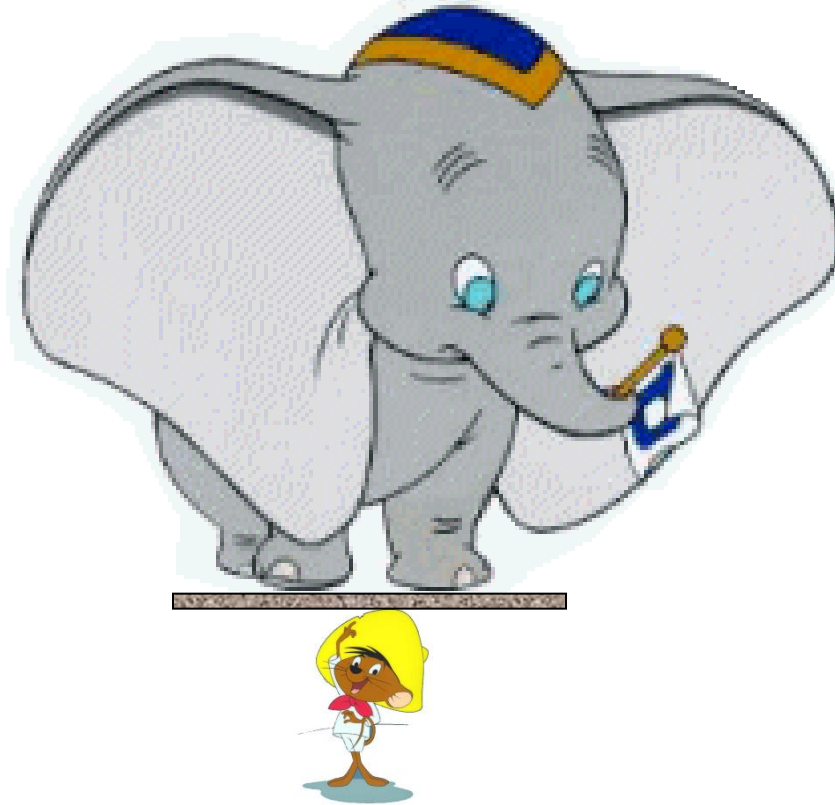
Exposition Palace: B Pavilion, Torino, 1949-50



Why fibres in the precast industry?



The connection as the weak point of the structure







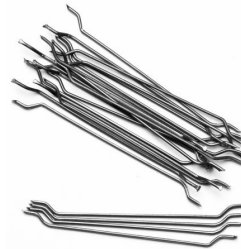


Research in progress at JRC ISPRA



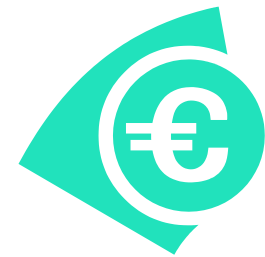
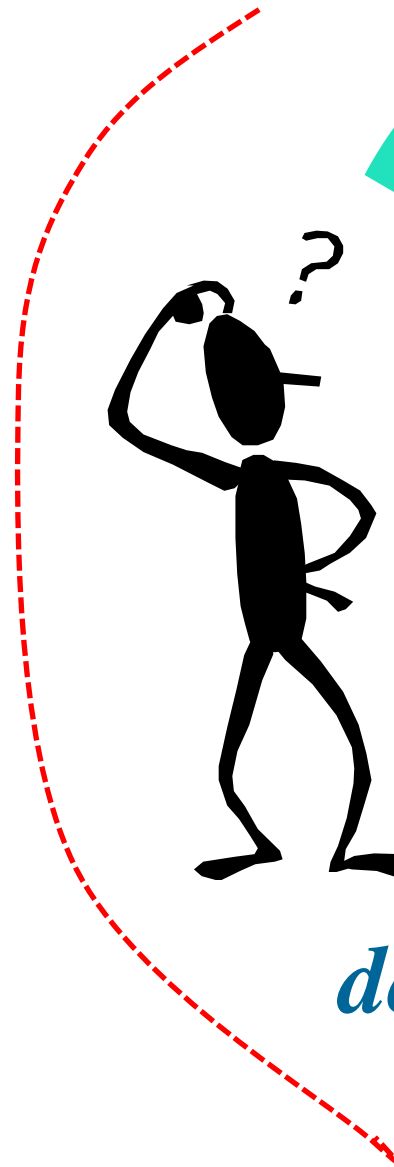






researcher

belt and braces...

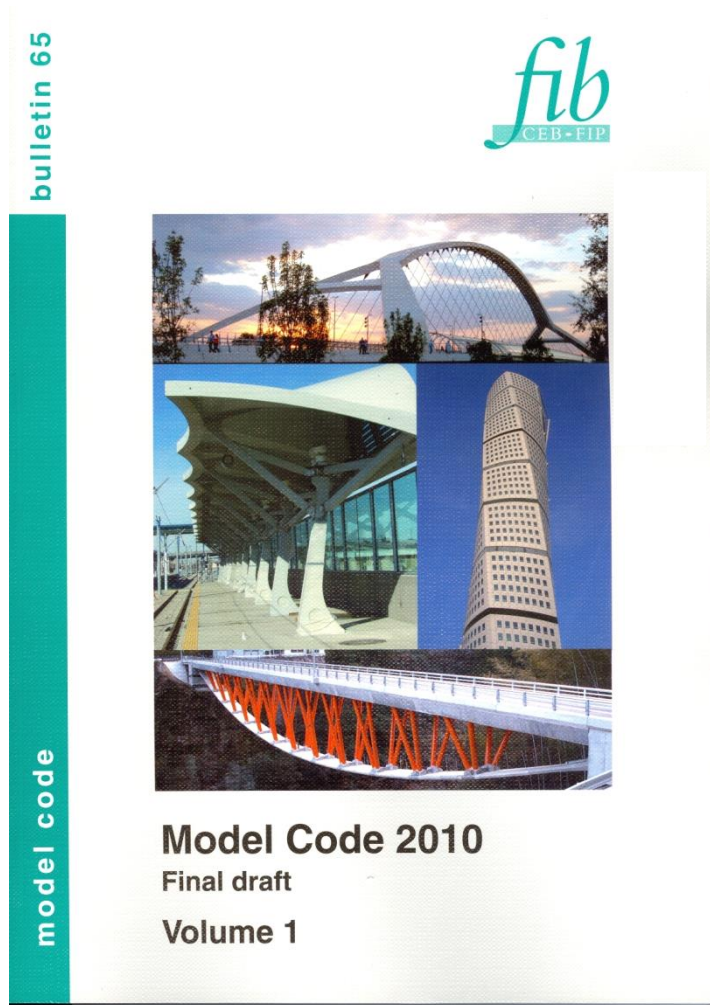


or

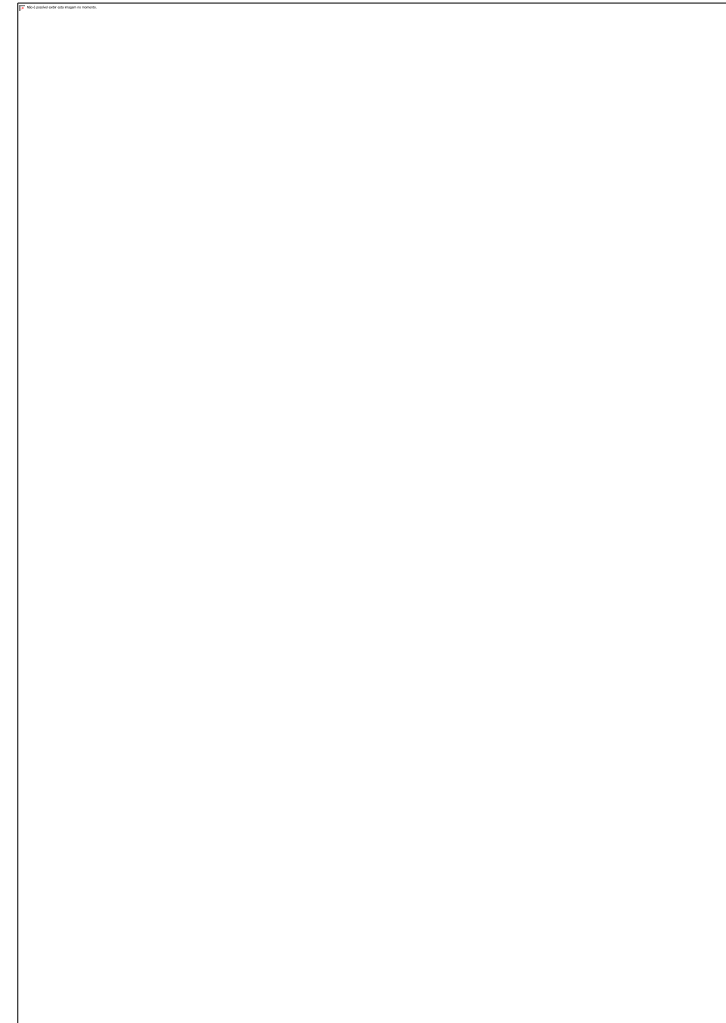


designer

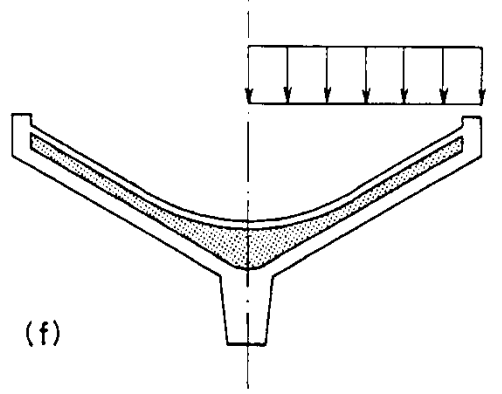
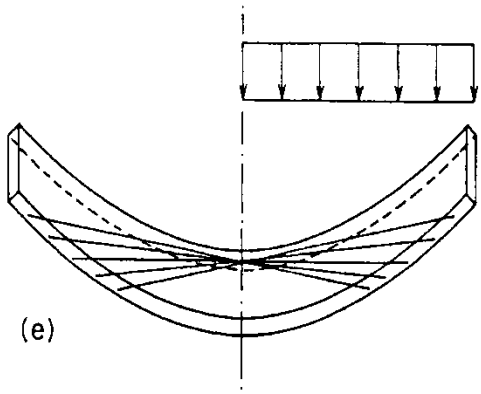
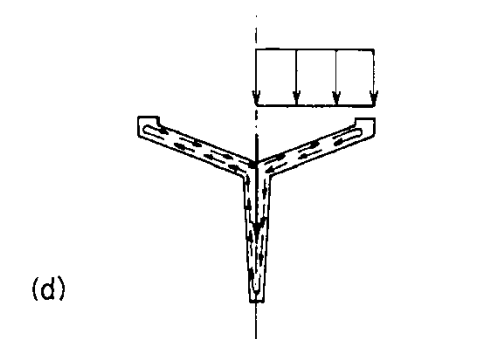
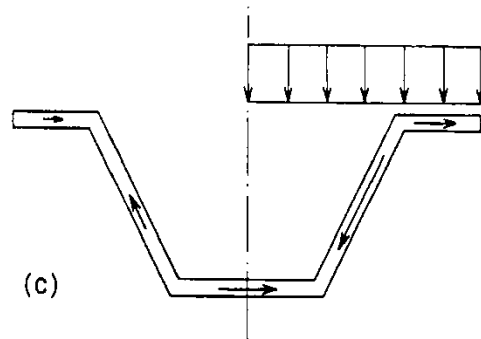
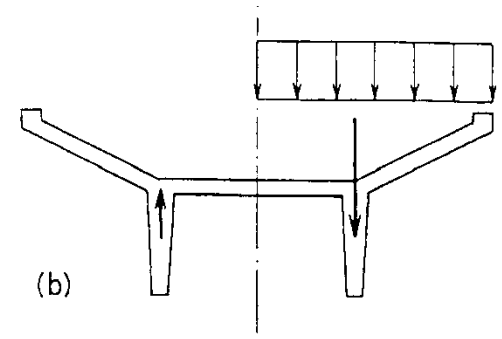
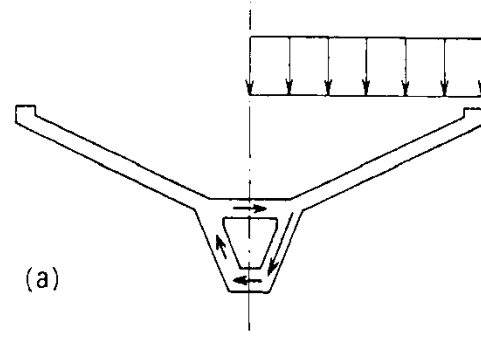
Model Code: material and structure design



Chapter §5.6

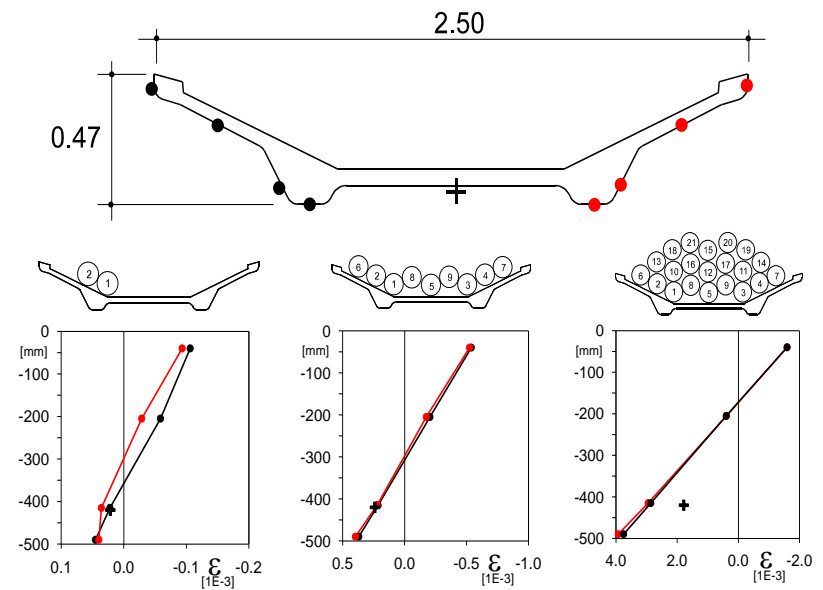
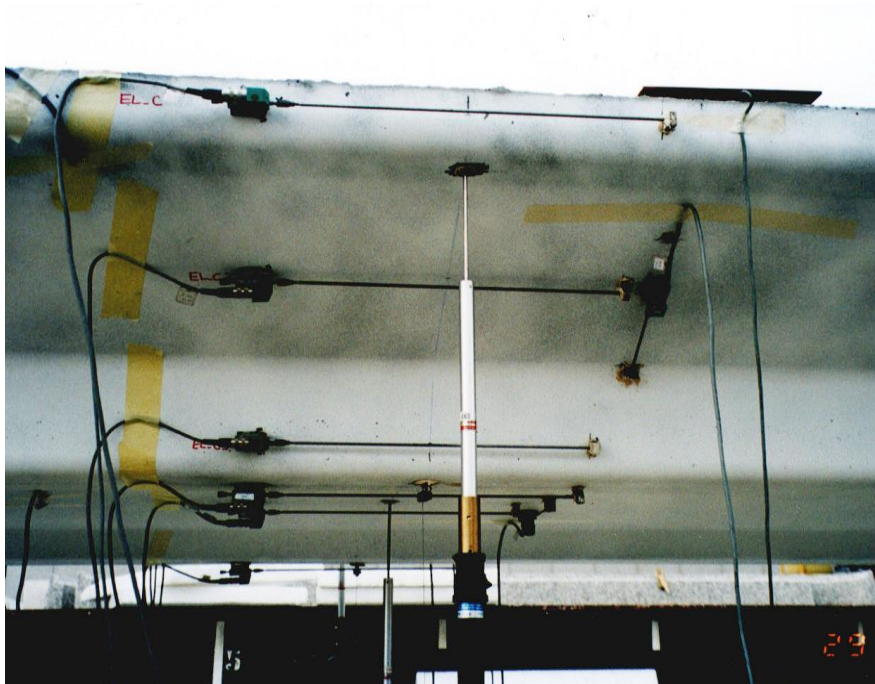


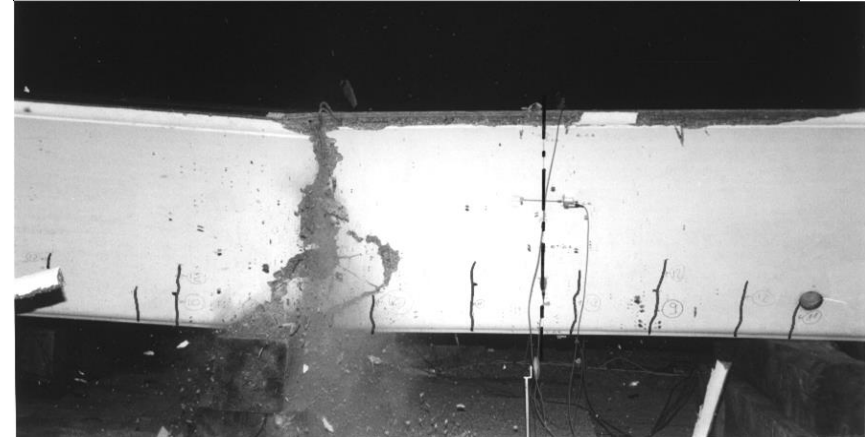
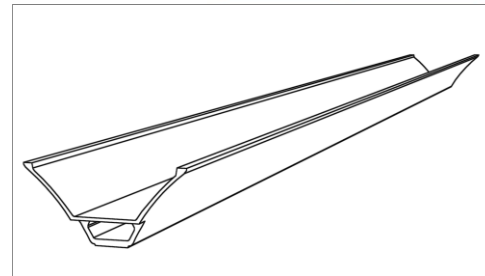
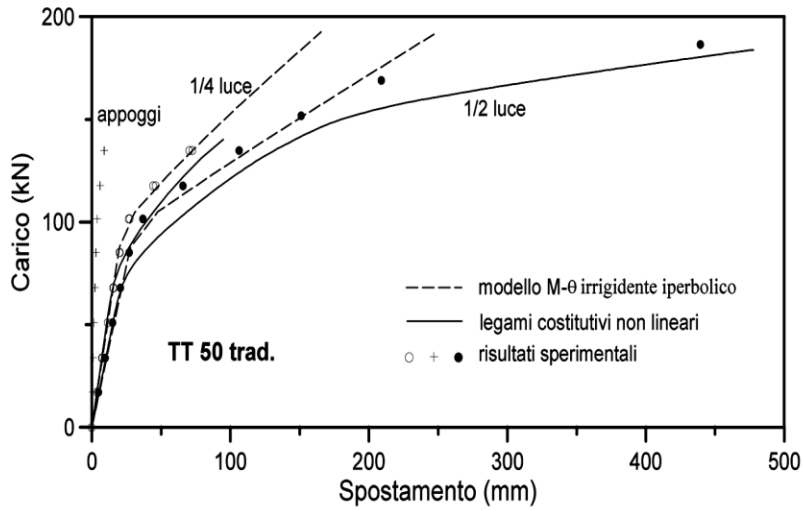
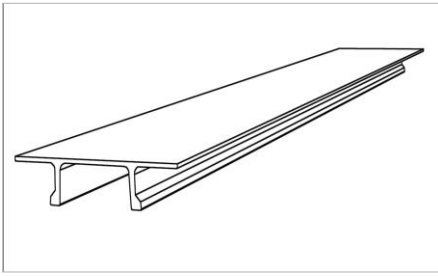
Chapter §7.7

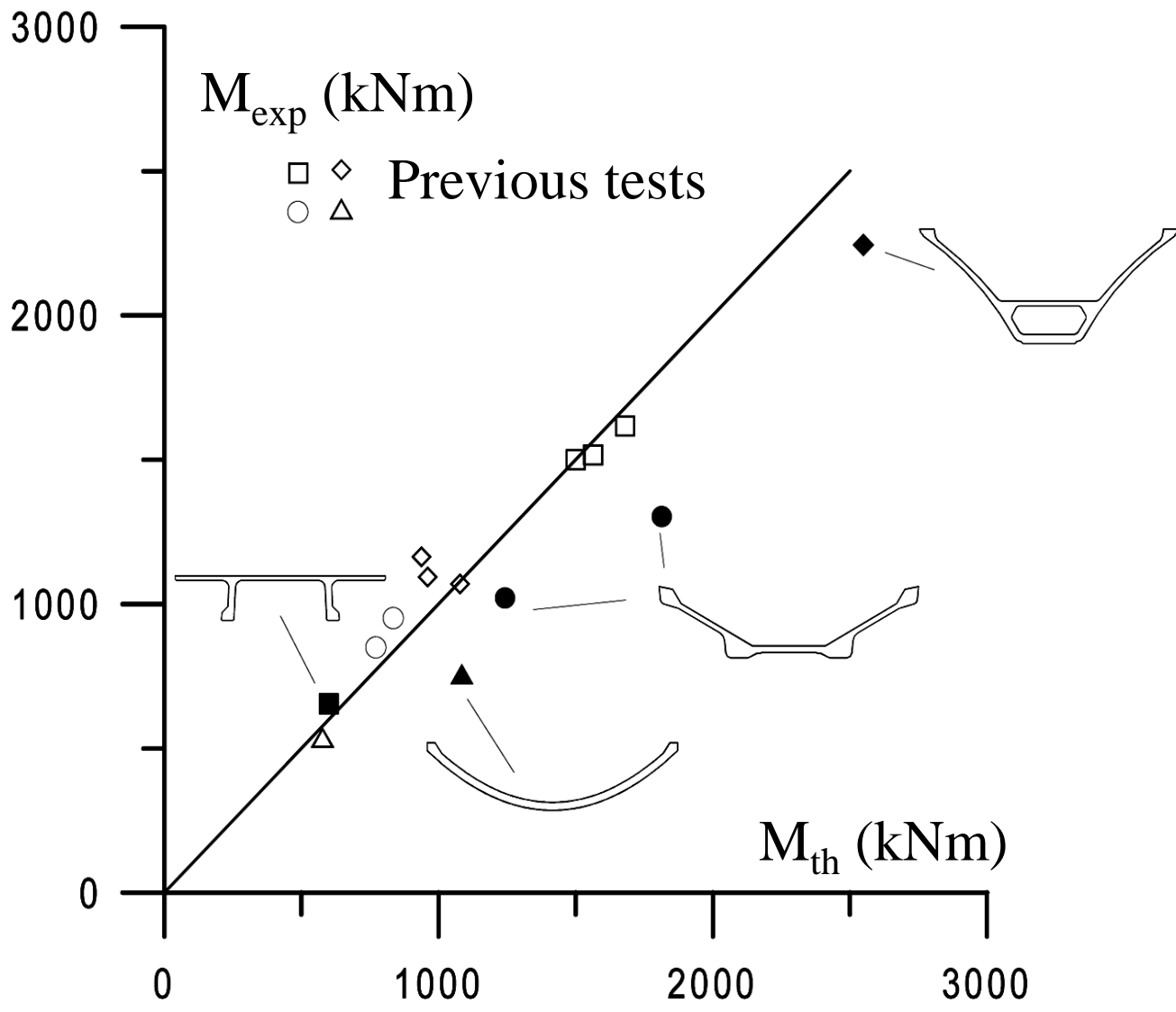


Longitudinal bending

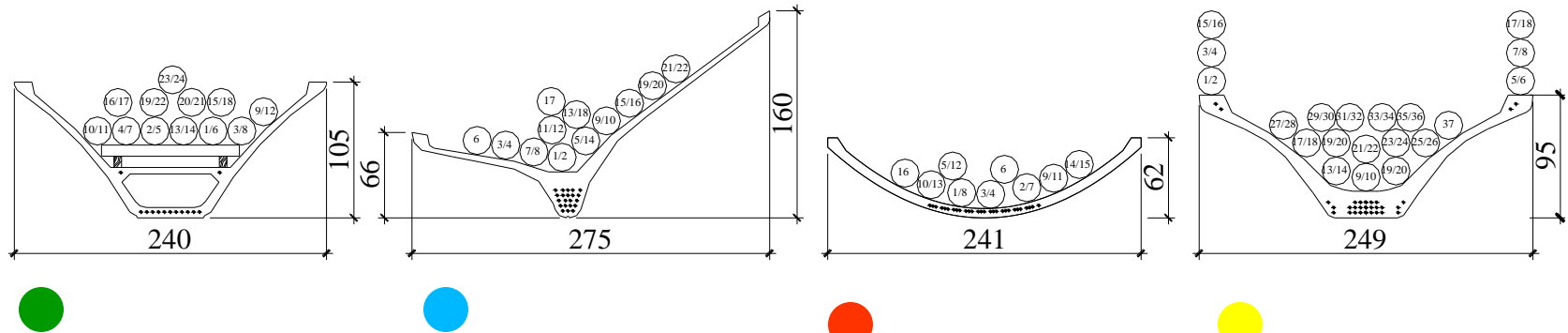
Plane section check





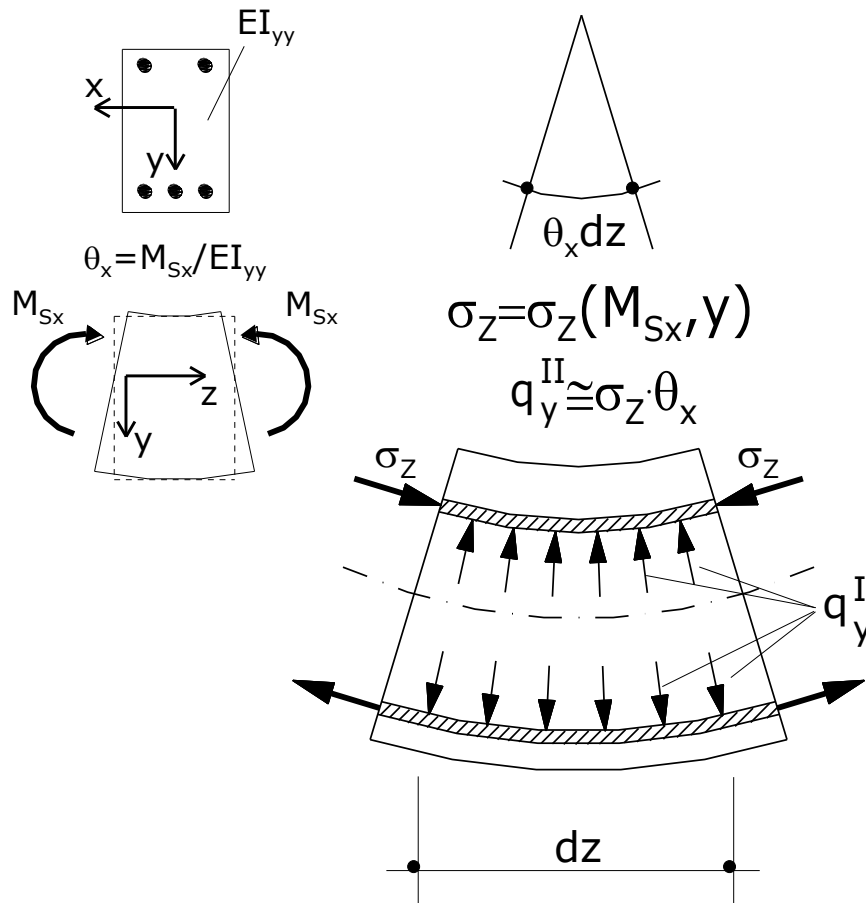


Real-size tests

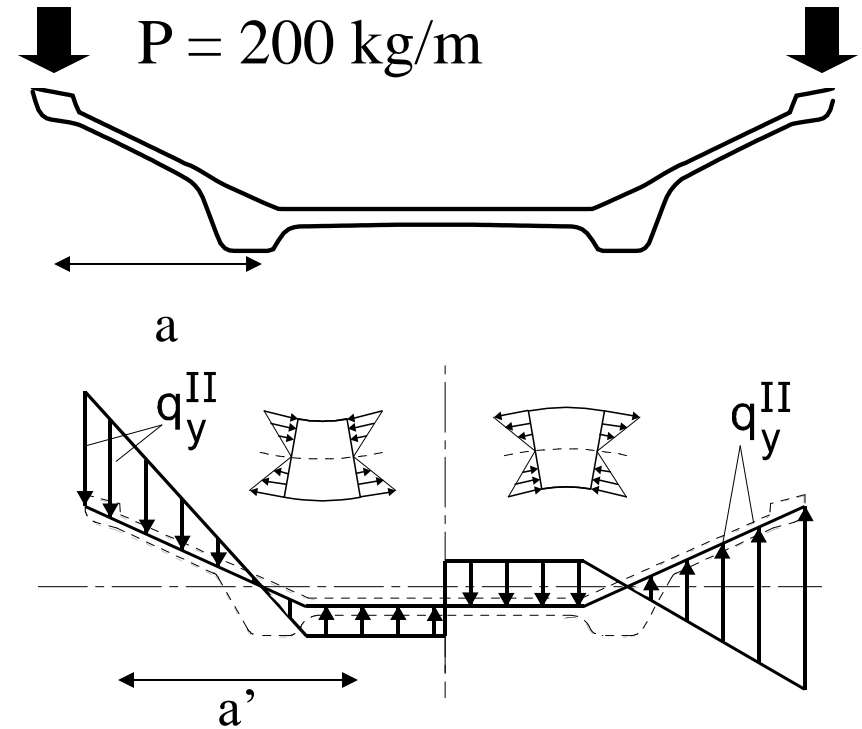


Precast Element	P_{max} [kN]	M_{CEB} [kNm]	M_{PRP} [kNm]	M_{EXP} [kNm]	Failure
T/50	502	2548.5 (+13.5%)	2484 (+10.7%)	2245	Longitudinal failure
P/60	419	2565 (+26.8%)	2461 (+20.3%)	2023	Local instability of a wing
S/50	209	1084.3 (+45.5%)	1057 (+41.8%)	745.3	Cross-section shape loss
A/50	703	2935 (-4.6%)	2905 (-5.7%)	3070	Wing failure in transversal bending

Simplified model



II order equilibrium

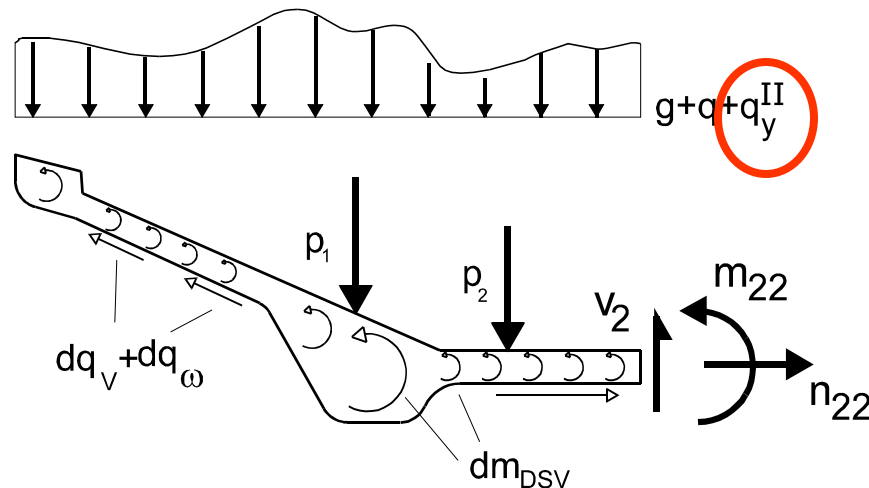


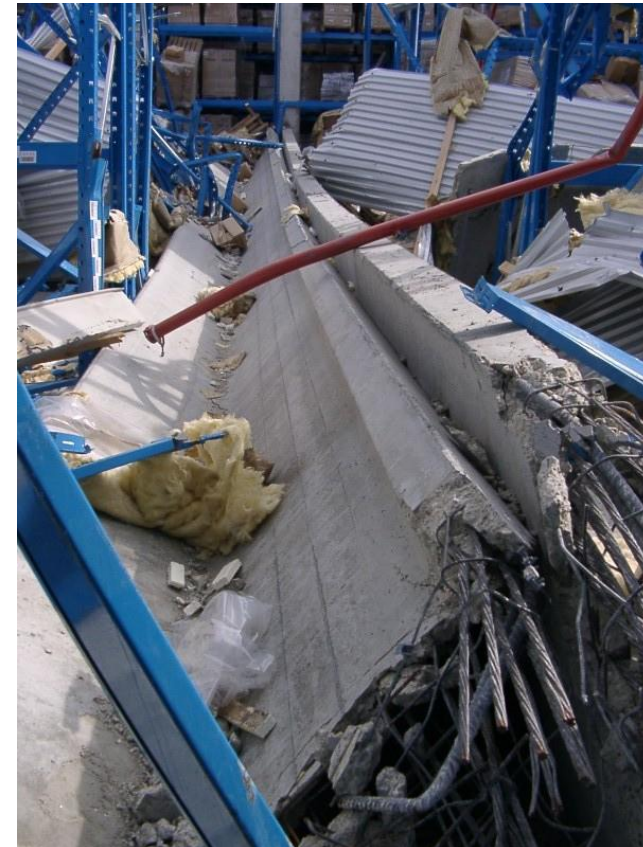
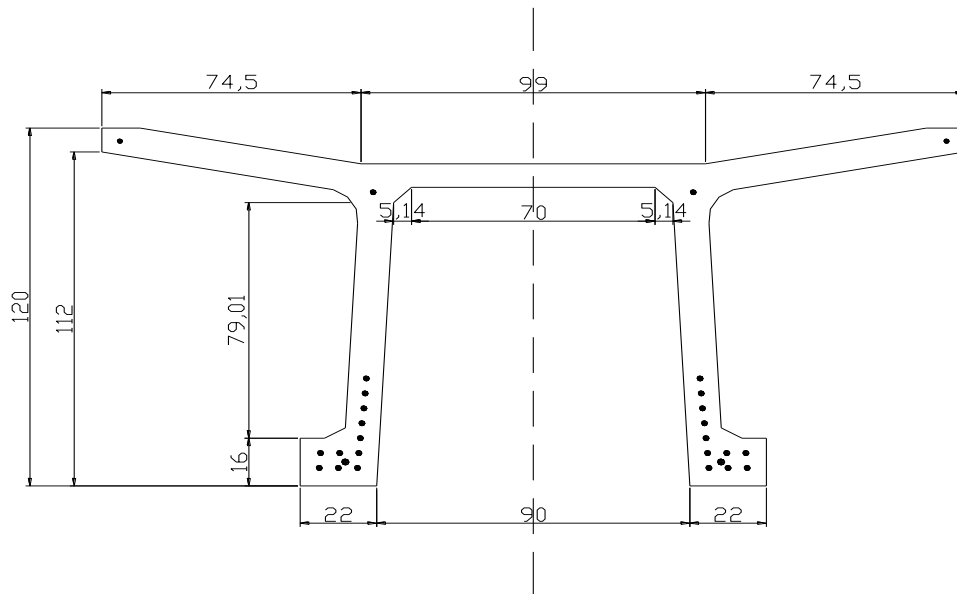
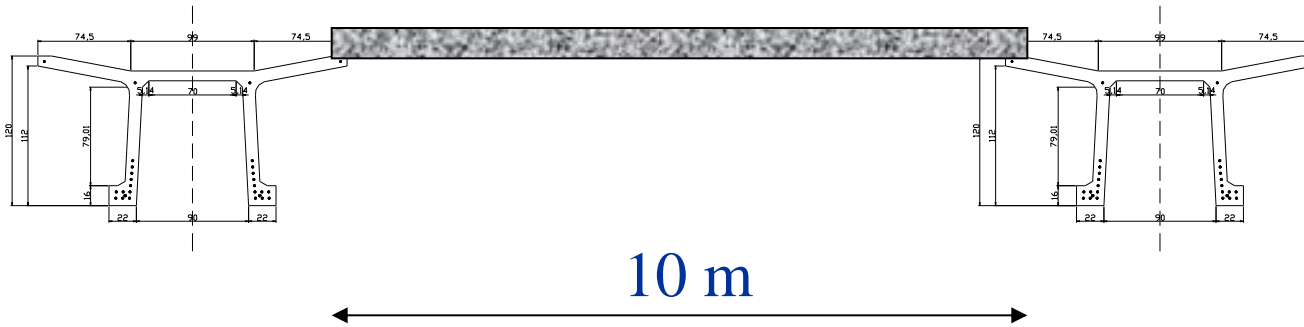
$$M^I = Pa \approx 2 \text{ N/mm} \cdot a$$

$$M^{II} = \sigma_z \cdot 10^4 \text{ mm}^2 \cdot 10^{-5} \text{ mm}^{-1} \cdot a' = 40 \text{ N/mm}^2 \cdot 0.1 \text{ mm} \cdot a' = 4 \text{ N/mm} \cdot a'$$

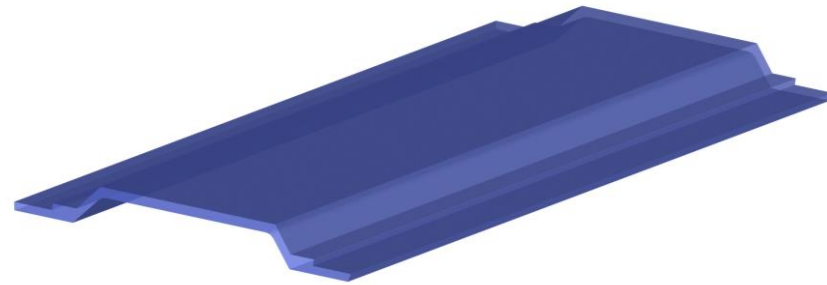
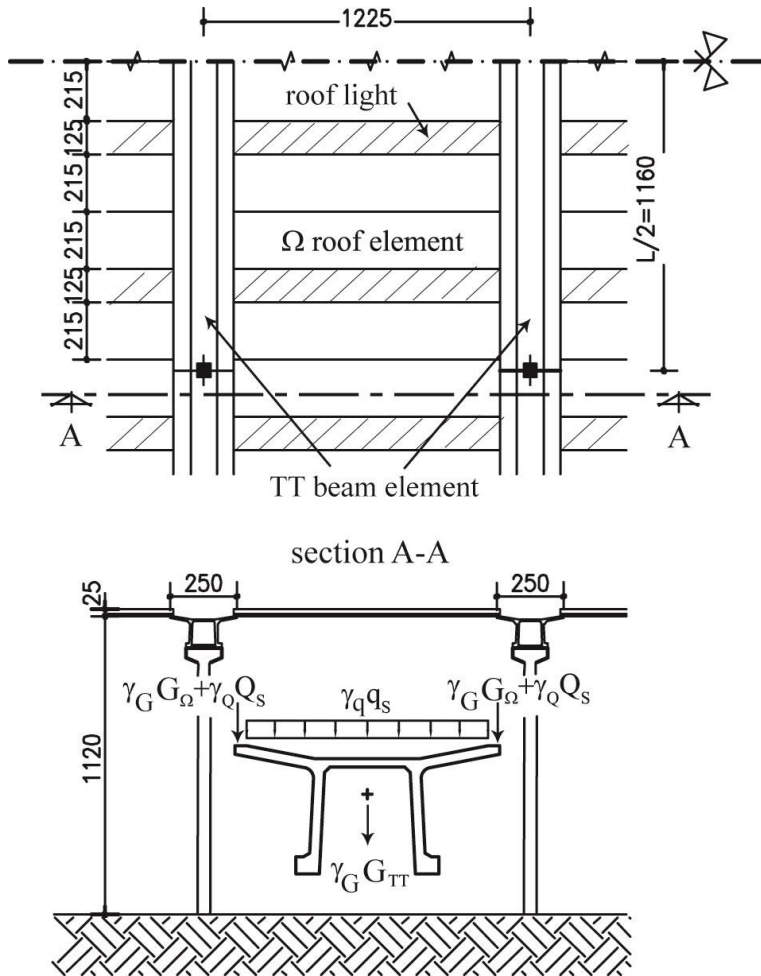
Simplified model

- By assuming plane-section model compute longitudinal stresses related to longitudinal bending (mechanical non-linearity) and the longitudinal curvature in the middle section
- Compute $q^{\text{II}} = \sigma\theta$ (geometrical non-linearity)
- By considering the cross-section perfectly stiff in its plane, compute by equilibrium the transverse stresses, taking into account also q^{II}





Roofing system

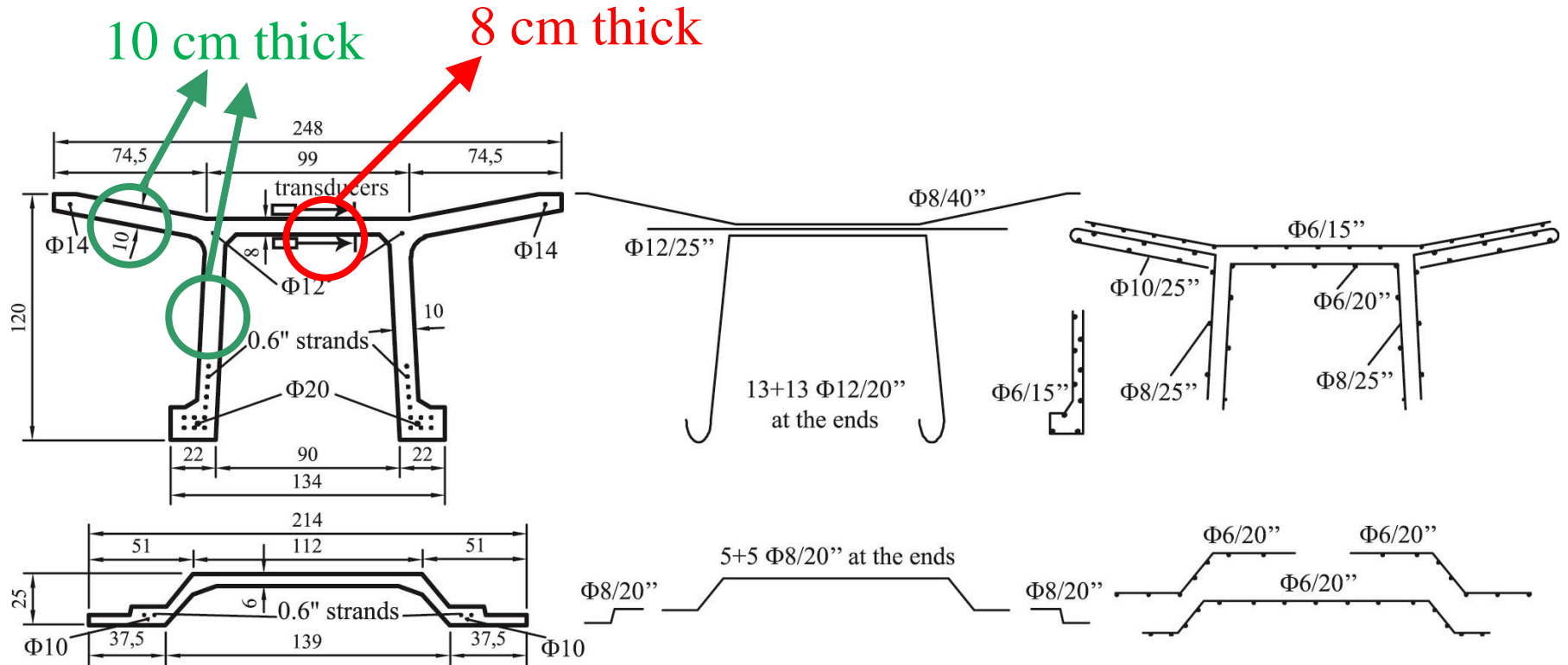


Ω roof element (10 m long)

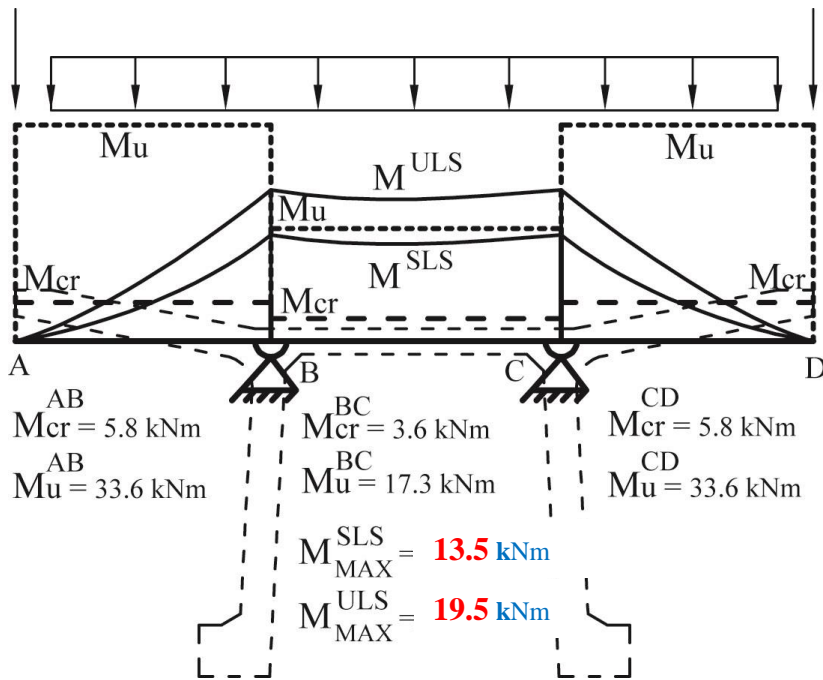


Safety factor	SLS	SLU	G_{TT} [kN/m]	G_{Ω} [kN/m]	Q_s [kN/m]	q_s [kN/m ²]
γ_G	1	1.4	12.30	9.84	6.67	1.33
γ_Q	1	1.5				
γ_q	1	1.5				

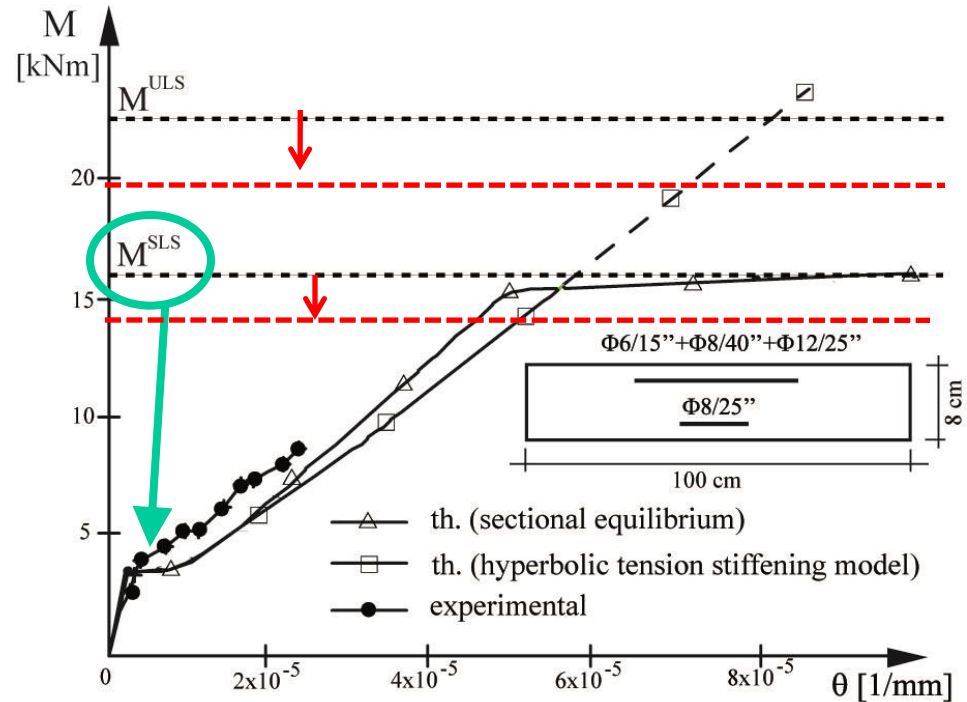
Longitudinal and transversal reinforce of TT beam element and Ω roof element



TT beam element



Transversal equilibrium
bending moments
(characteristic values)

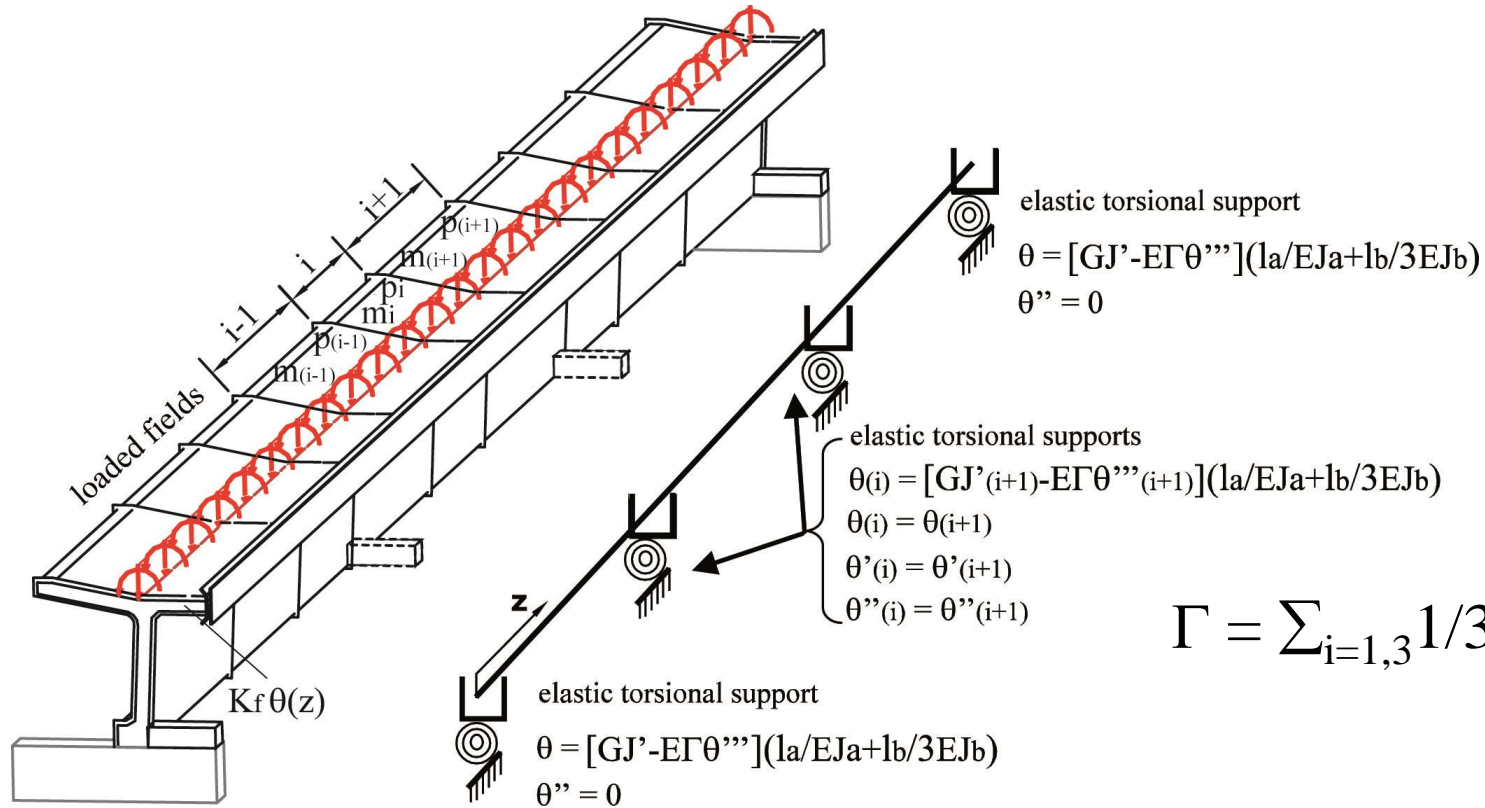


Experimental vs. predicted
moment-curvature relationship
(upper TT beam element plate)

Situation after structure breakdown



TT beam element: torsional behaviour



$$\Gamma = \sum_{i=1,3} 1/36 a^3 b^3$$

$$\frac{d^4 \vartheta(z)}{dz^4} - \frac{GJ_T (\vartheta')}{E\hat{\Gamma}} \frac{d^2 \vartheta(z)}{dz^2} + \frac{K_f (J_f (\vartheta))}{E\hat{\Gamma}} \vartheta(z) = \frac{m_t}{E\hat{\Gamma}}$$

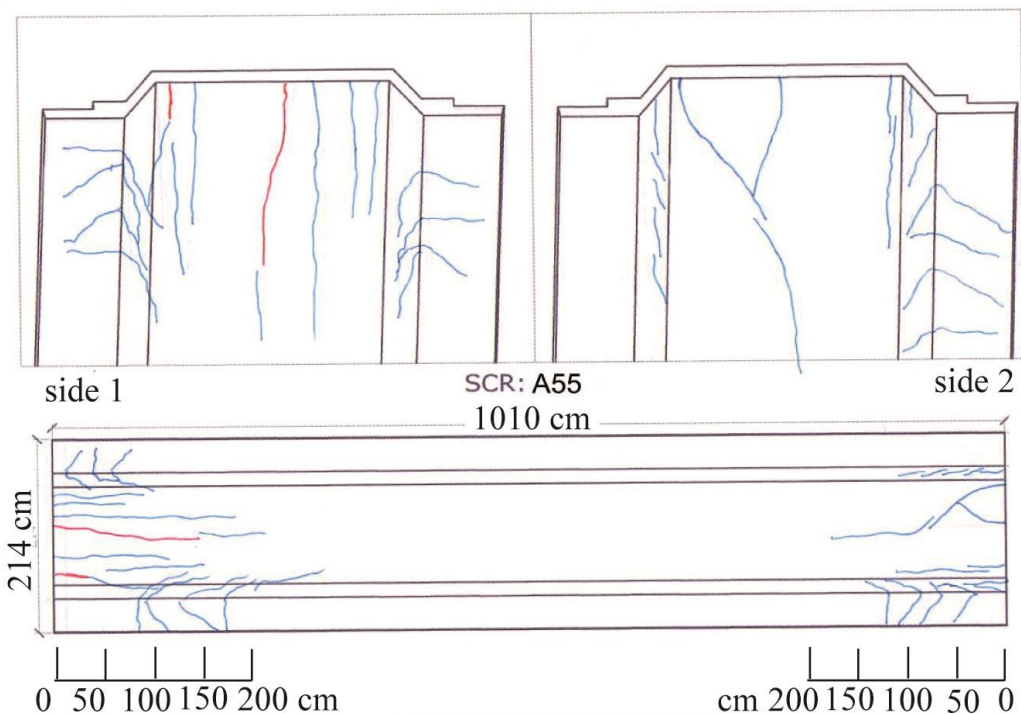
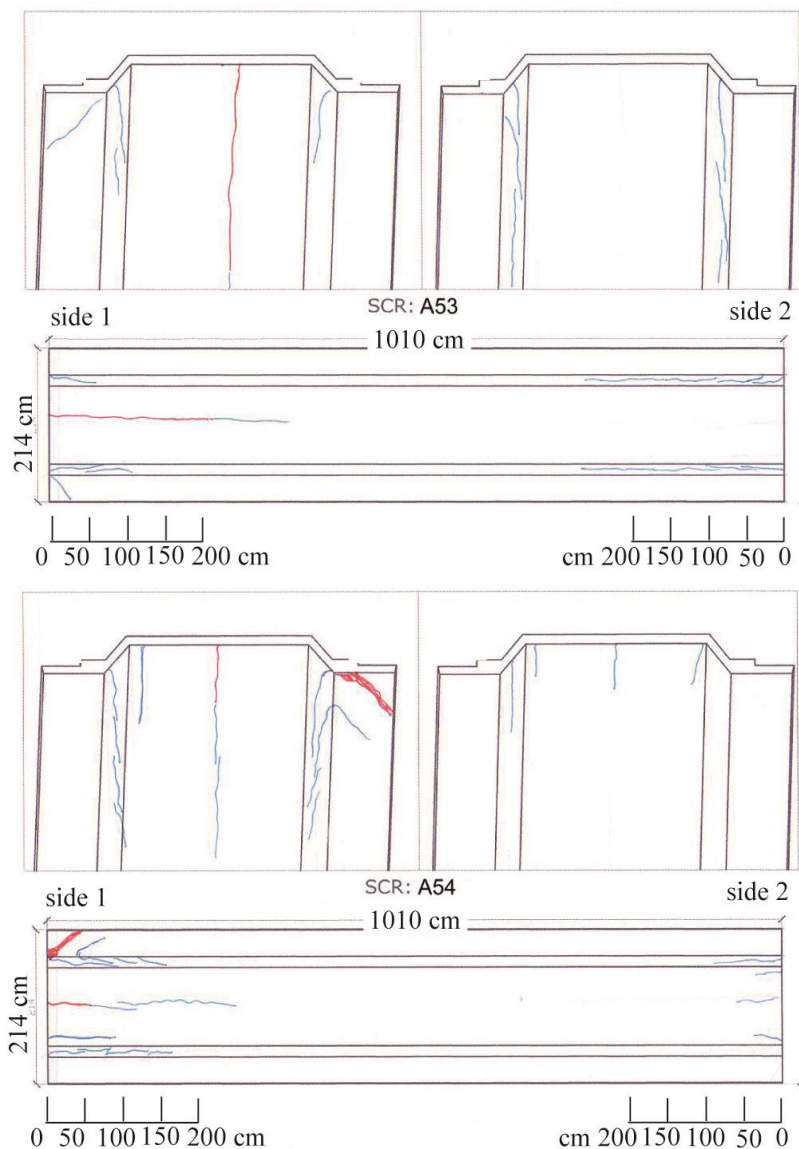
$$\lambda_{1,2,3,4} = \pm \sqrt{\frac{\frac{GJ_T}{E\hat{\Gamma}} \pm \sqrt{\left(\frac{GJ_T}{E\hat{\Gamma}}\right)^2 - 4 \frac{K_f}{E\hat{\Gamma}}}}{2}}$$

$$\vartheta_{(i)}(z) = A_{(i)} \cdot e^{\lambda_{1(i)} z} + B_{(i)} \cdot e^{\lambda_{2(i)} z} + C_{(i)} \cdot e^{\lambda_{3(i)} z} + D_{(i)} \cdot e^{\lambda_{4(i)} z} + \frac{m_{t(i)}}{K_{f(i)}}$$

Ω roof element

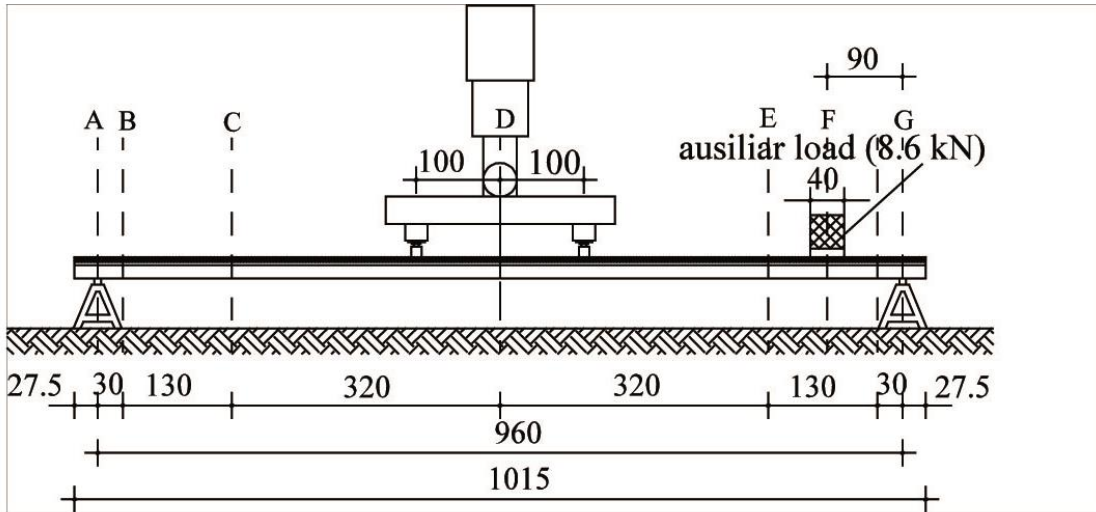
Transversal deformability problems interested also the Ω roof elements placed on TT beams:

- not negligible deflection
- significant crack pattern

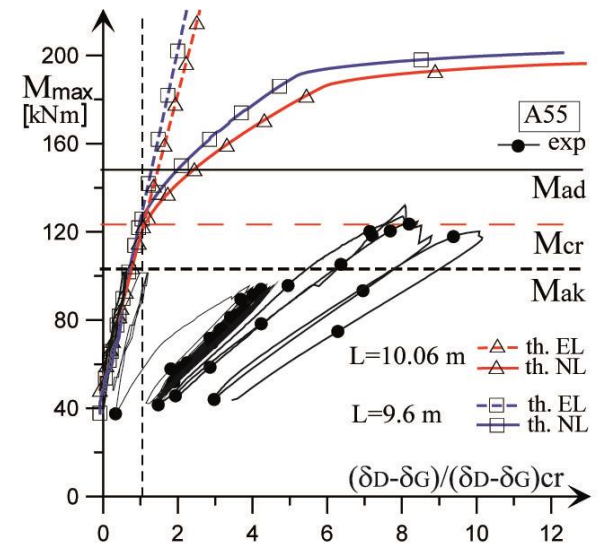
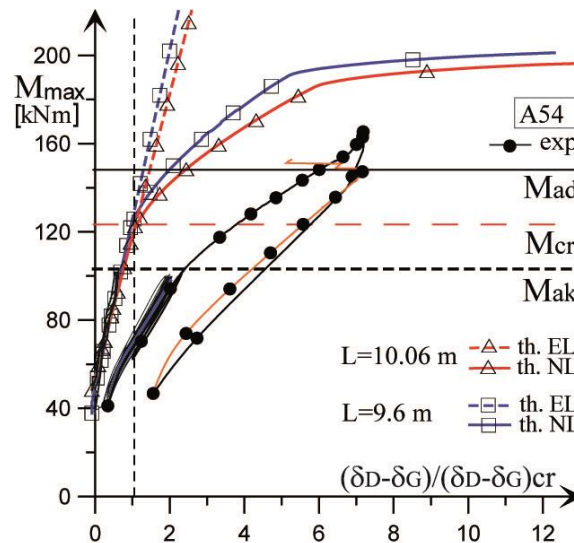
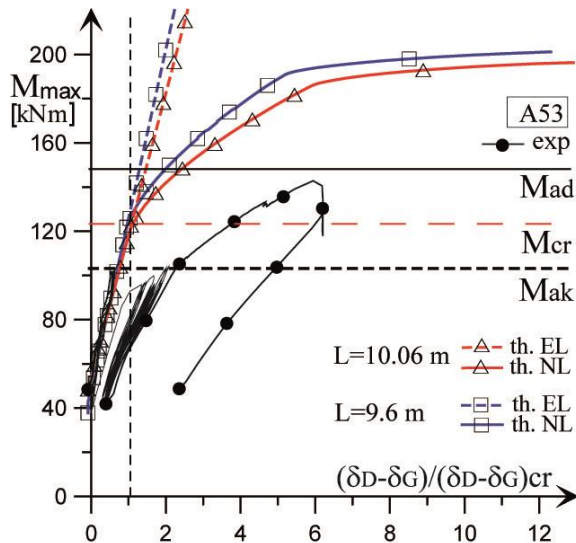


crack pattern of in-situ Ω roof elements

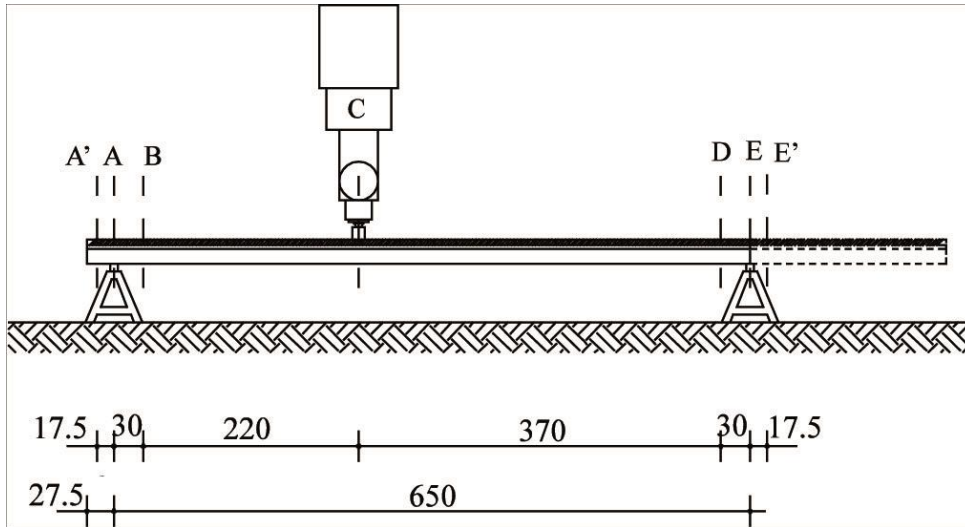
Ω roof element: laboratory tests



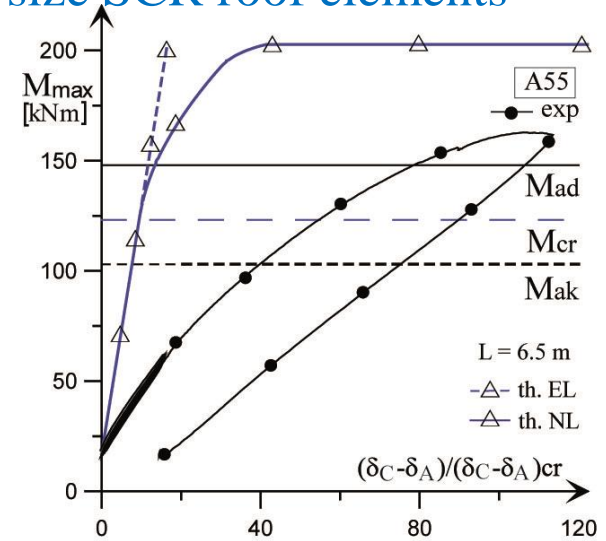
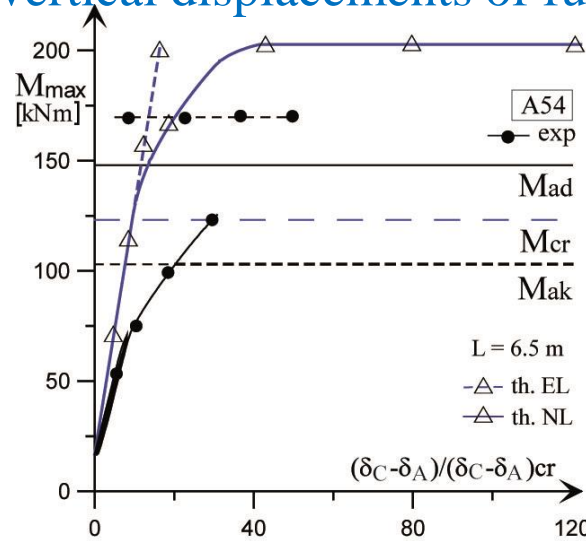
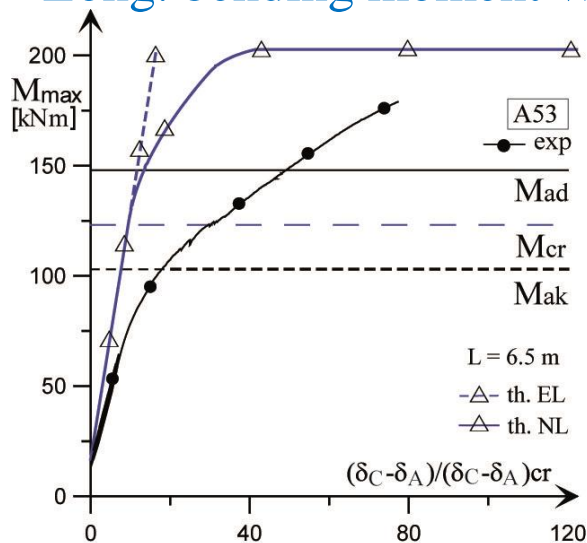
Long. bending moment vs. vertical displacements of full size SCR roof elements



Ω roof element: laboratory tests



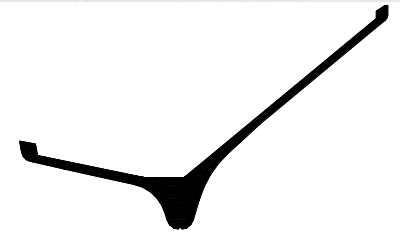
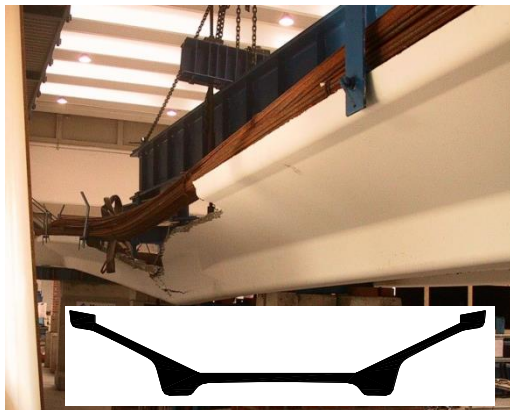
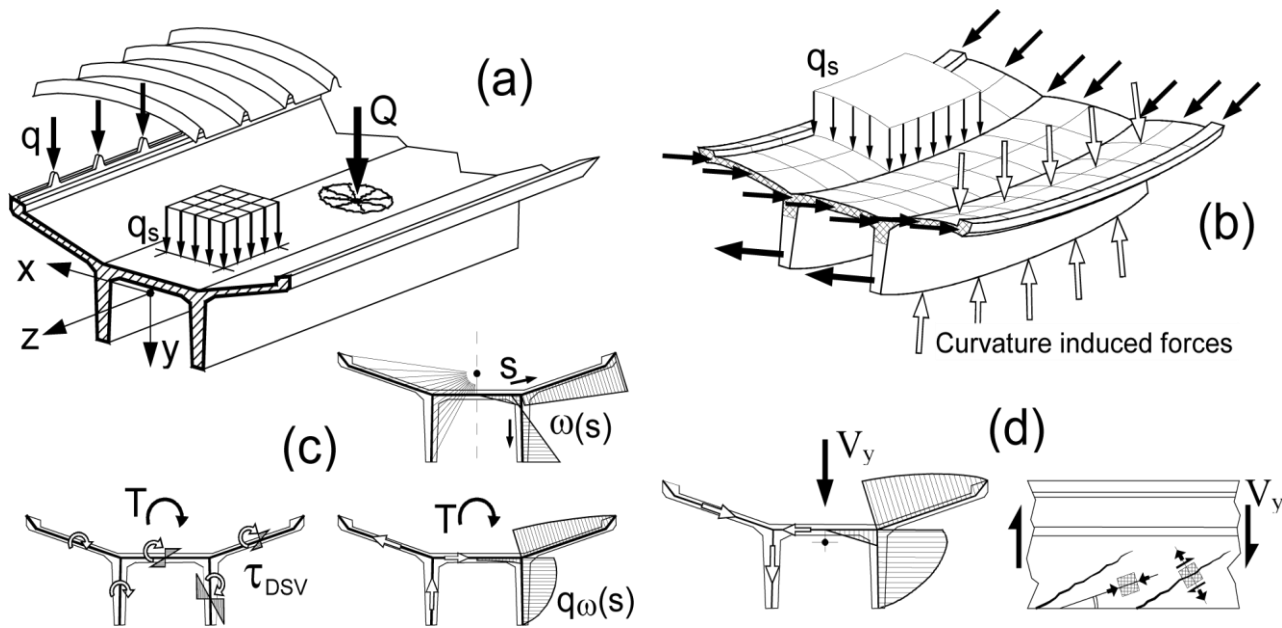
Long. bending moment vs. vertical displacements of full size SCR roof elements



Outline

- ✓ FRC as transverse reinforcement:
 - σ -w constitutive law
 - classification and “structural specimen”
 - fibre alignment
 - second order effects
- ✓ FRC for local bending
 - self stresses due to shrinkage and thermal effects
 - which structural ductility
 - stress diffusion and size effects
- ✓ Advanced materials for light composite structures
 - opportunities
 - complex resistant mechanisms
 - open question and unexplored potentialities

FRC to substitute transverse reinforcement



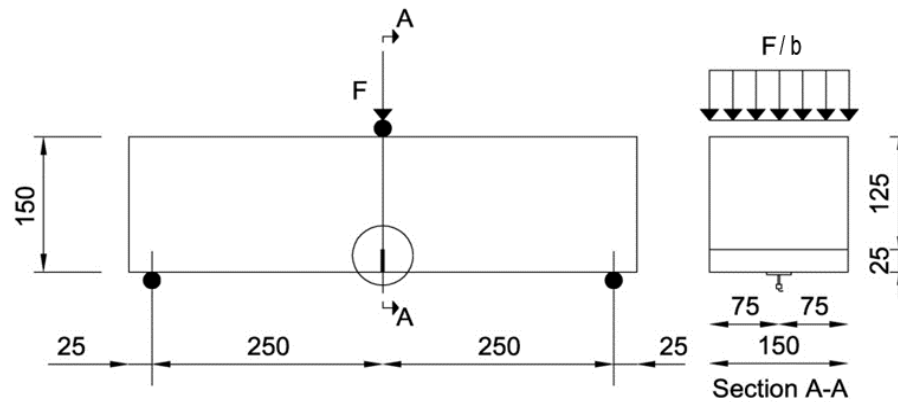
Classification for FRC market

Reference test

EN 14651

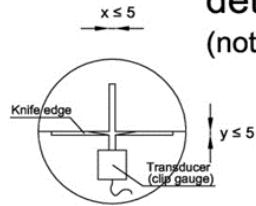
$h_{sp} = 125 \text{ mm}$

$b = 150 \text{ mm}$

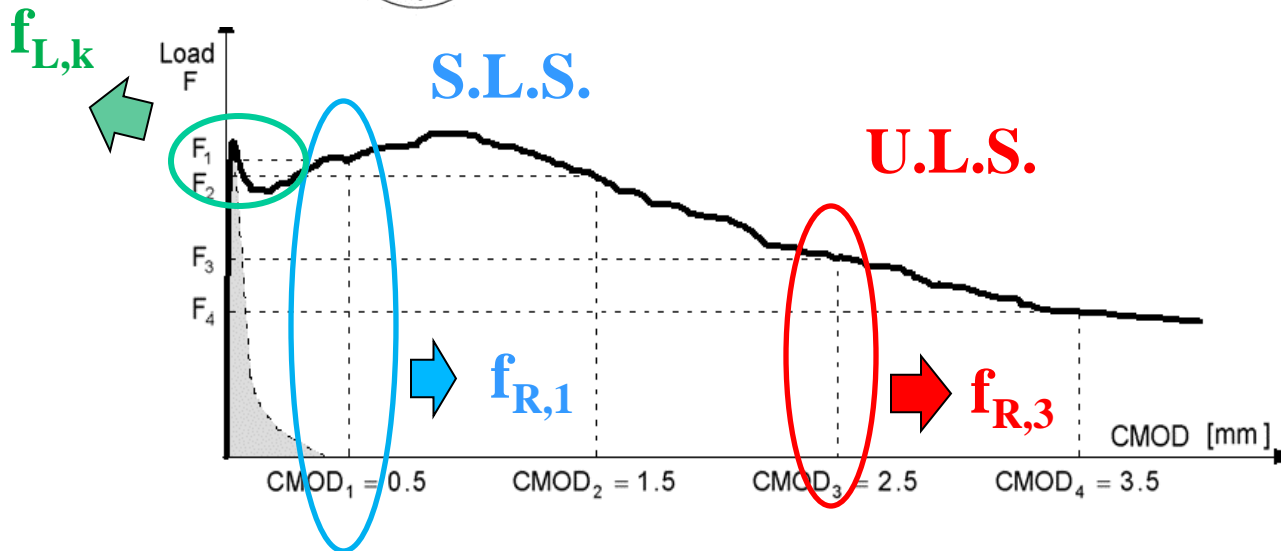


all sizes in mm

detail
(notch)



$$f_{R,j} = \frac{3 F_j l}{2 b h_{sp}^2}$$



Performance based design

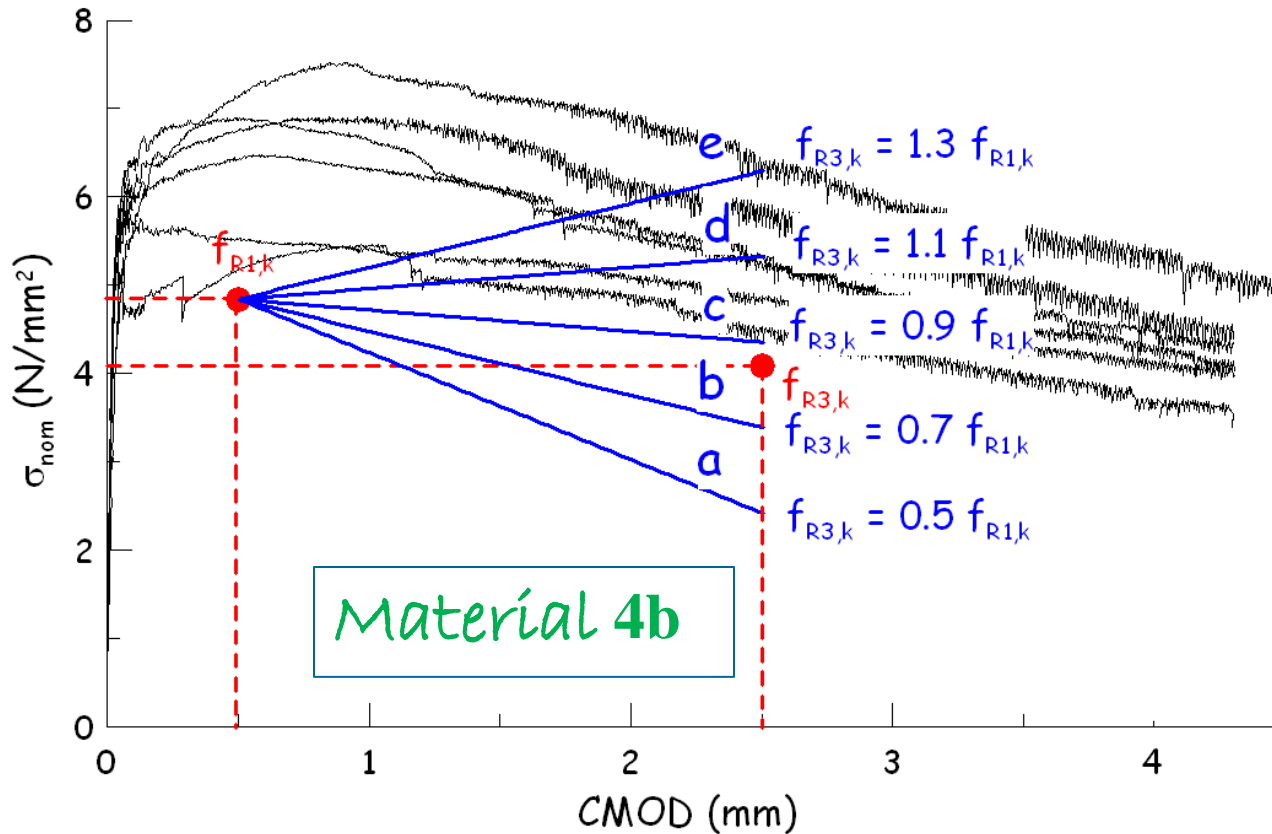
cement 425: 472 kg
 fly ash: 45 kg
 water: 200 l (w/b =0.39)
 superplast. 1.3%

fine sand 0/4 850kg
 coarse sand 4/8 886 kg
hooked-end fibres 65/35 50 kg

slump flow diameter: 690 mm
 T50 2 sec
 V-funnel time (0 min) 3.5 sec
 V-funnel time (5 min) 4 sec
 L-box (standard) h2/h1 = 1

Classification

f_{R1k} 1.0; 1.5; 2.0; 2.5; 3.0; 4.0; 5.0; 6.0; 7.0; 8.0 [MPa]

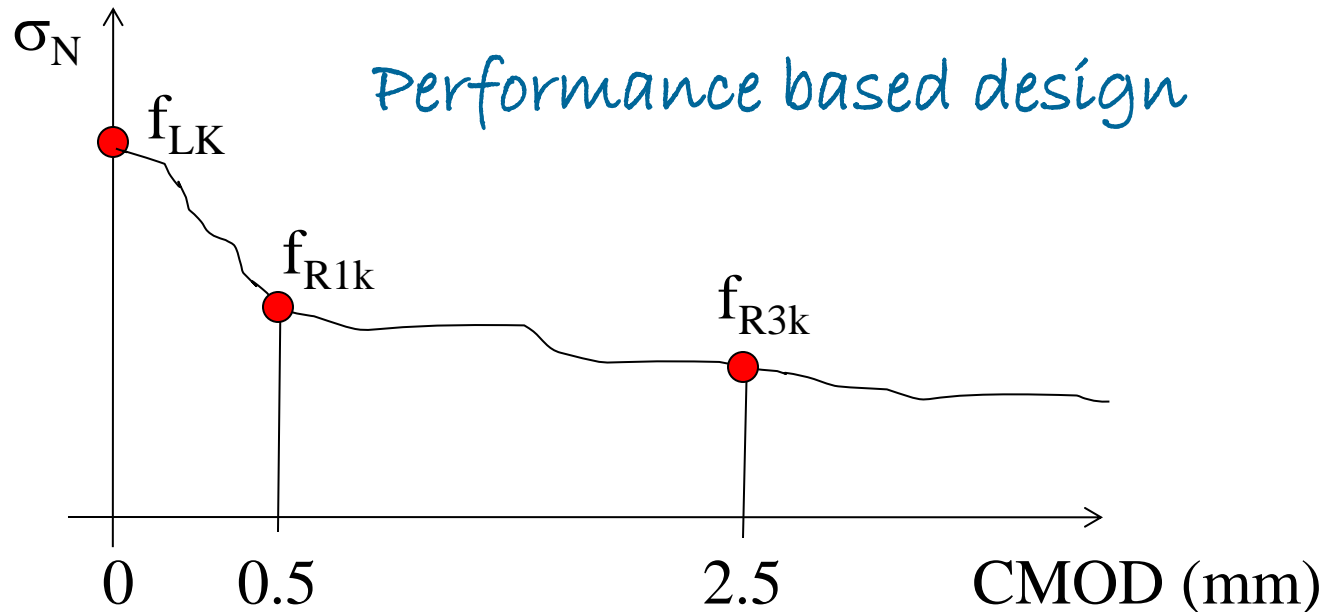


$$f_{eq,k} = f_{eq,av} - ks$$

$$n = 6: k = 1,87$$

	strength [Mpa]	st. dev [Mpa]
$f_{L,av}$	5,43	0,47
f_{Lk}	4,55	
$f_{R1,av}$	6,32	0,79
f_{R1k}	4,84	
$f_{R3,av}$	5,32	0,66
f_{R3k}	4,08	

Minimum performance for a FRC

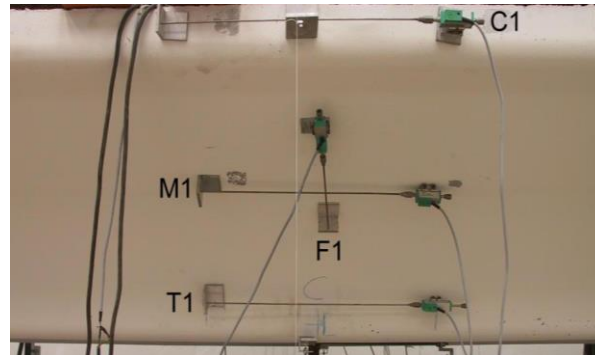
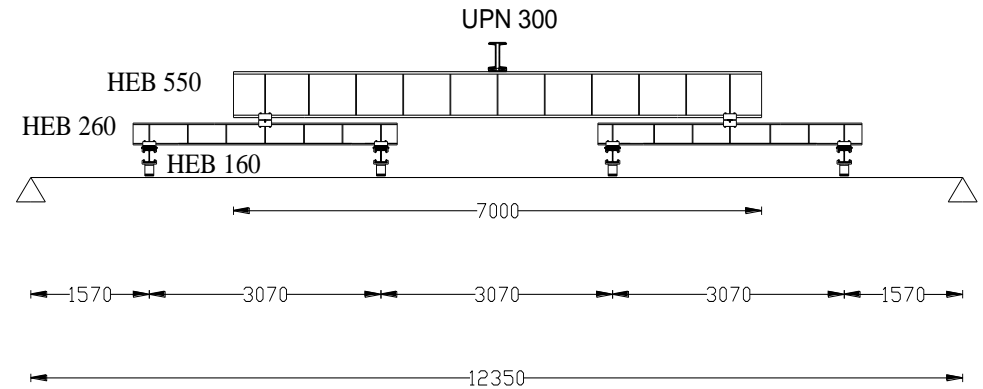


(5) Fibre reinforcement can substitute (also partially) conventional reinforcement at ultimate limit state if the following relationships are fulfilled:

$$f_{R1k}/f_{LK} > 0.4; \quad f_{R3k}/f_{R1k} > 0.5$$

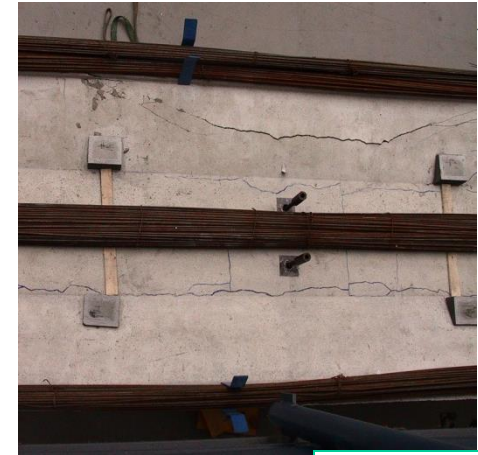
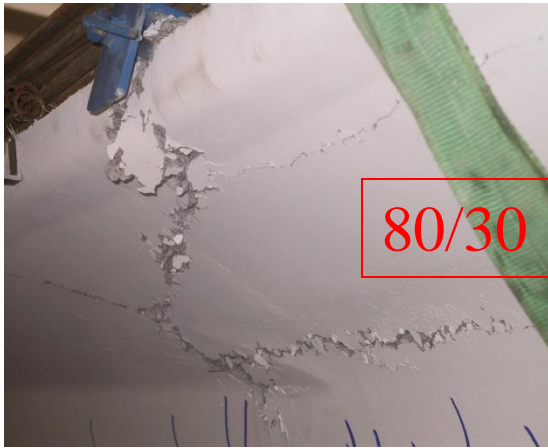
Bending tests on roof elements

by di Prisco, Failla, Plizzari, 2003

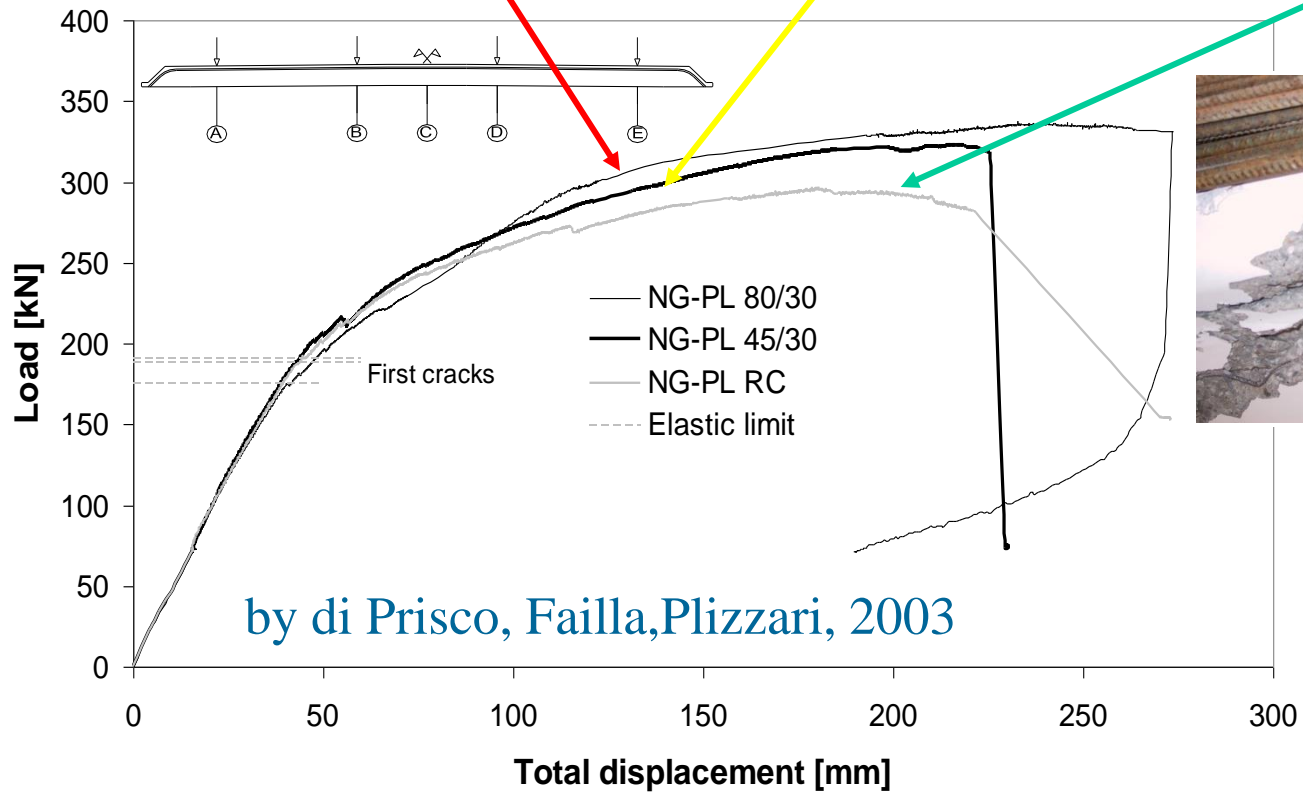


$l_{cs,wing}$

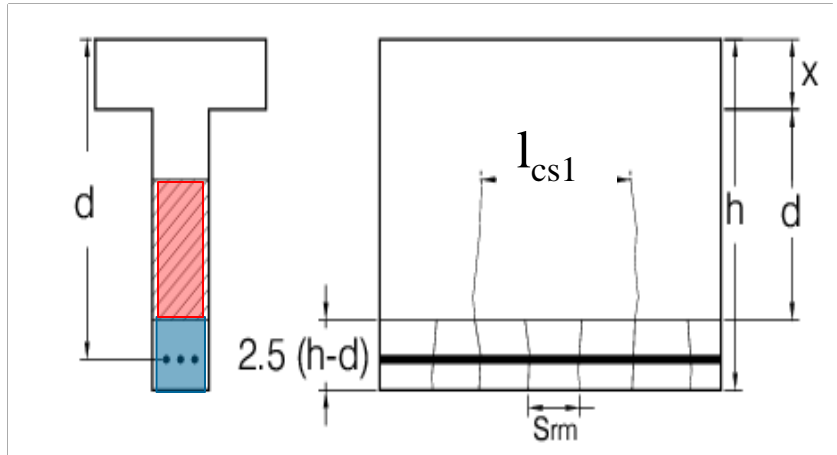
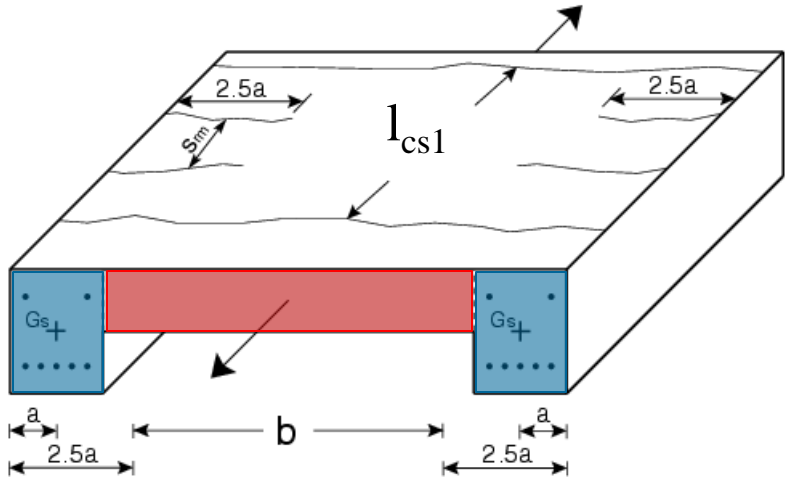
$l_{cs,slab}$



COMPARISON - SECTION C
Load - Total displacement



✓ the bridge ... of the characteristic structural length

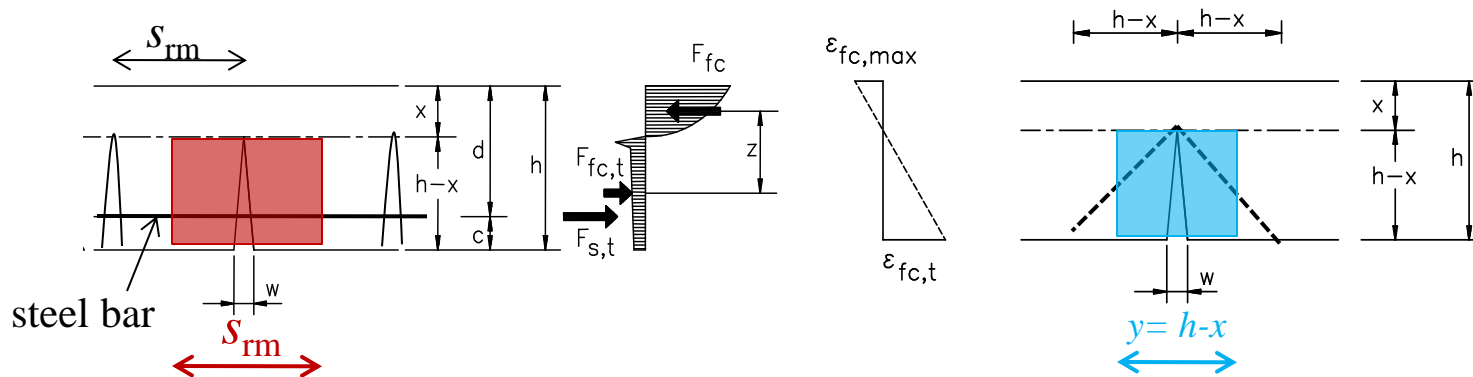


✓ the bridge ... of the characteristic structural length

The characteristic structural length

Plane section approach

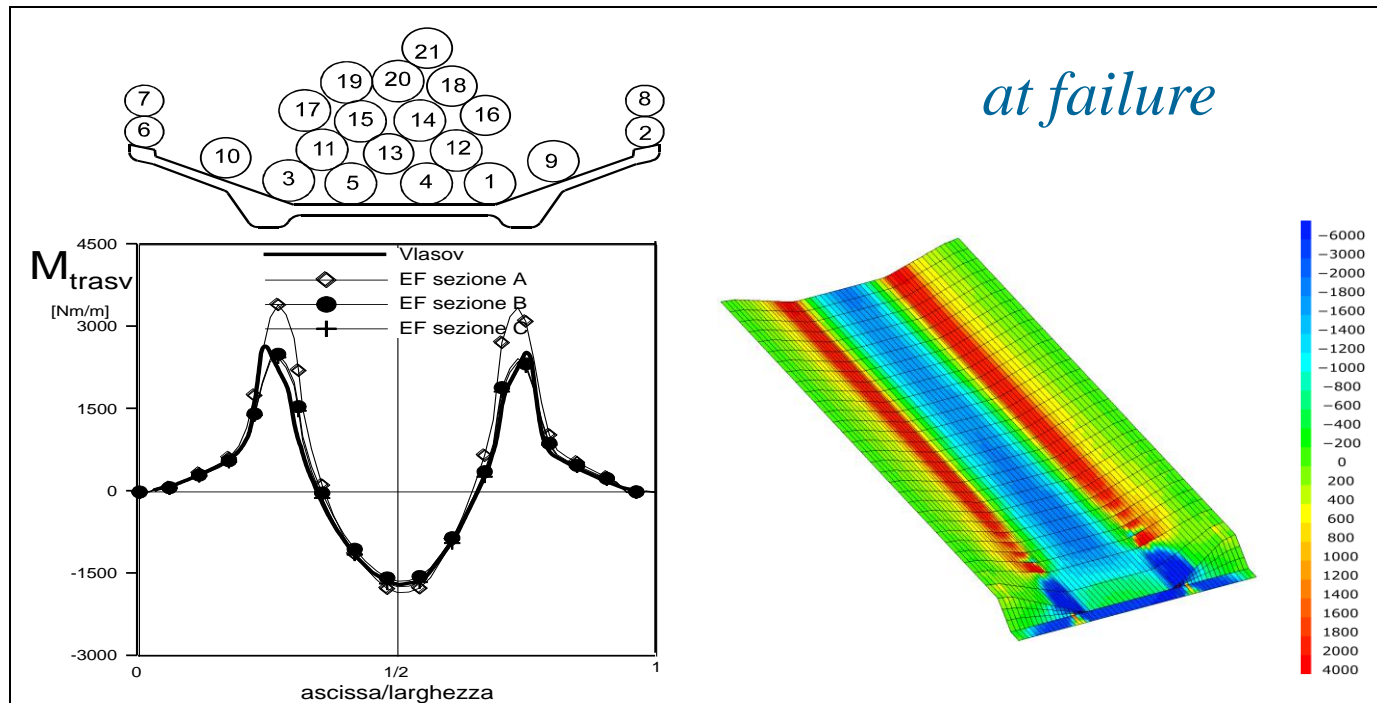
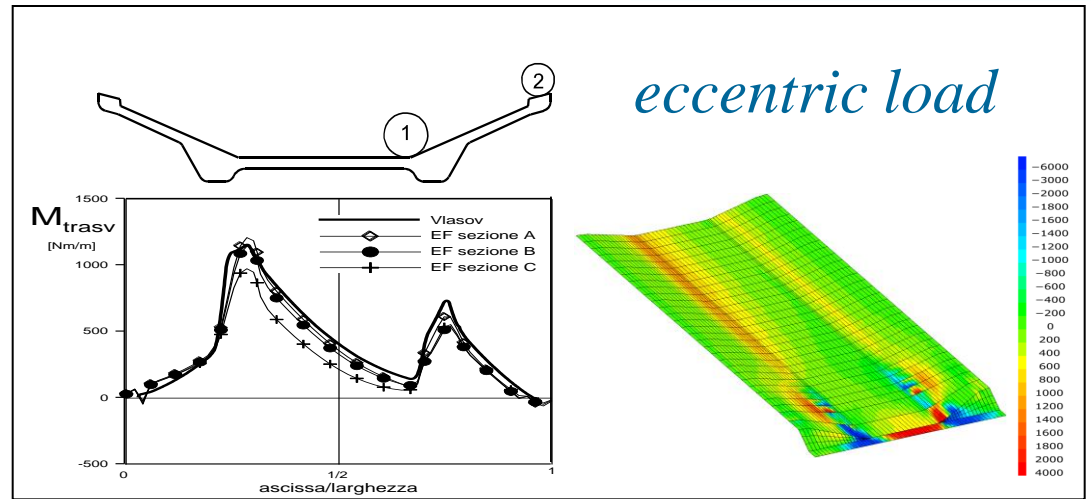
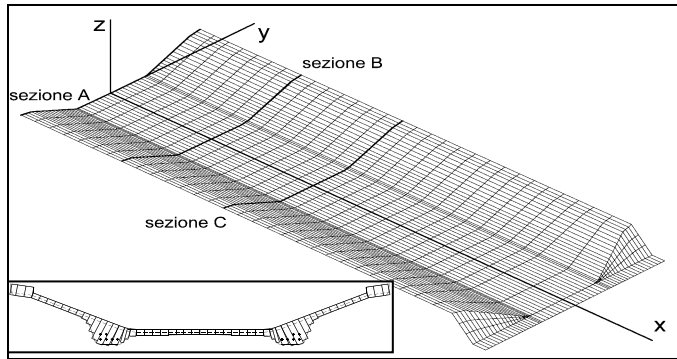
$$l_{cs} = \min\{s_{rm}, y\}$$

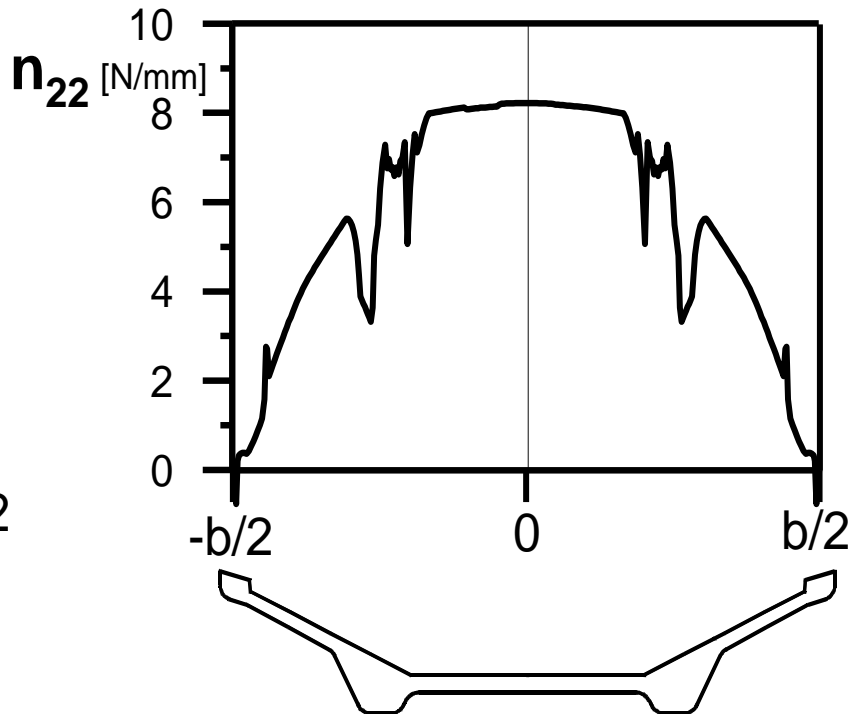
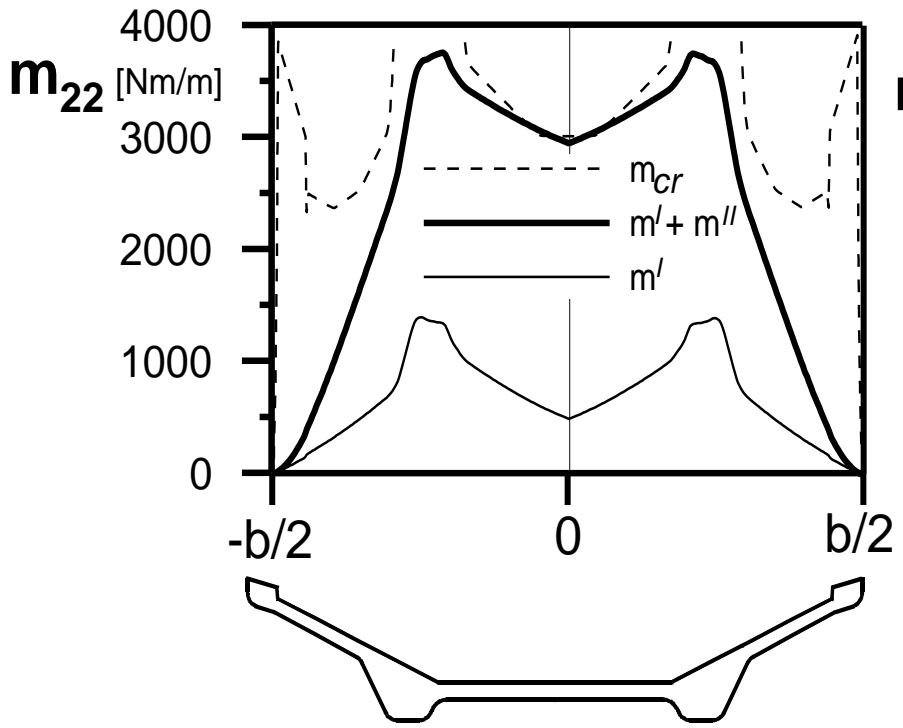
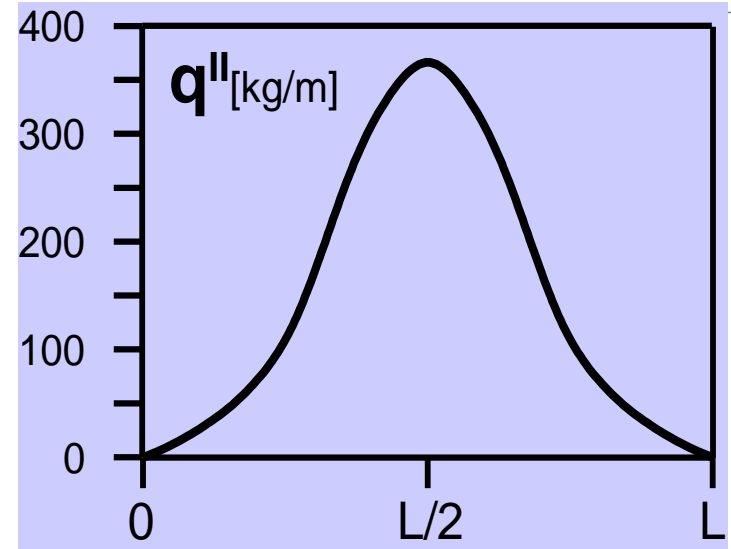
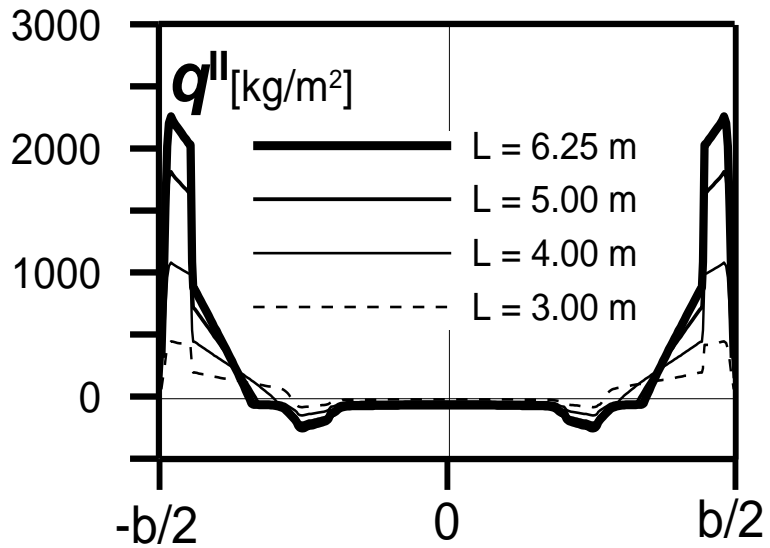


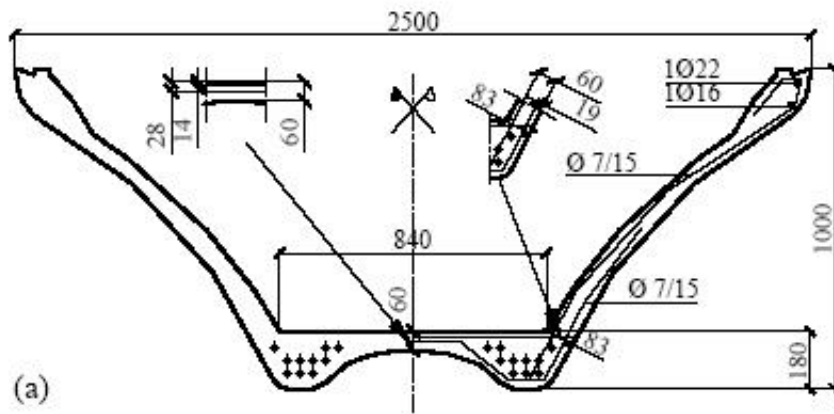
N.B. In sections without traditional reinforcement under bending or under combined tensile – flexural and compressive – flexural forces with resulting force external to the section, $y = h$ is assumed. The same assumption can be taken for slabs.

F.E. approach: $l_{cs} = \textit{localization limiter}$

elastic check by FE



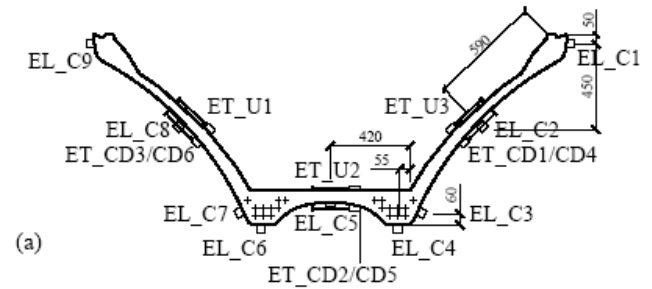




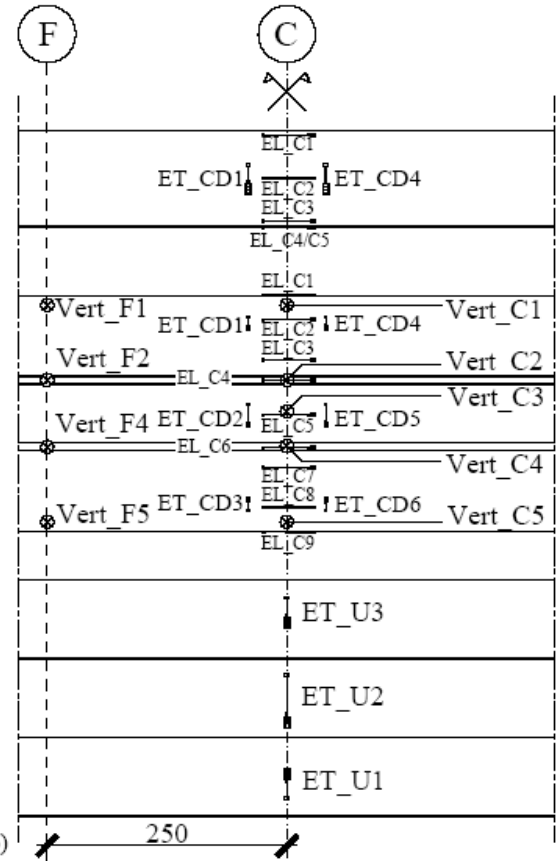
(a)



(b)



(a)



(b)

Figure 2. Instrumental equipment in the central segment: (a) cross section view; (b) longitudinal projections.

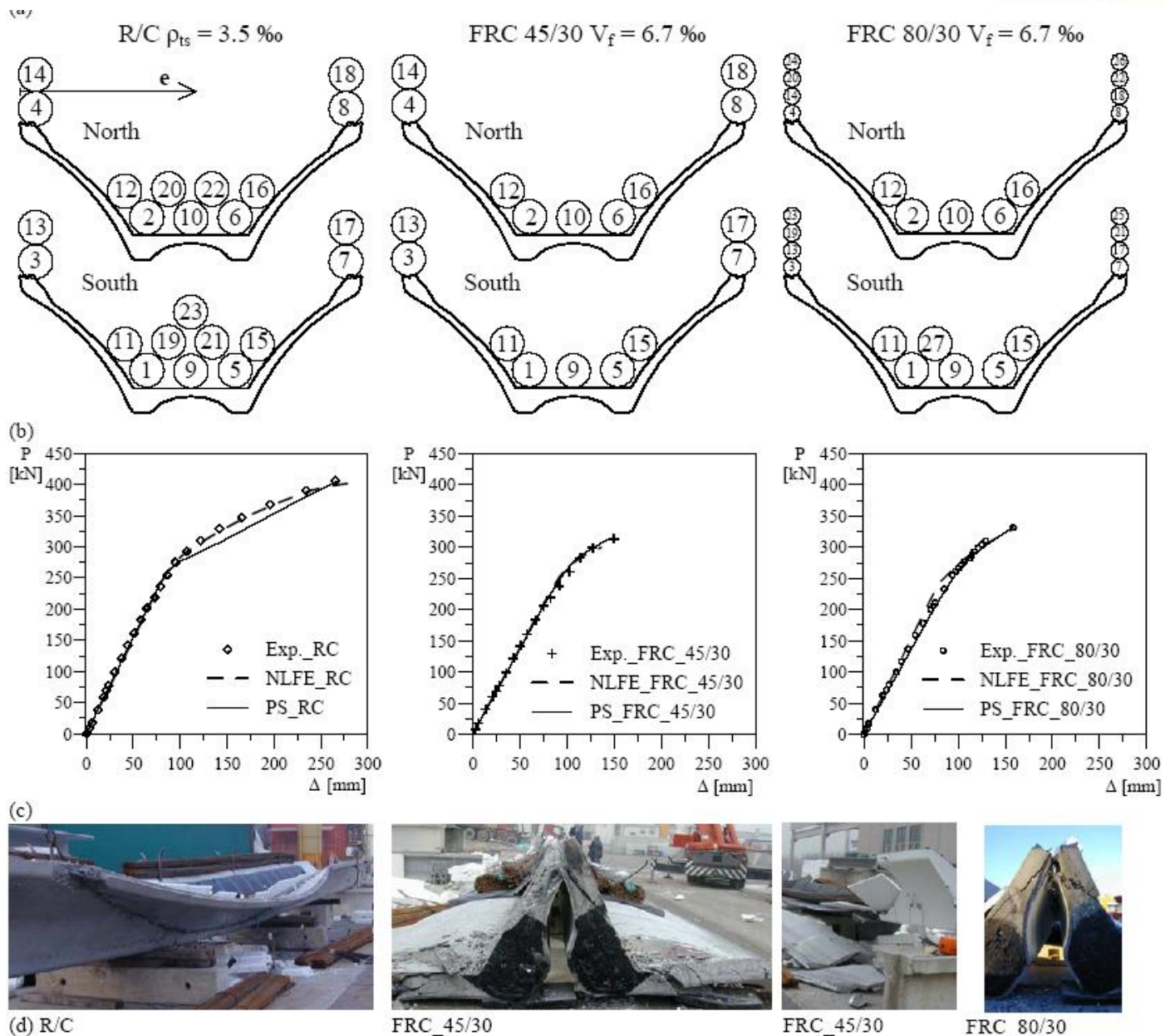
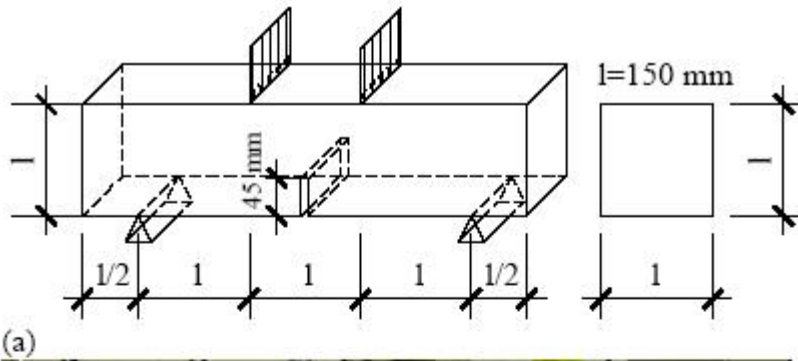
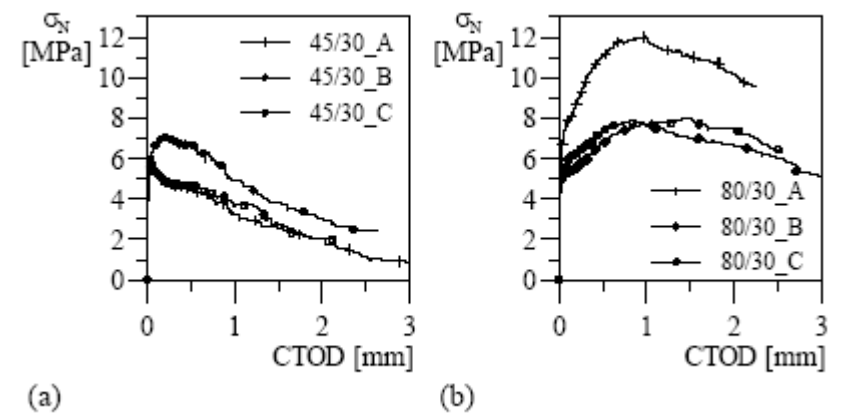


Figure 3. Structural tests: (a) typical loading situation view; (b) steel bundle location, (c) total load vs. midspan deflection measured with bottom LVDTs; (d) collapse views.



(b) Figure 4. UNI test: (a) geometry and test set-up; (b) specimen image during testing.



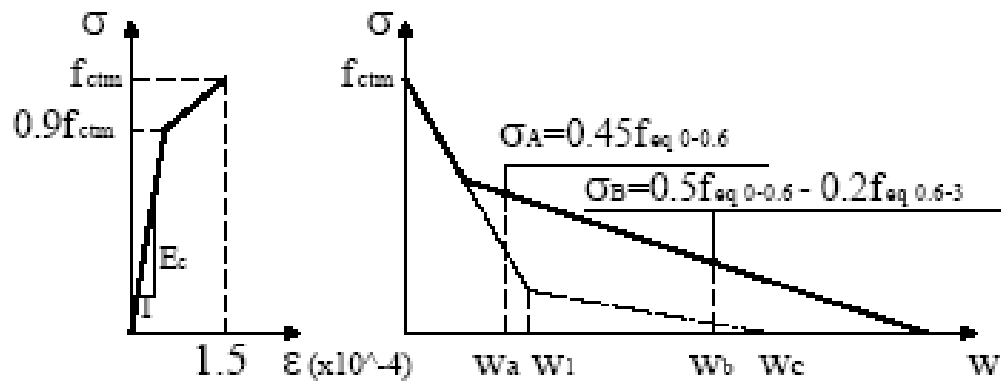
(a) (b) Figure 5. Load vs. CTOD for UNI tests: (a) 45/30; (b) 80/30

Table 1. Experimental mechanical characteristics of materials.

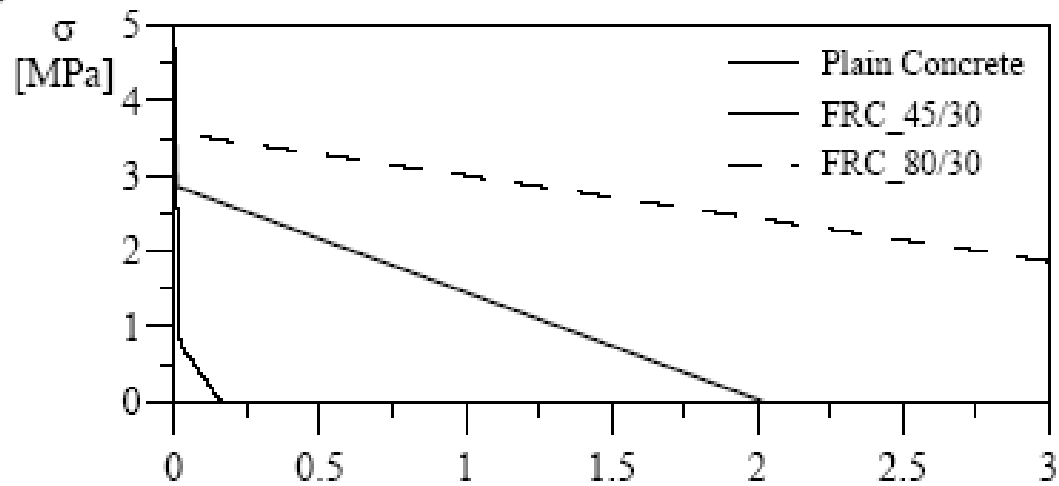
	R_{cm}	$f_{if,m}$	$f_{eq0-0.6m}$	$f_{eq0.6-3m}$	f_{yk}	f_{ptk}
	MPa	MPa	MPa	MPa	MPa	MPa
R/C	82.58	-	-	-	500	1860
45/30	75.65	5.22	5.44	2.80	-	1860
80/30	73.20	5.22	7.56	8.12	-	1860

Table 2. Computed mechanical characteristics of materials.

	E_c	ν	f_c	f_{ct}	σ_a	w_a	σ_b	w_b
	MPa		MPa	MPa	MPa	mm	MPa	mm
R/C	39193	0.2	68.54	5.02	-	-	-	-
45/30	38176	0.2	62.79	4.70	2.45	0.3	0.31	1.8
80/30	37801	0.2	60.76	4.70	3.40	0.3	2.55	1.8

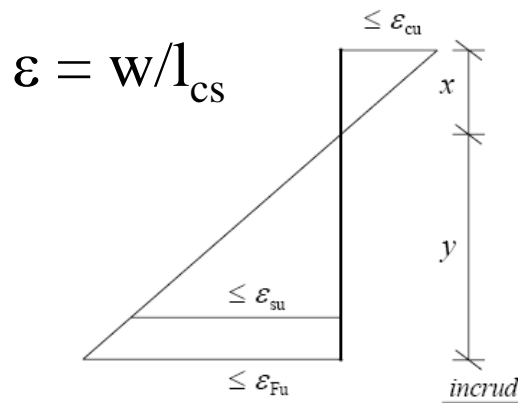
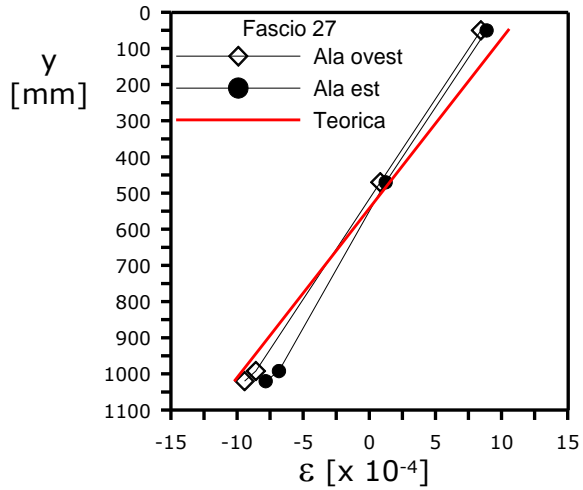


(a)

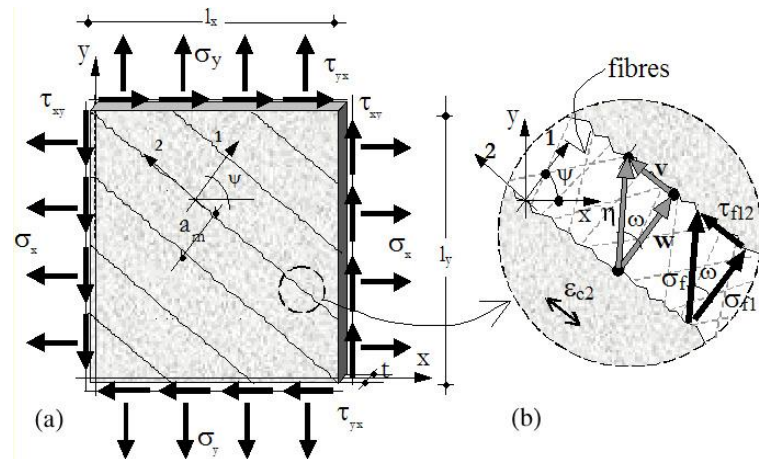
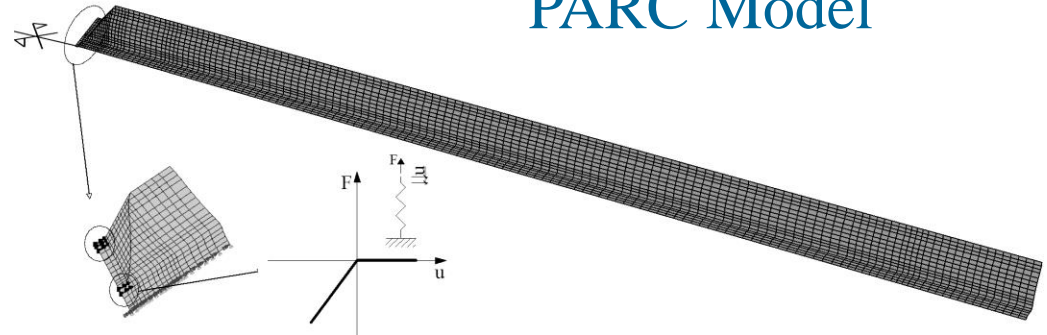


Two theoretical approaches

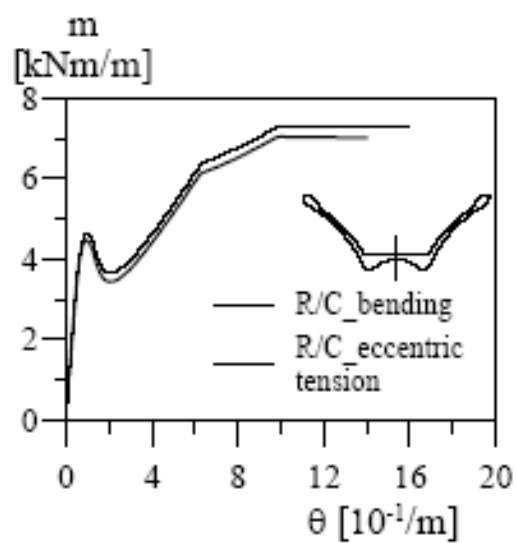
Plane Section



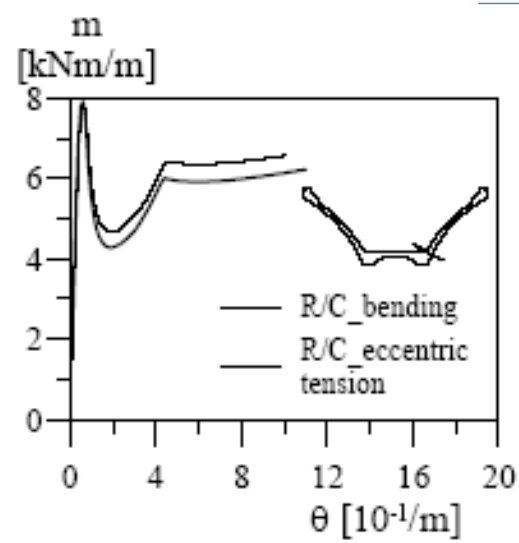
Finite Element & PARC Model



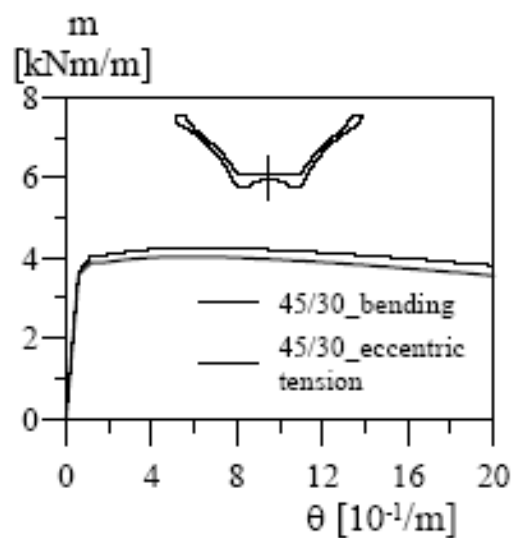
by Belletti, Cerioni, Iori, 2002



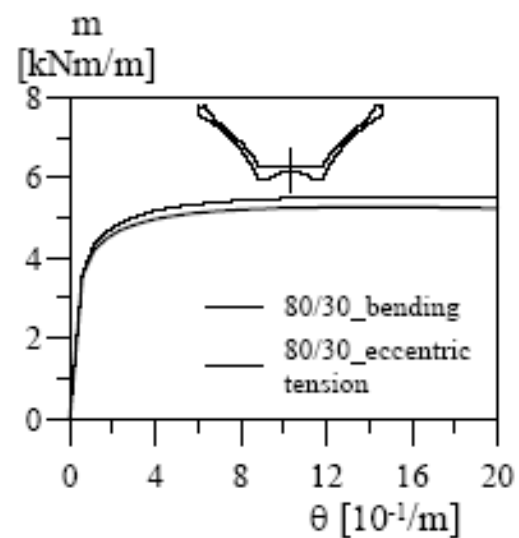
(a)



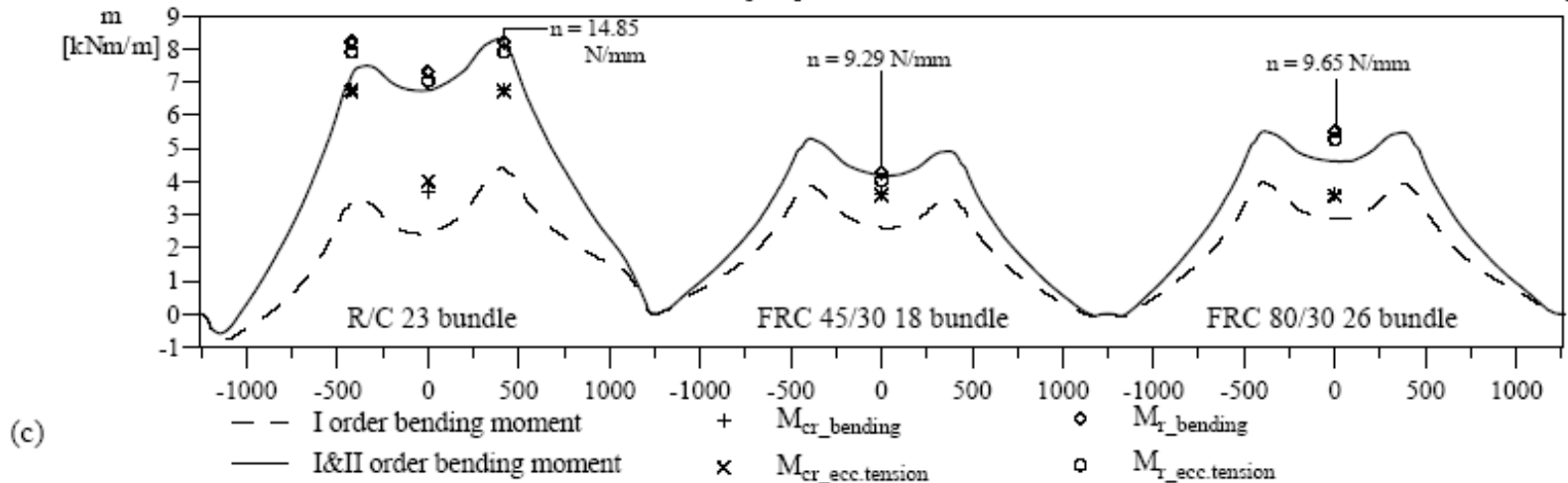
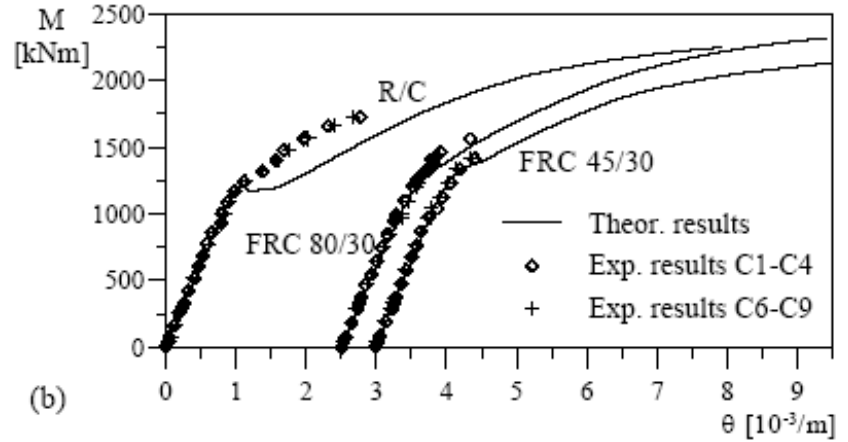
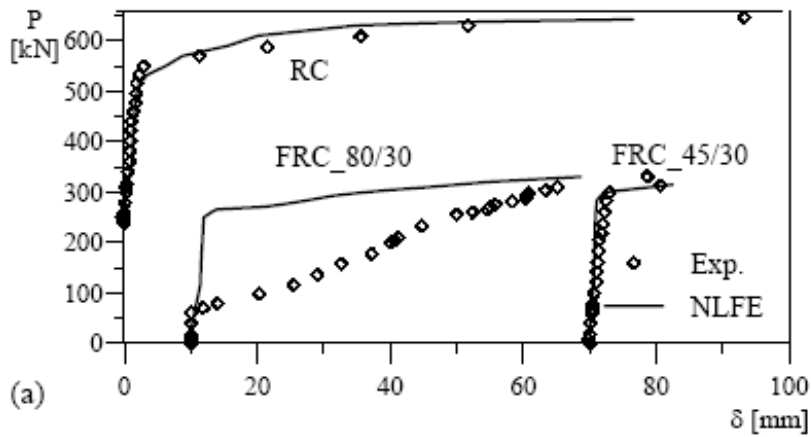
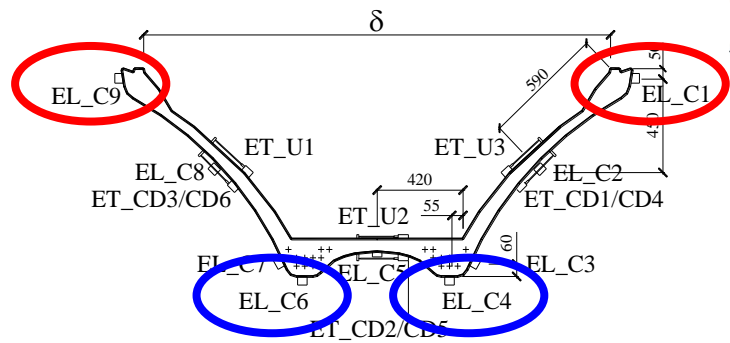
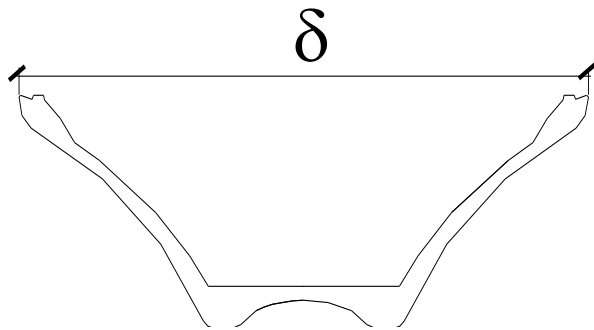
(b)



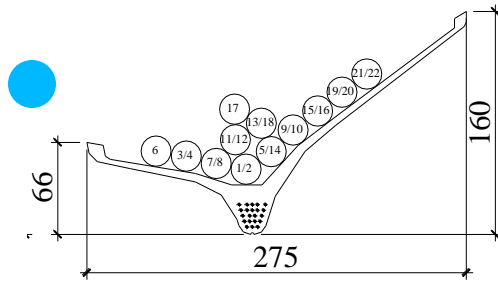
(c)



(d)



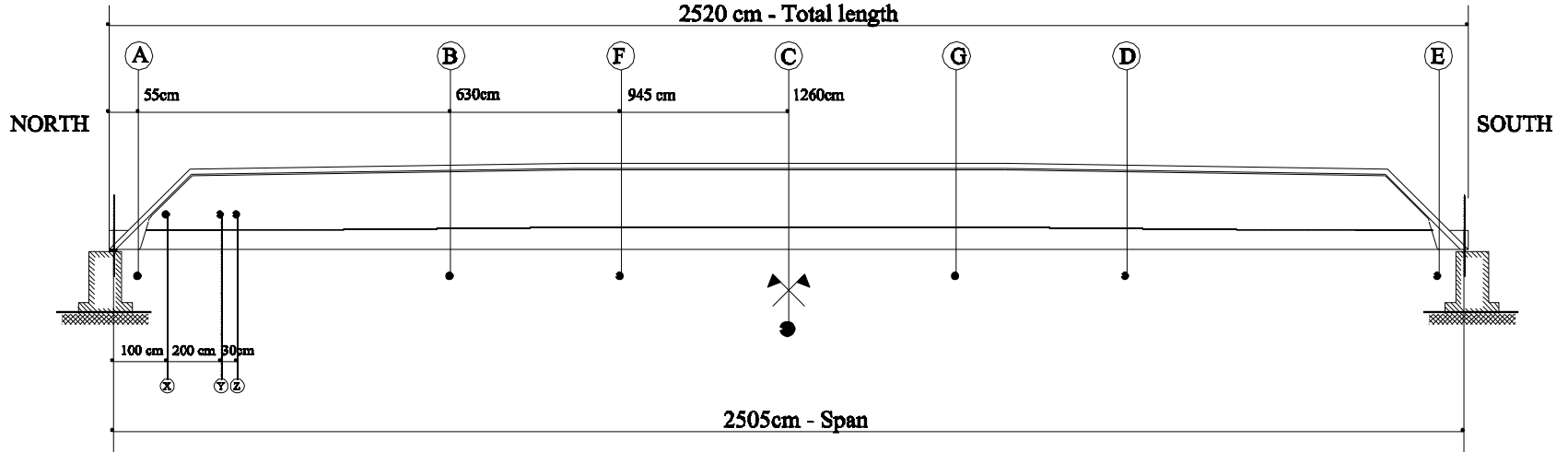
Real-size structures



Element	Age [days]	Fibre	R_{cm} [MPa]	Element weight [kg]
P 70 00	17	-	71.20	22840
F 95 45	63	45/30	92.70	18740
F 60 45	45	45/30	62.25	18820
F 110 80	75	80/30	109.90	18480

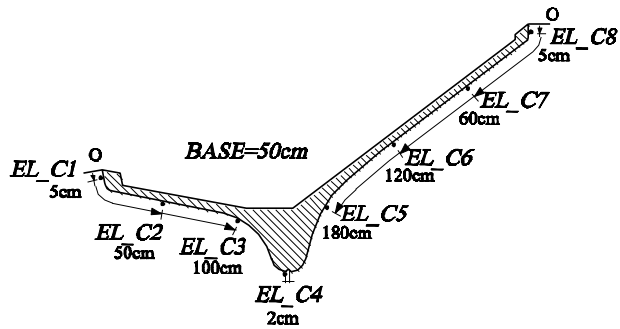


Real-size structures

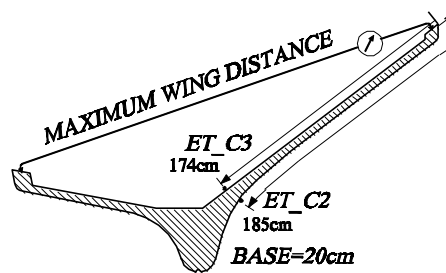


SECTION C

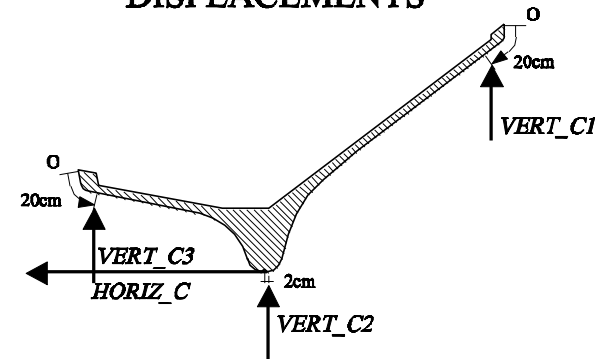
LONGITUDINAL STRAINS



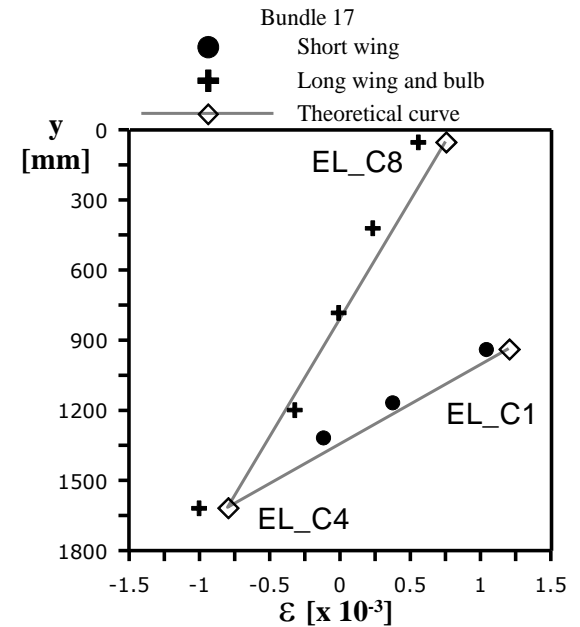
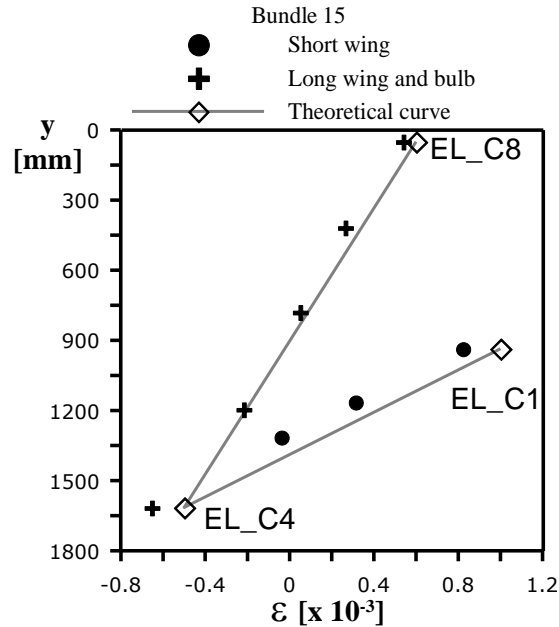
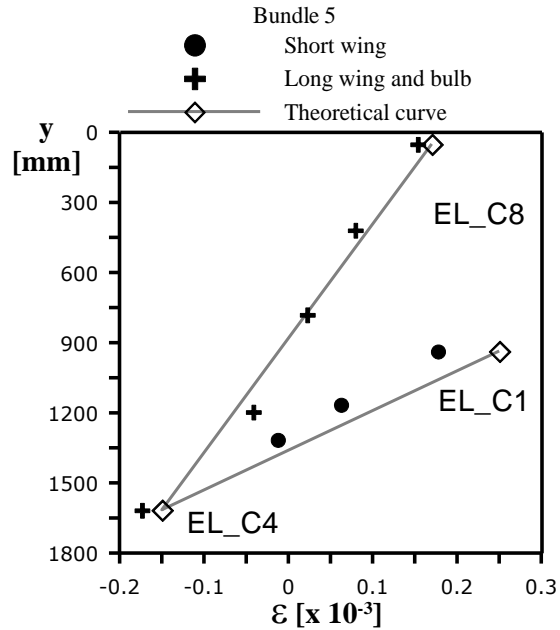
TRANSVERSAL STRAINS



VERTICAL/HORIZONTAL DISPLACEMENTS



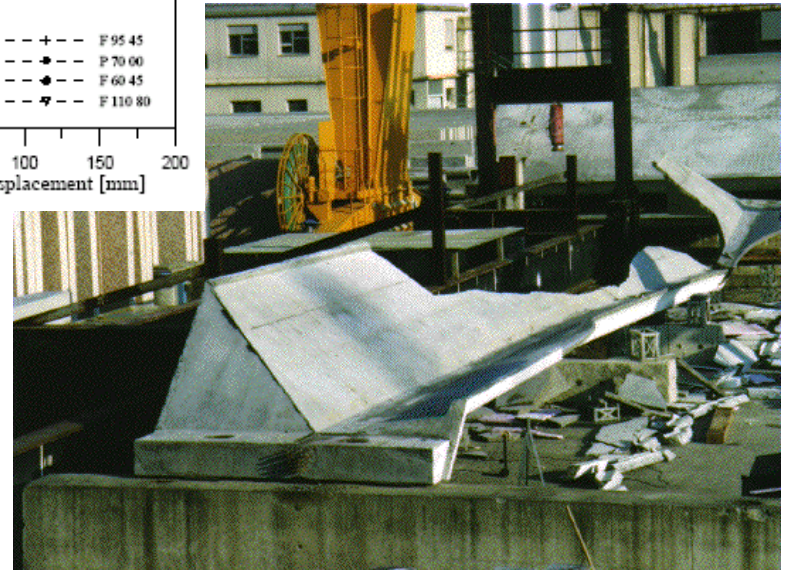
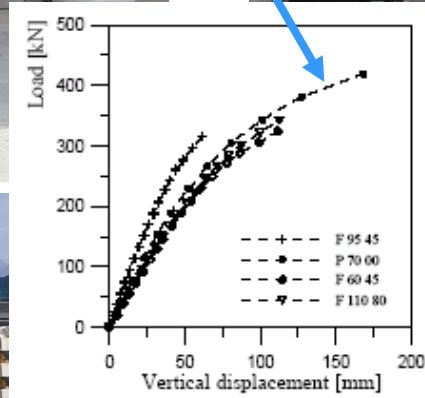
Real-size structures



Precast Element	P [kN]	M_{CEB} [kNm]	M_{EC2} [kNm]	M_{EXP} [kNm]
P 70 00	418.80	2565 (+26.8%)	2461 (+20.3%)	2023
F 95 45	351.48	2383 (+40.4%)	2232 (+31.5%)	1697
F 60 45	343.01	2090 (+25.8%)	2042 (+22.9%)	1661
F 110 80	342.40	2530 (+53.4%)	2294 (+39.1%)	1649

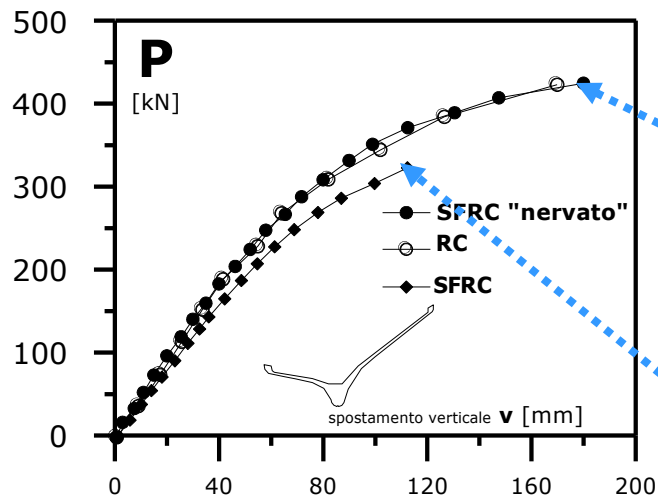
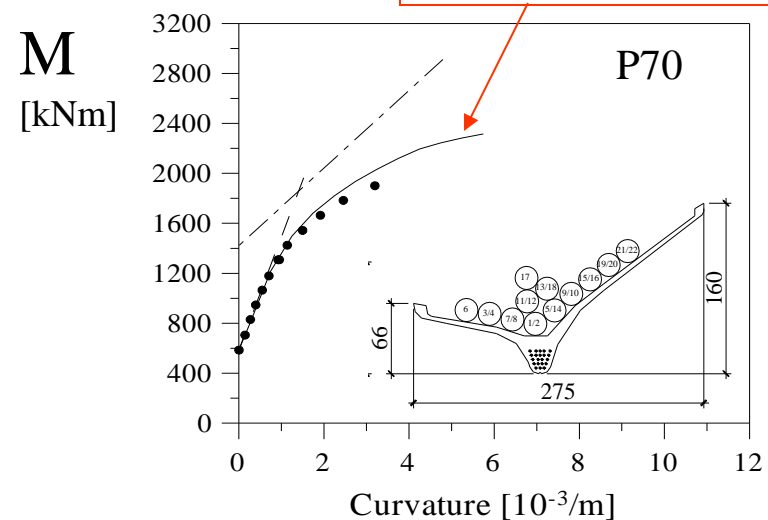
-35%

Full-size structures



Real-size structures

theoretical prediction



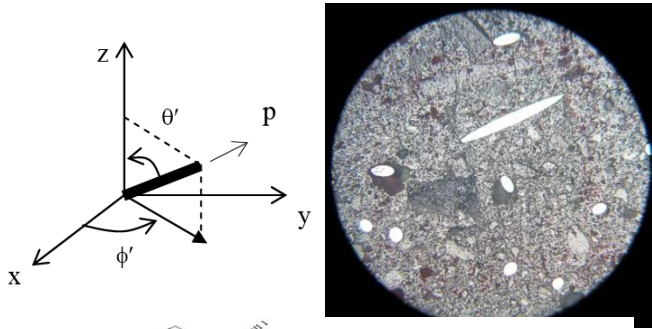
Workability, passing and filling ability



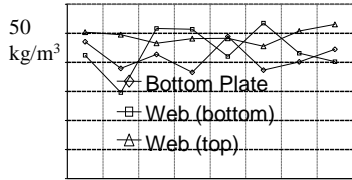
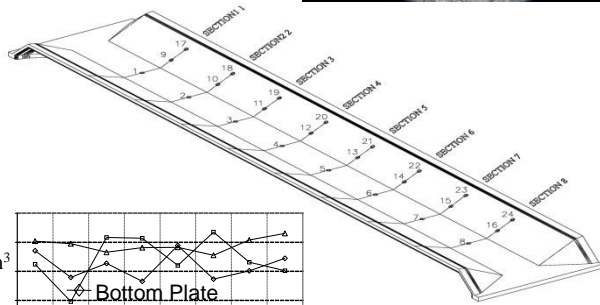
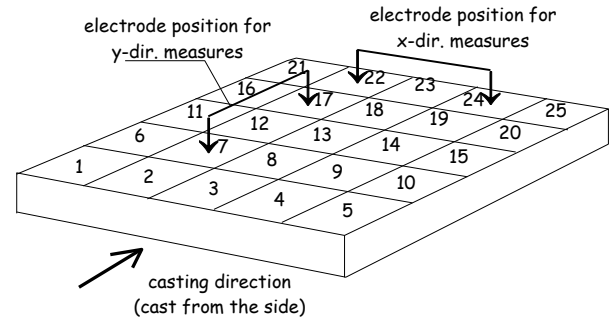
Conventional tests on fresh concrete to guarantee a homogeneous fibre distribution

The real question remains: is the mix robust enough?

A "triangular" optimization

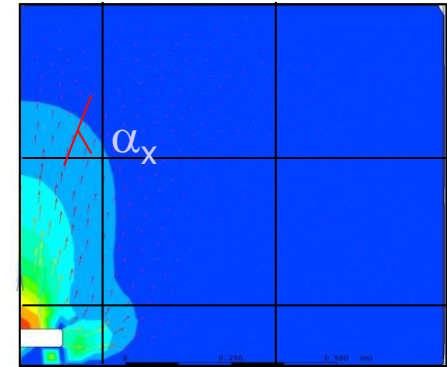


Fiber dispersion and orientation



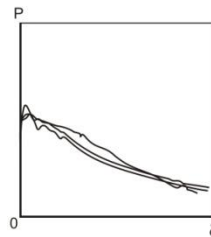
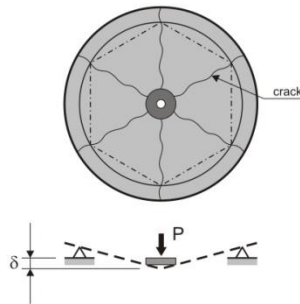
Mechanical properties

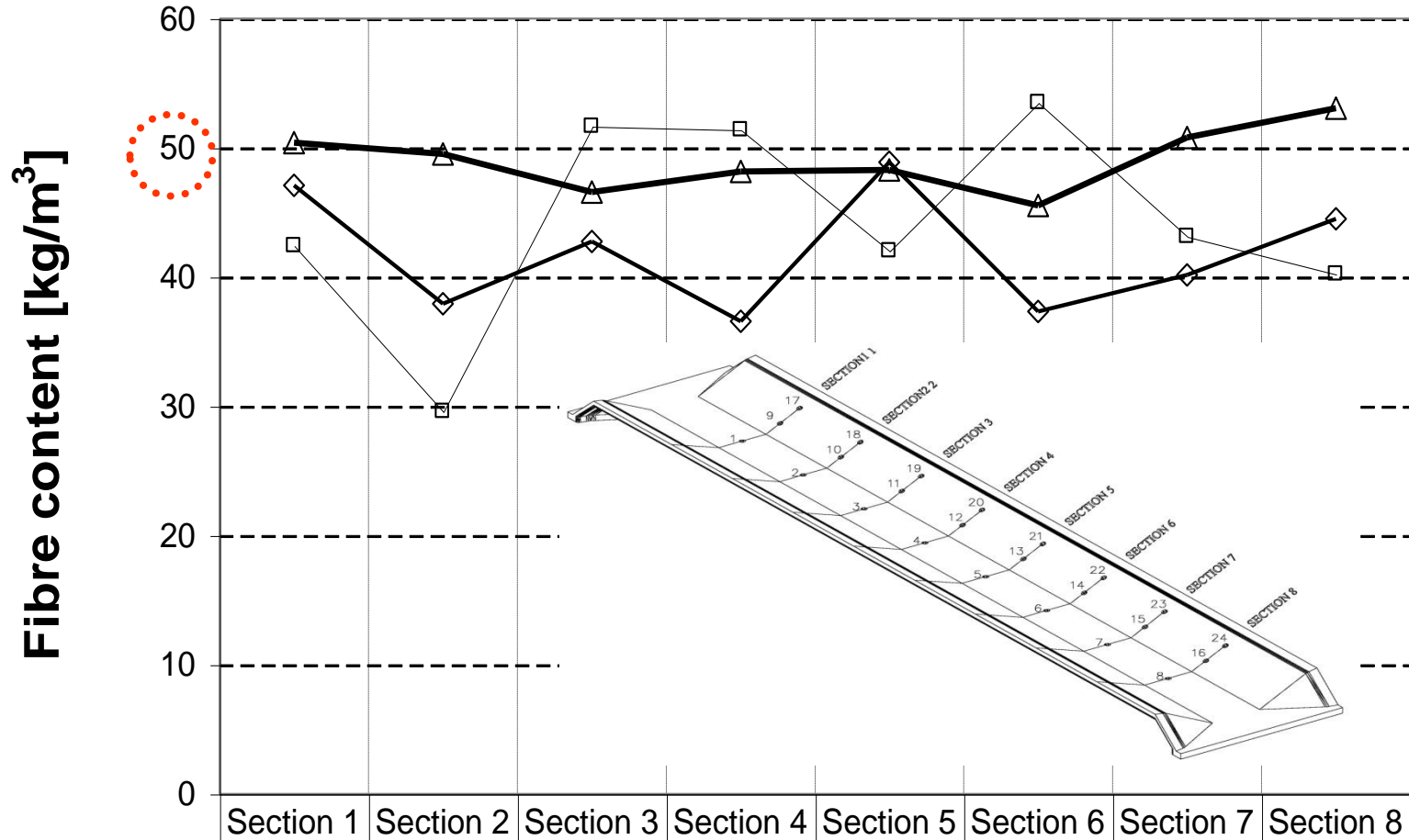
SCSFRC structural performance



Fractional shear rate vector orientation

Fresh state behaviour





by Ferrara and Meda, 2006

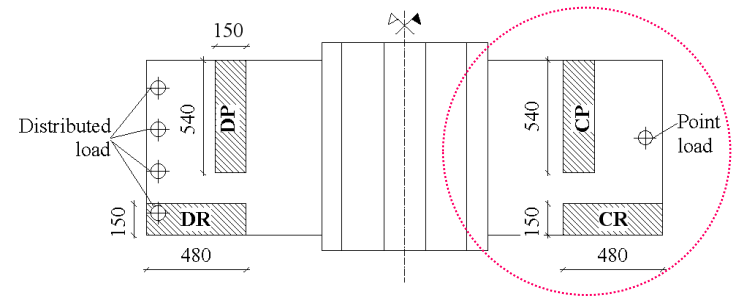
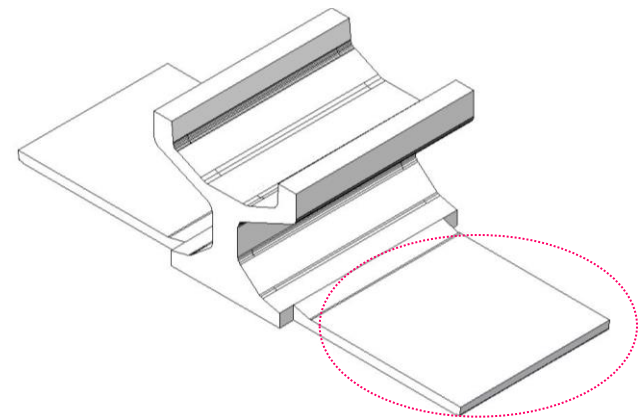
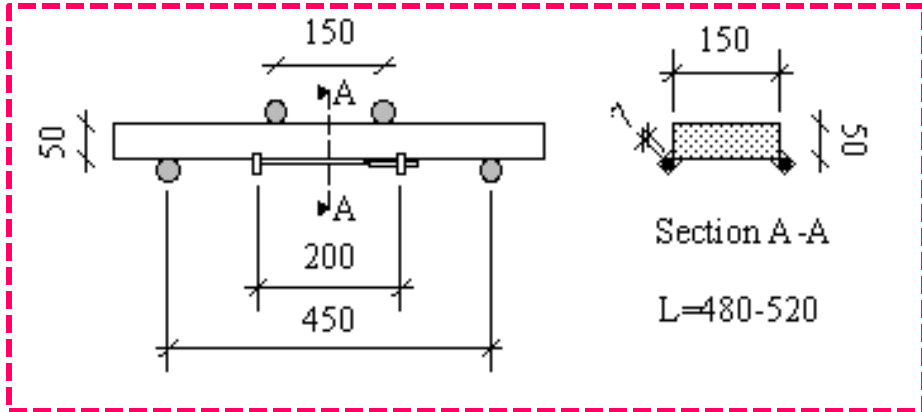
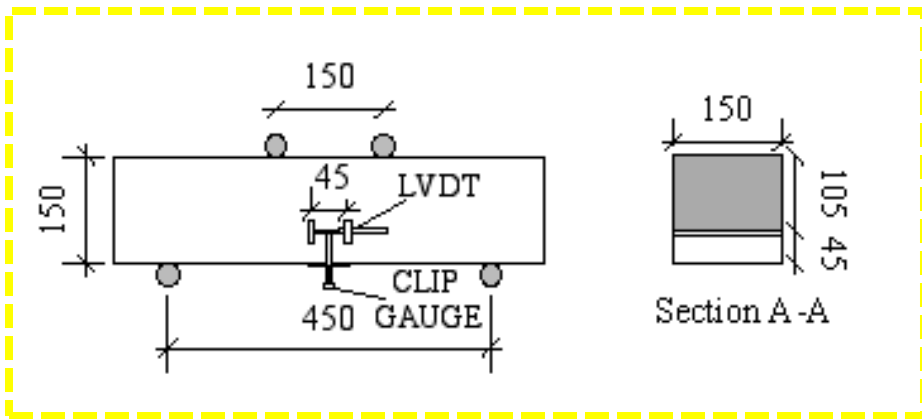
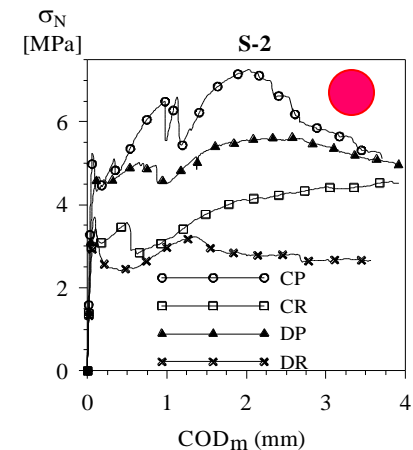
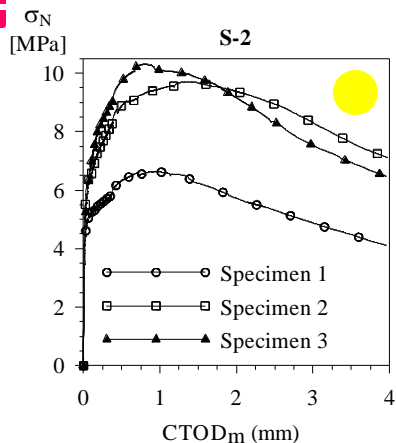


Table 1. Material description

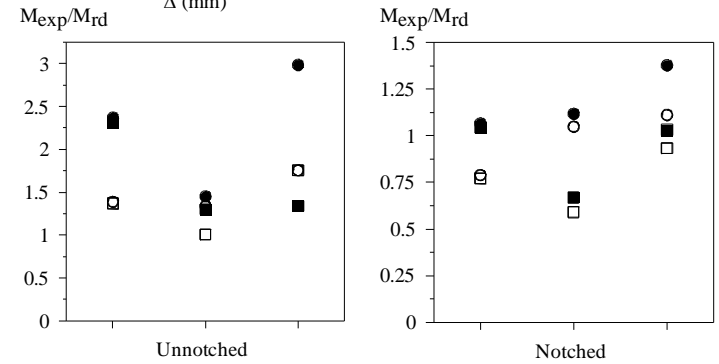
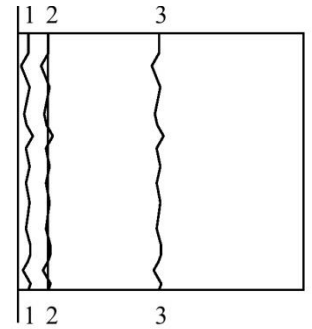
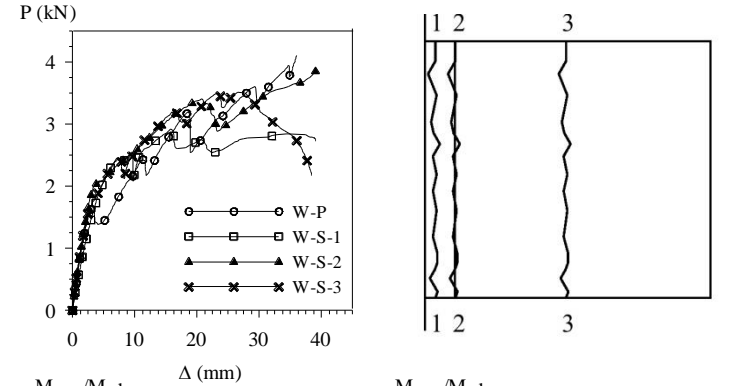
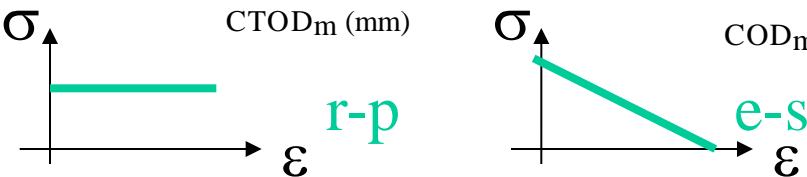
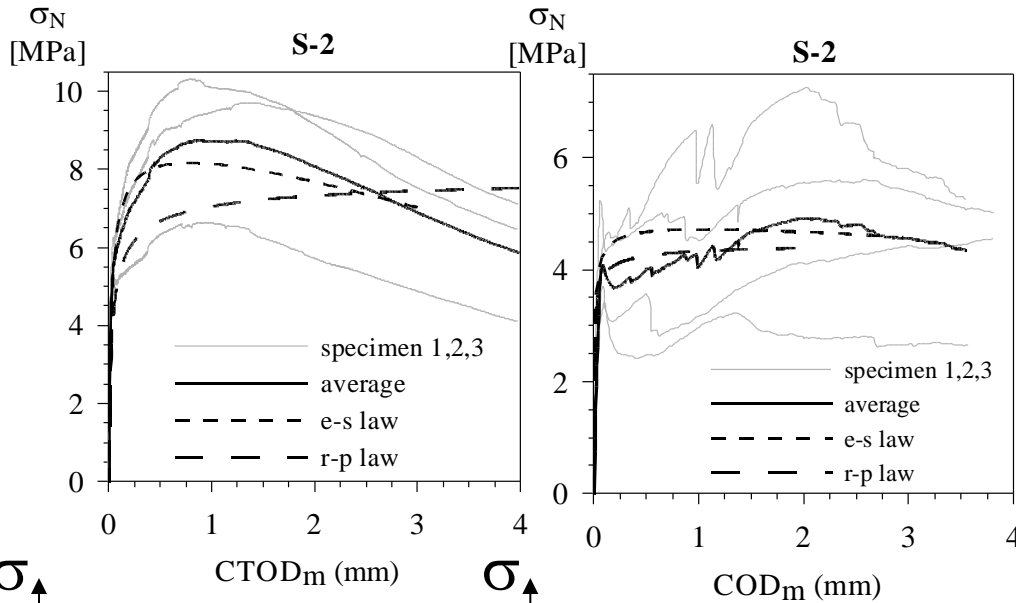
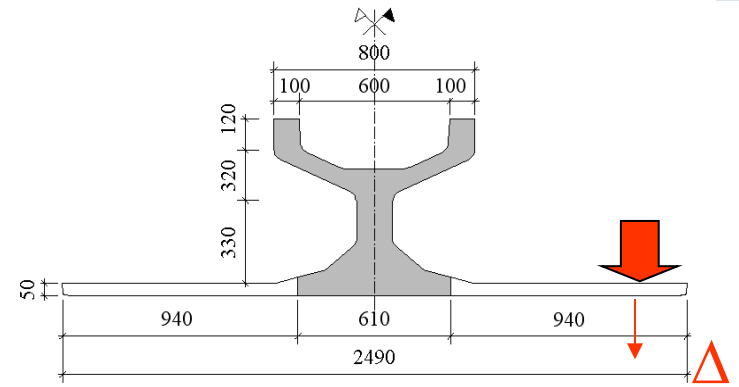
Code	Steel				Polypropylene			
	R_{cm} [MPa]	c_f [kg/m ³]	l_f/d_f	l_f [mm]	f_{fu} [MPa]	c_f [kg/m ³]	l_f [mm]	f_{fu} [MPa]
P	61.19	-	-	-	-	-	-	-
S-1	54.43	25+	75	60	1192	3	12	450
S-2	57.09	50	80	30	2300	3	12	450
S-3	61.09	50	45	30	1250	3	12	450



by Bonalumi et al., 2006

Classification tests

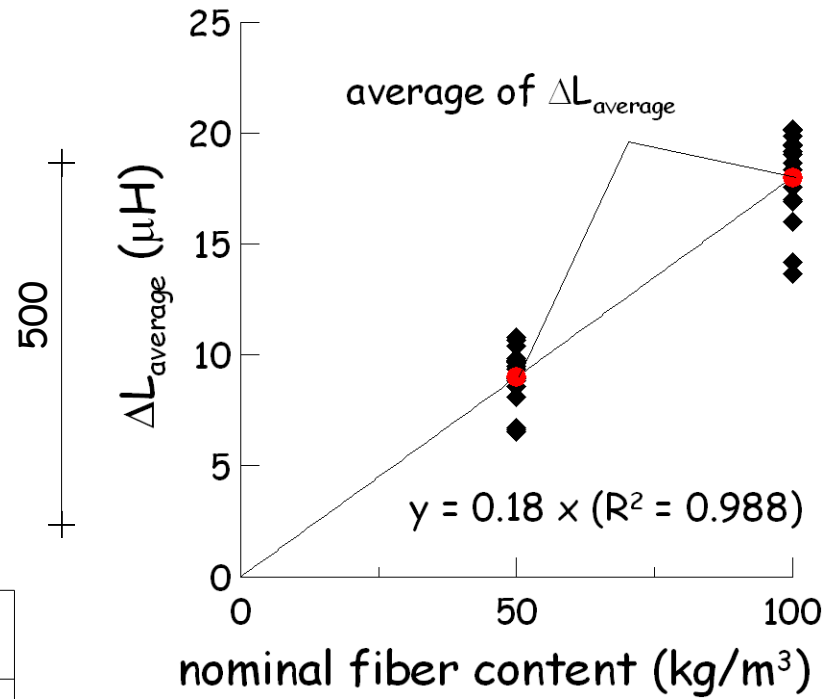
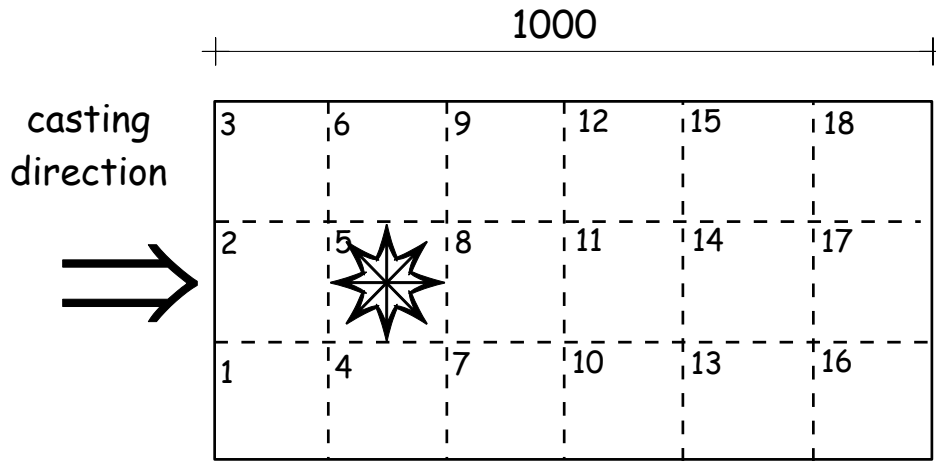
Structural test



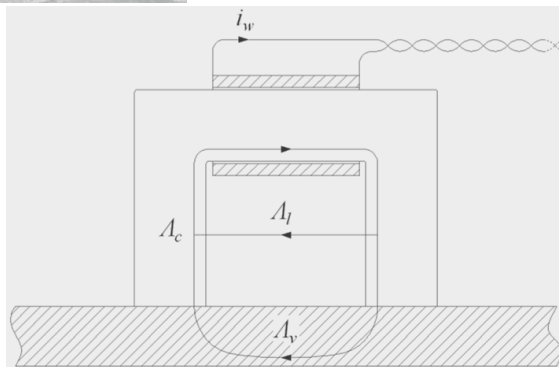
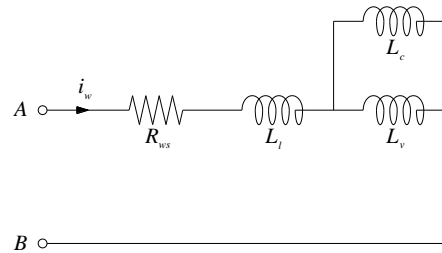
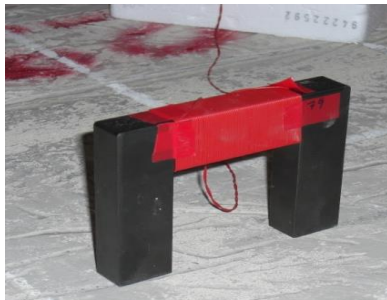
	concentrated load	distributed load
elasto-softening law	○	□
rigid-plastic law	●	■

A non destructive test to identify fibre distribution

by Ferrara et al. 2010

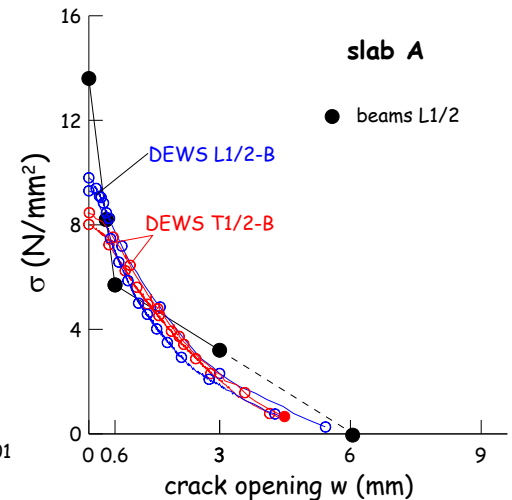
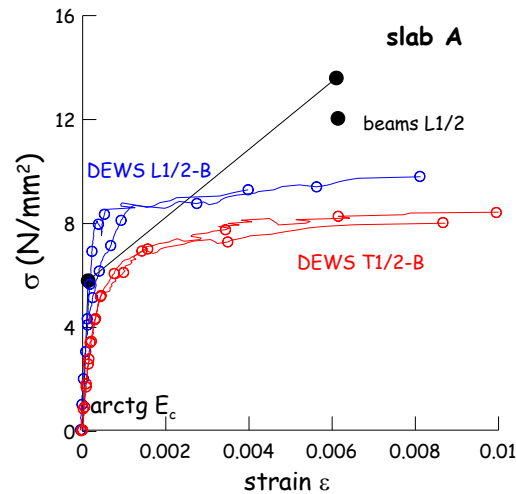
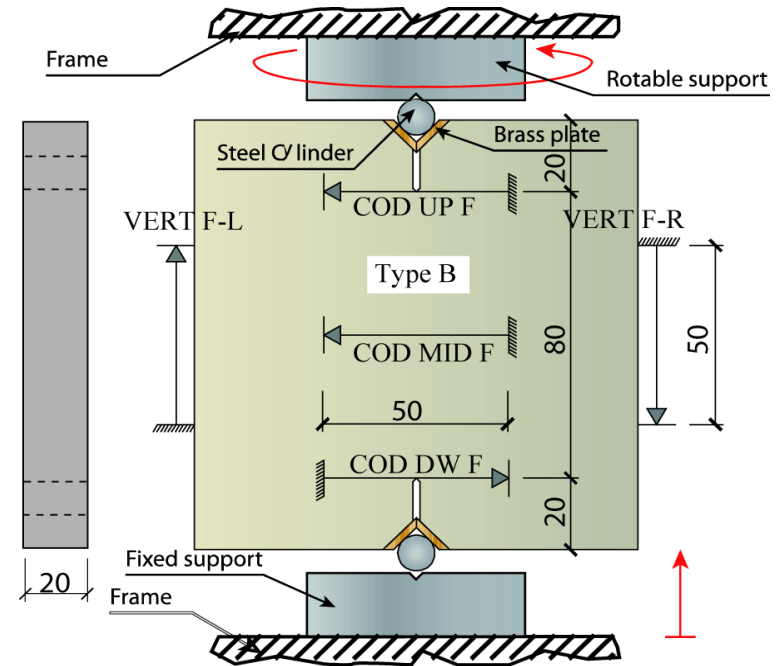
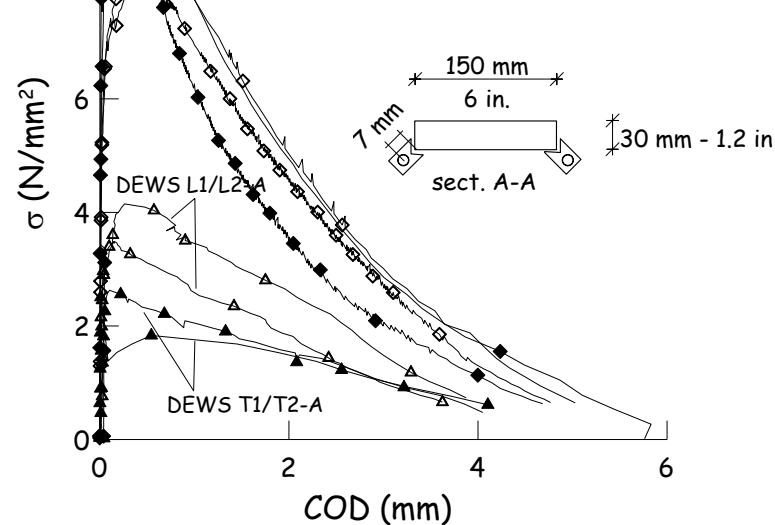
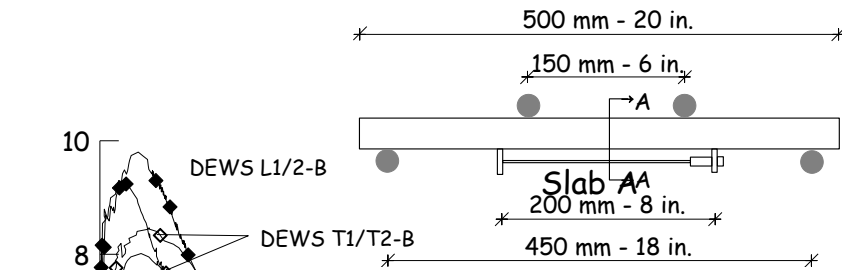
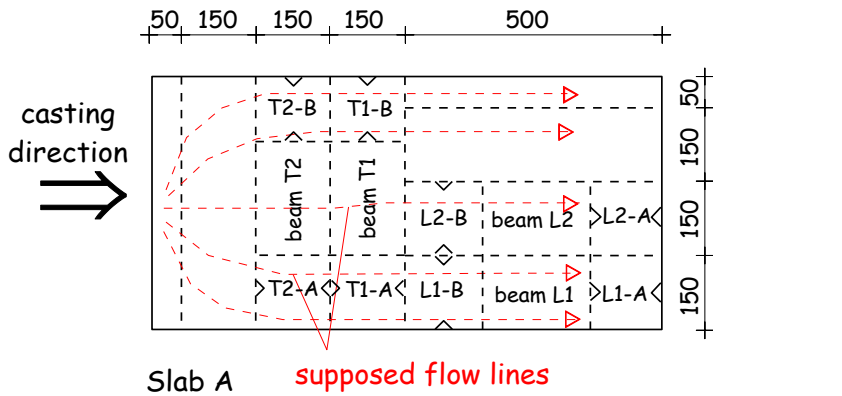


100 kg/m³



3	6	9	12	15	18
ND = 110.5	ND = 110.5	ND = 106.6	ND = 103.6	ND = 97.5	ND = 88.7
		D = 109.9	D = 106.7		
2	5	8	11	14	17
ND = 101.8	ND = 108.7	ND = 103.5	ND = 100	ND = 93.7	ND = 79.4
D = 119.1	D = 109.5	D = 107.8	D = 101.9	D = 98.2	D = 85
1	4	7	10	13	16
ND = 100.8	ND = 111.7	ND = 105.7	ND = 99.5	ND = 94.2	ND = 75.9
		D = 105.6	D = 99.4		

A destructive test to characterize FRC anisotropy



FRC is not homogeneous and not isotropic!
The inhomogeneity and anisotropic effects due to casting procedure can be taken into account by a special coefficient K that is at this time just empirical.

5.6.7 Orientation factor

$$f_{\text{Ftsd,mod}} = f_{\text{Ftsd}} / K \quad f_{\text{Ftud,mod}} = f_{\text{Ftud}} / K$$

Isotropic fibre distribution is assumed $K = 1.0$

For favourable effects $K < 1.0$

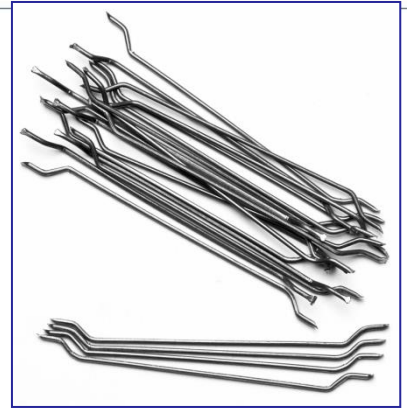
For unfavourable effects $K > 1.0$

✓ the limit state definition

$$w_u = \min (l_{cs} \cdot \epsilon_{Fu}, 2.5 \text{ mm})$$

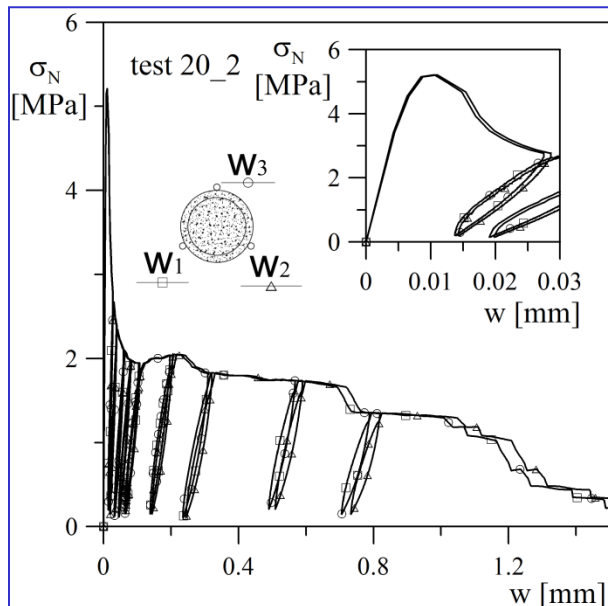
ductility

*2% for variable strain distribution along the cross section
1% for constant tensile strain distribution along the cross section.*

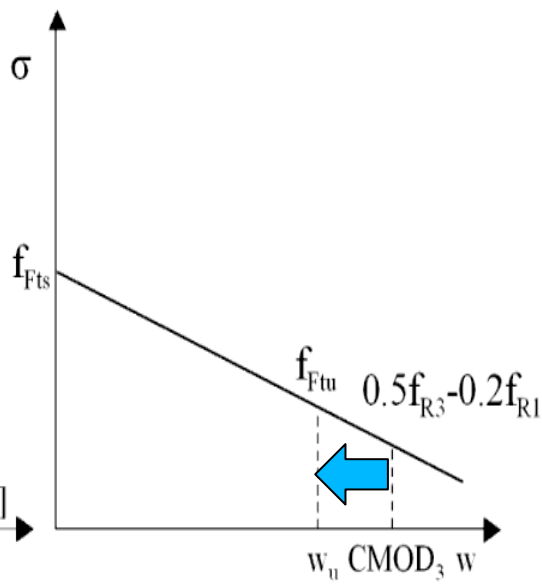
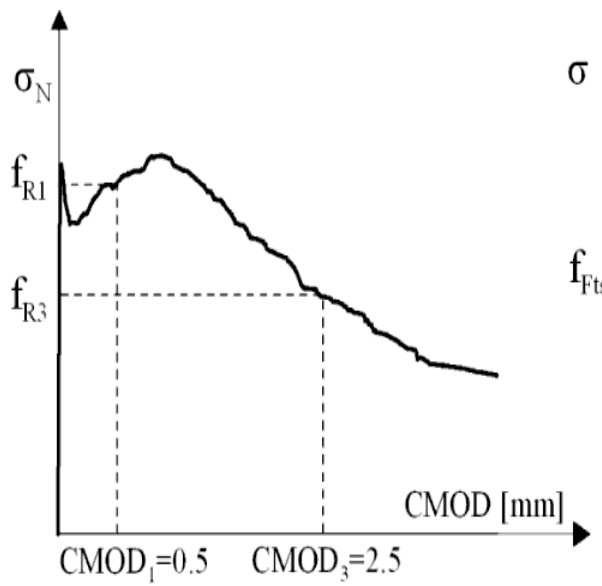


Fibre geometry

*valid for all the fibres in the market
For long steel fibres (crimped or hooked) could be on the safe side!*

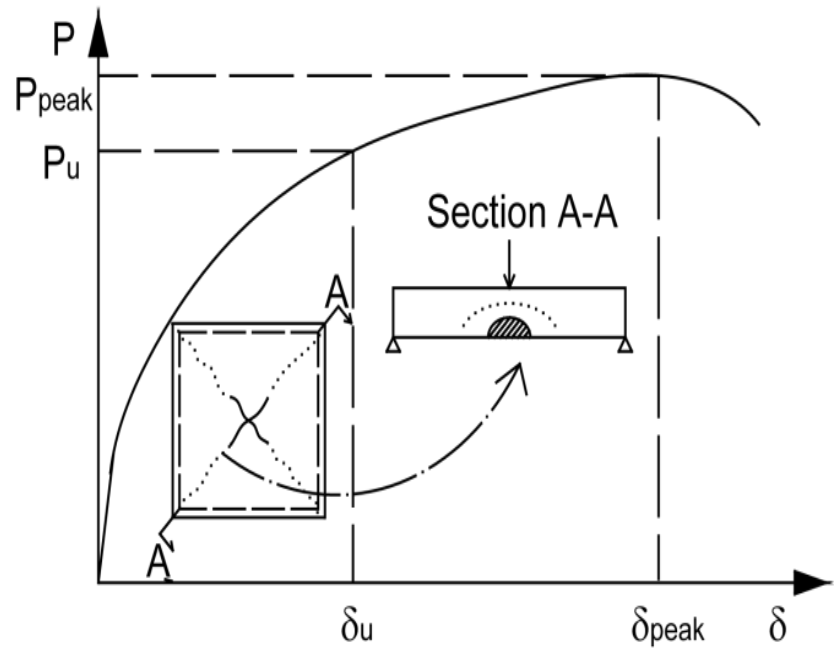
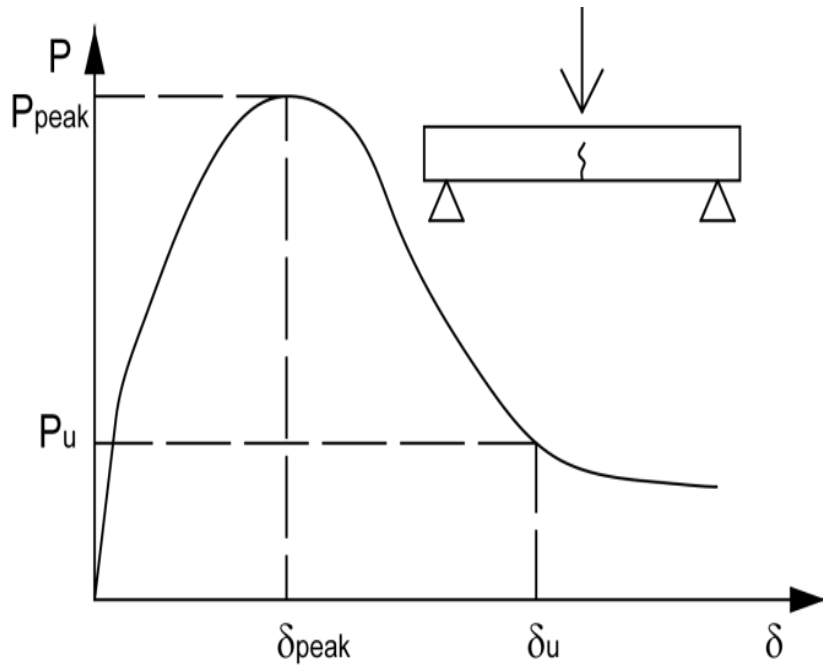


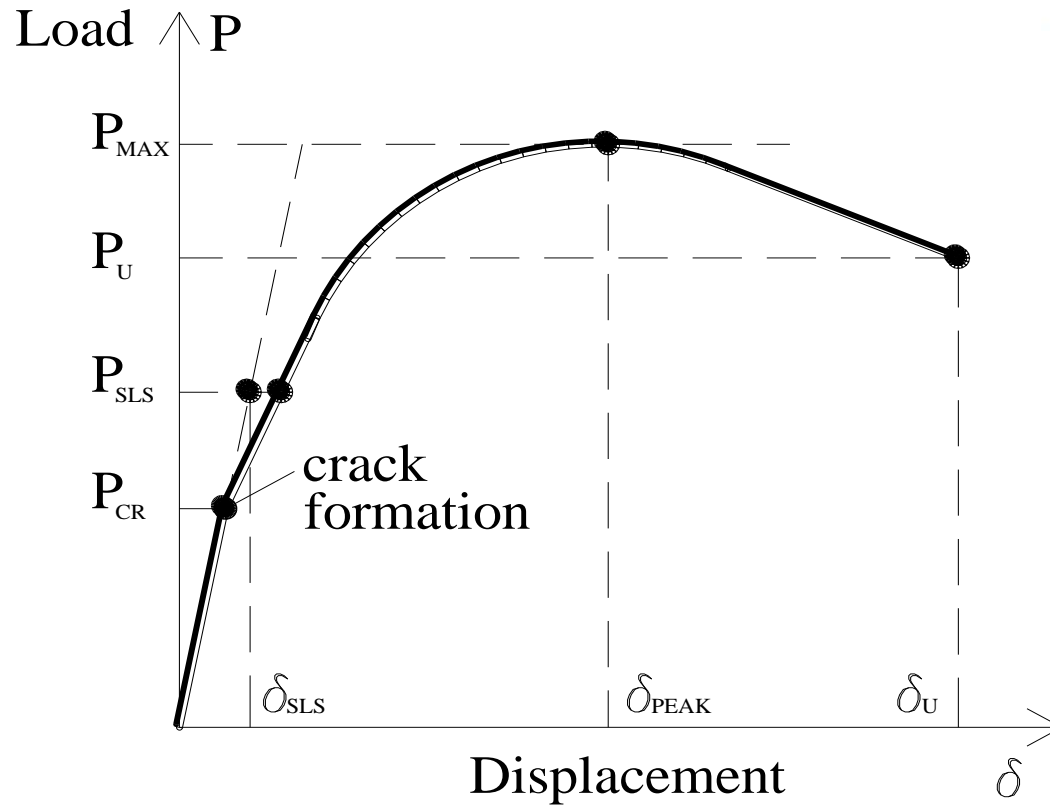
$f_c = 75 \text{ Mpa}$; Fibre content = 50 kg/m^3 ; Fibre length = 30mm ; Aspect ratio = 45 ; Low carbon



$$\theta_u = w_u/h$$

$$\delta_u = \delta_u(\theta_u, L_i)$$

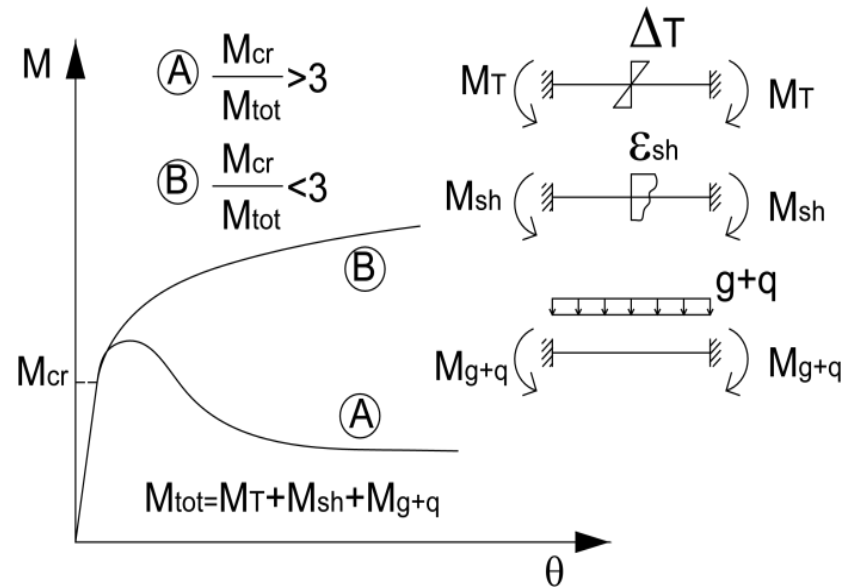
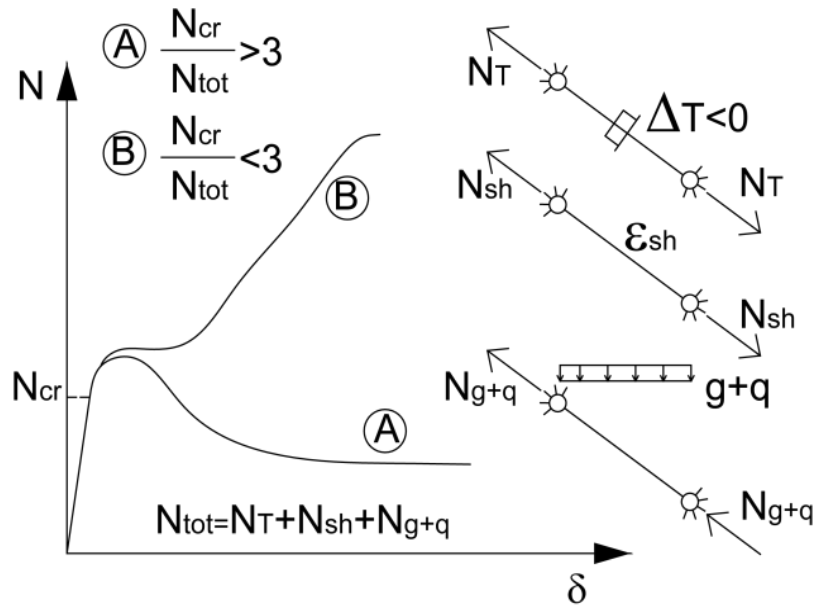




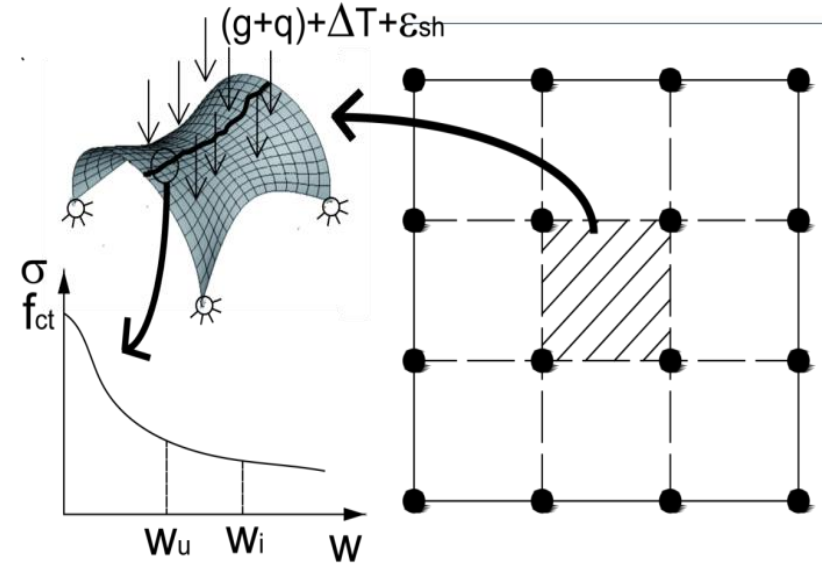
$$\delta_u \geq 20 \delta_{SLS}$$

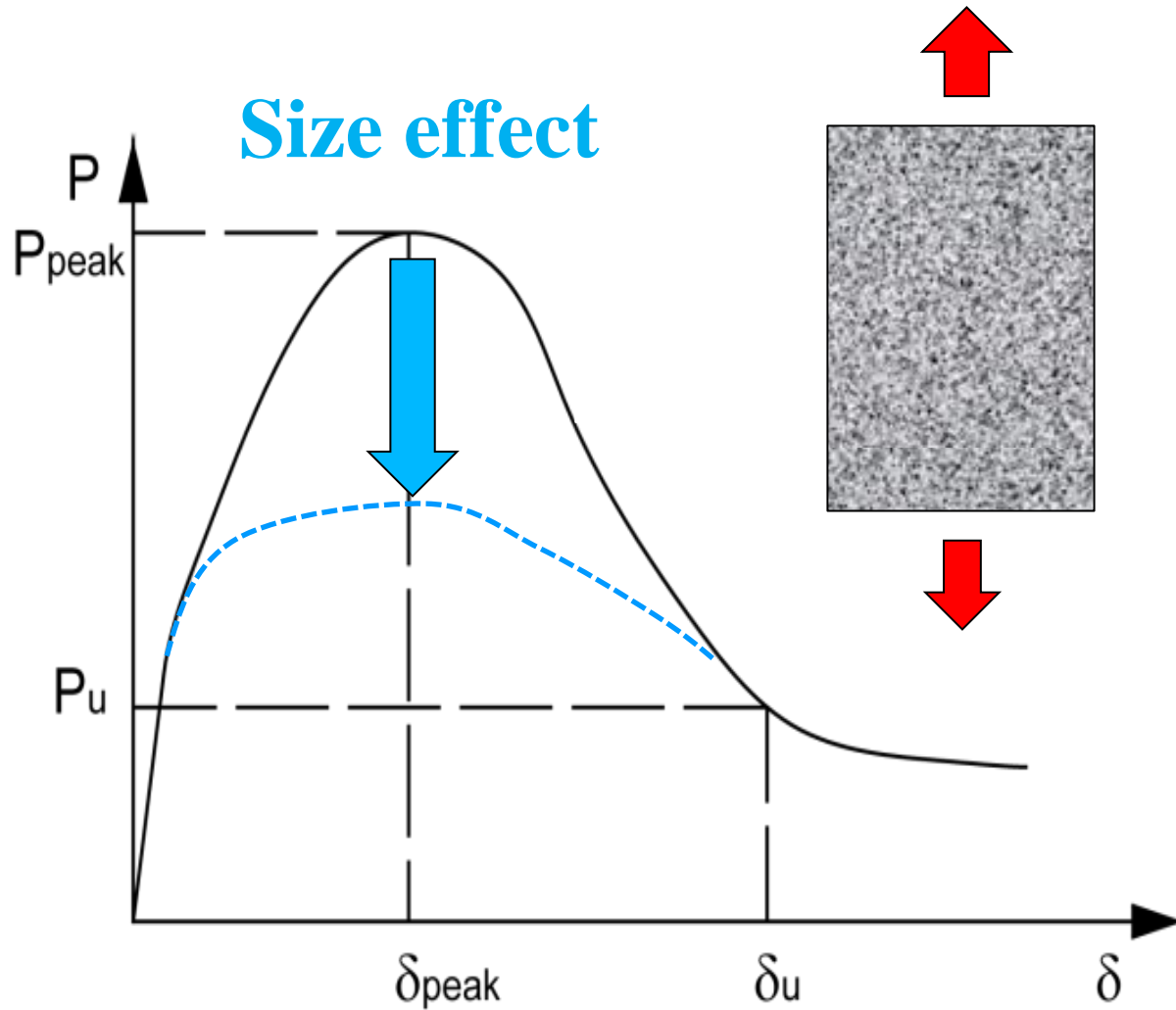
$$\delta_{peak} \geq 5 \delta_{SLS}$$

Shrinkage, thermal coactions, settlements ...

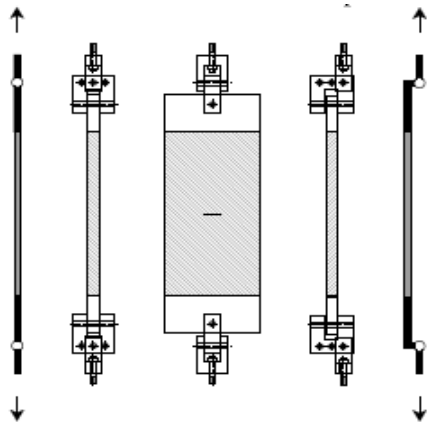


FRC for local bending

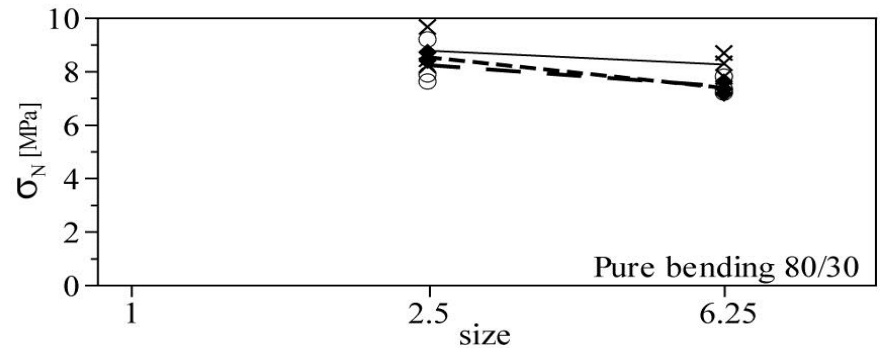
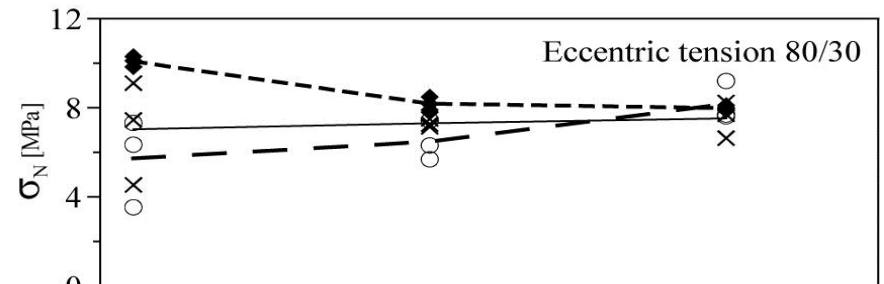
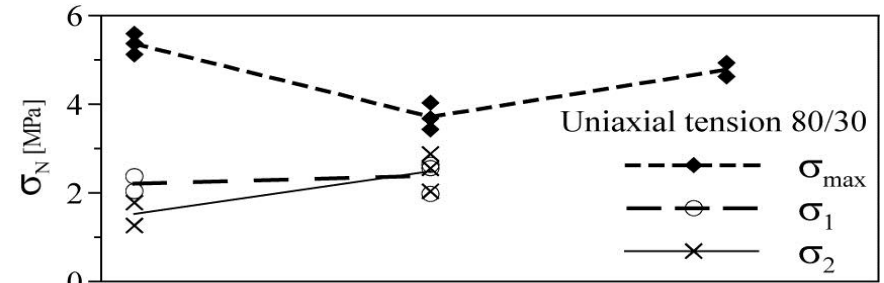
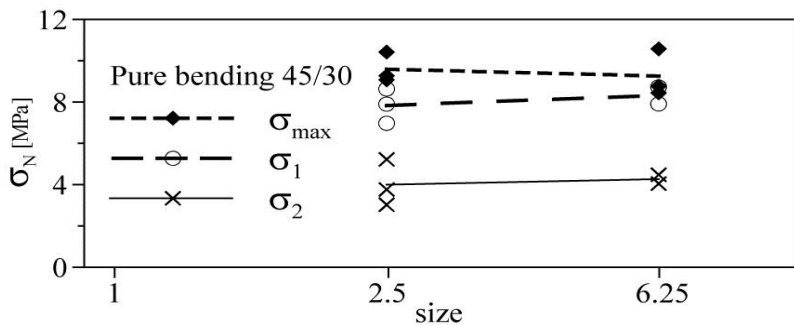
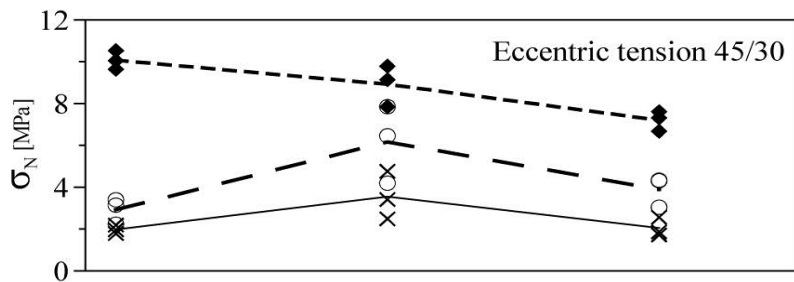
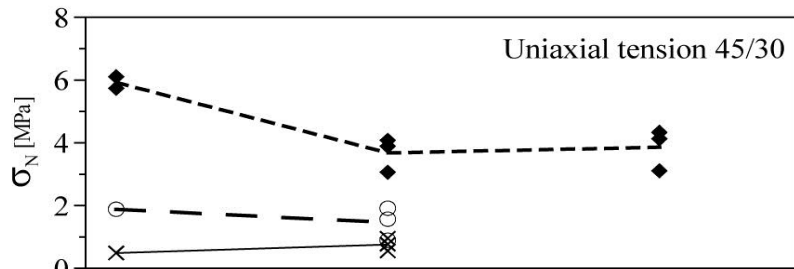




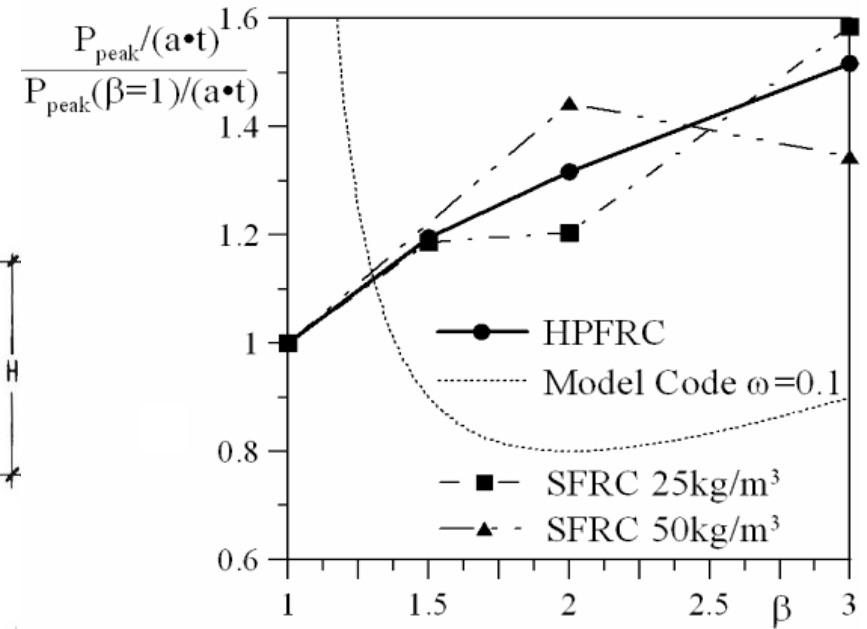
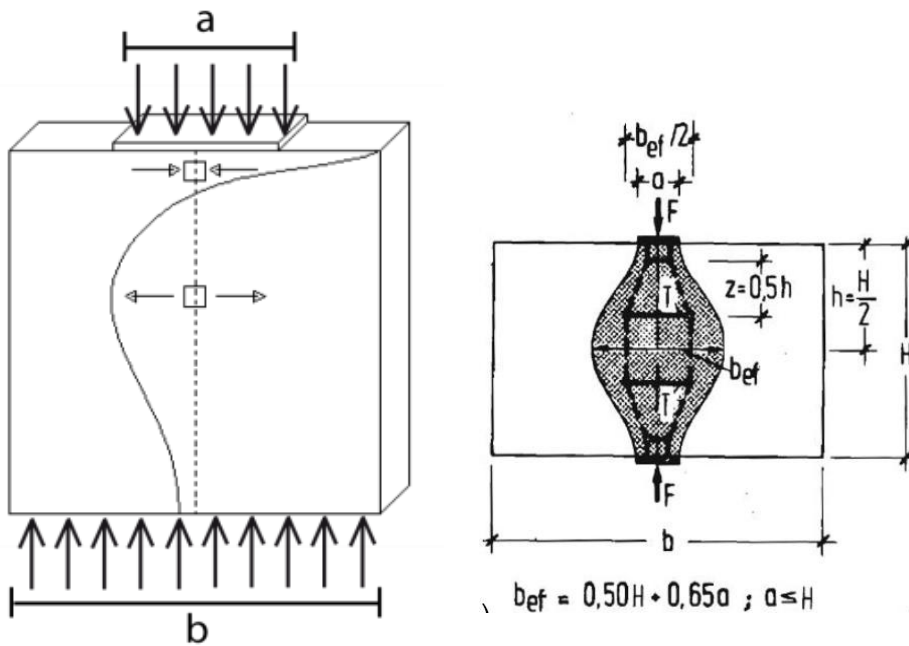
Size effect in tension



Specimen				
Type	Height [mm]	Width [mm]	Thick. [mm]	Notch [mm]
P	150	84	60	16.8
M	375	210	60	42
G	938	525	60	105



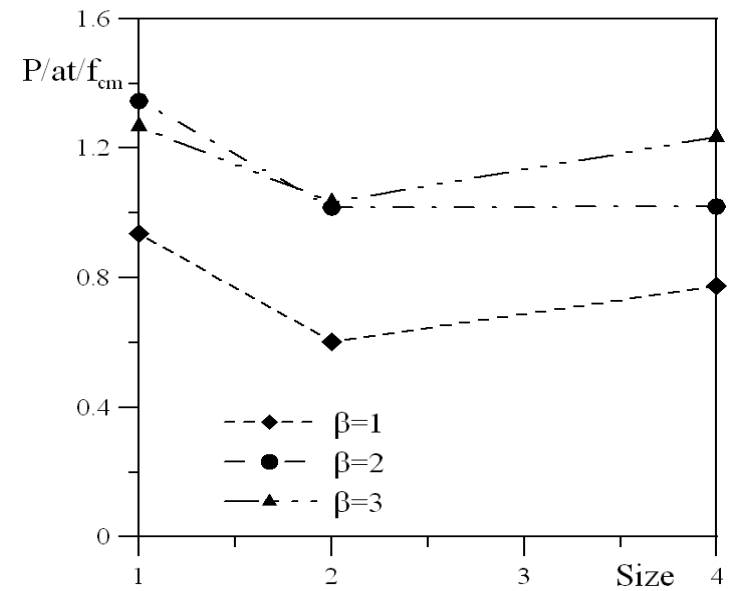
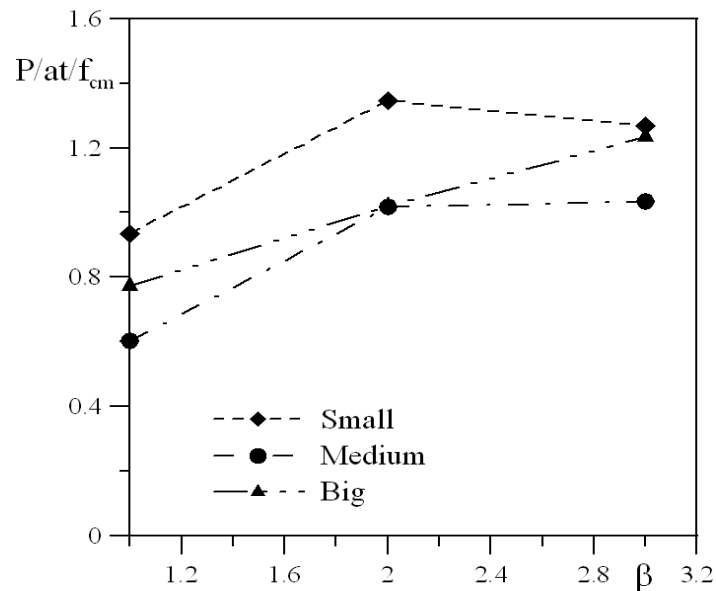
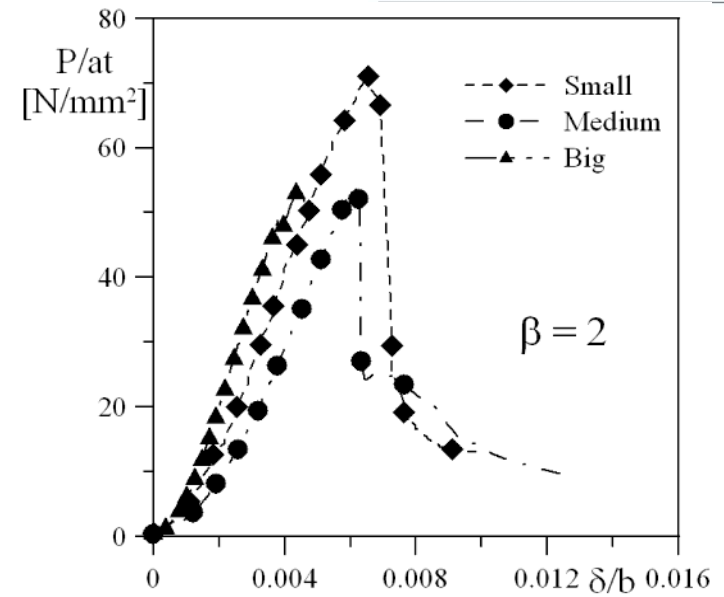
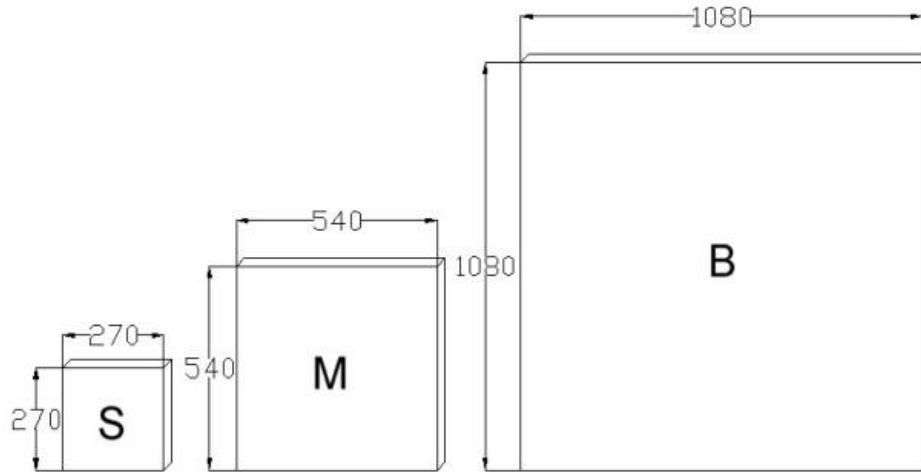
Bottle shaped strut



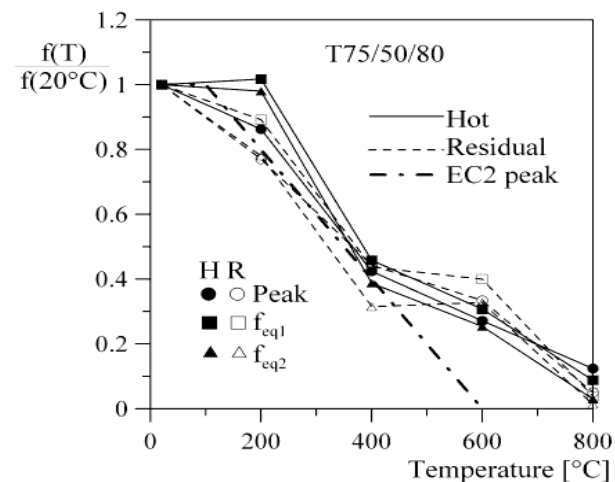
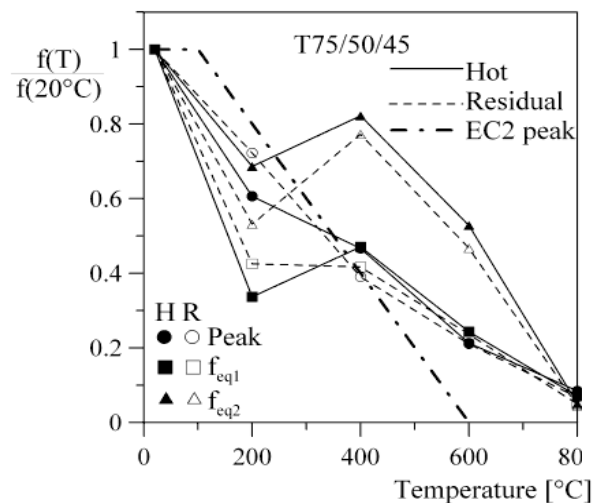
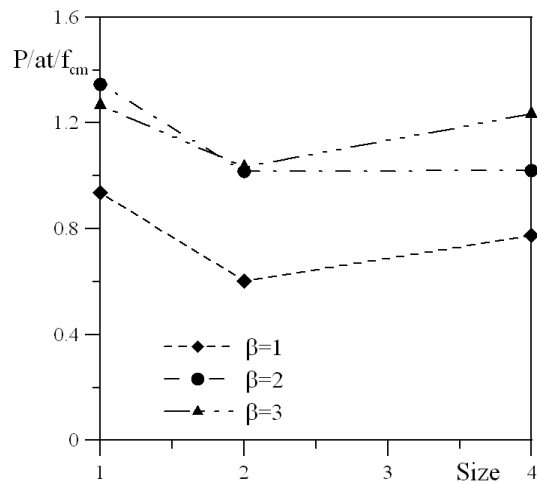
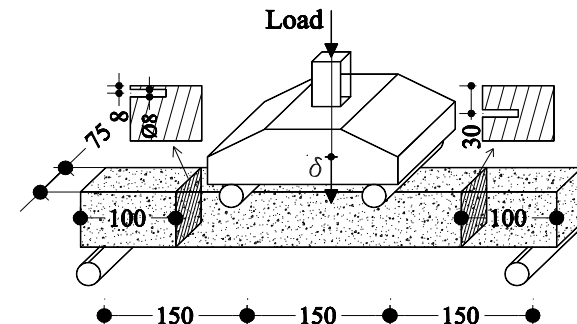
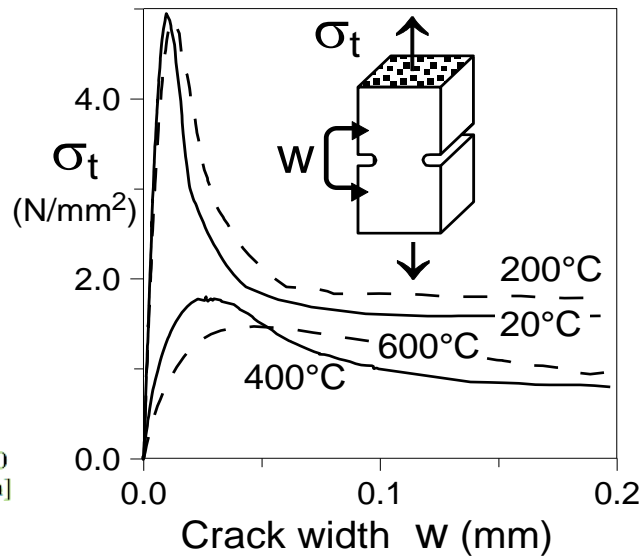
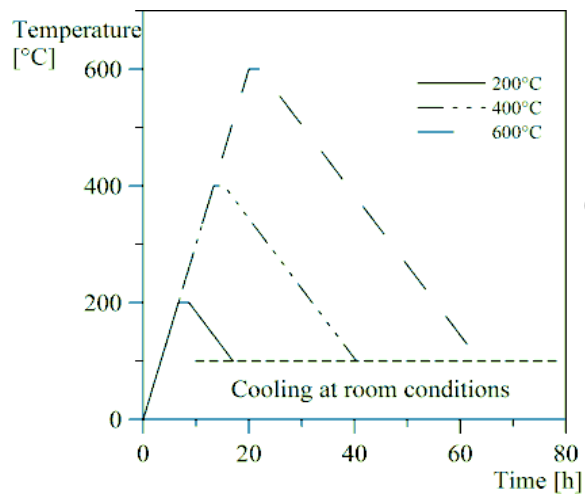
b/a	$\sigma_{c,max}/f_c$				
	NSC	HSC	UHSC	UHPC-1-HT	UHPC-2-HT
2.3	0.89	0.6	0.41	0.87	0.96
4.7	1.18	0.59	0.38	1.04	1.44
6.9	1.75	0.73	0.56	1.28	1.66
10.7	2.48	1.15	0.81	1.73	2.22

by T. Leutbecher, E. Fehling, 2012

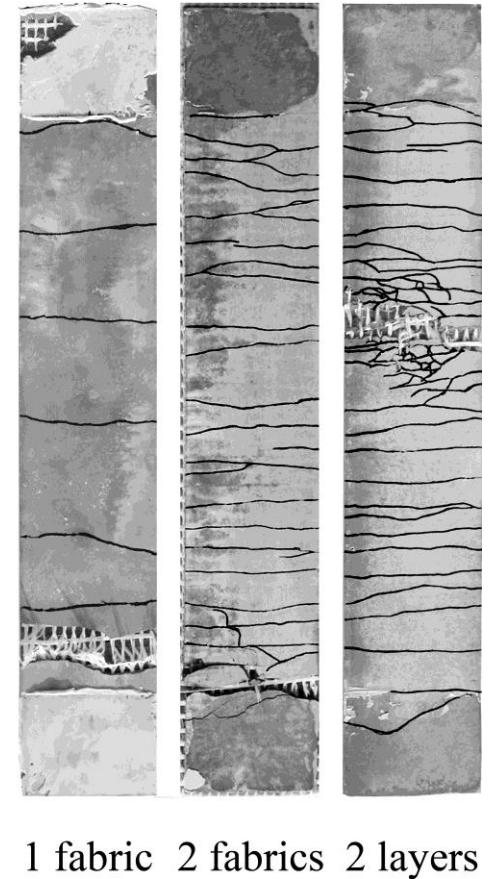
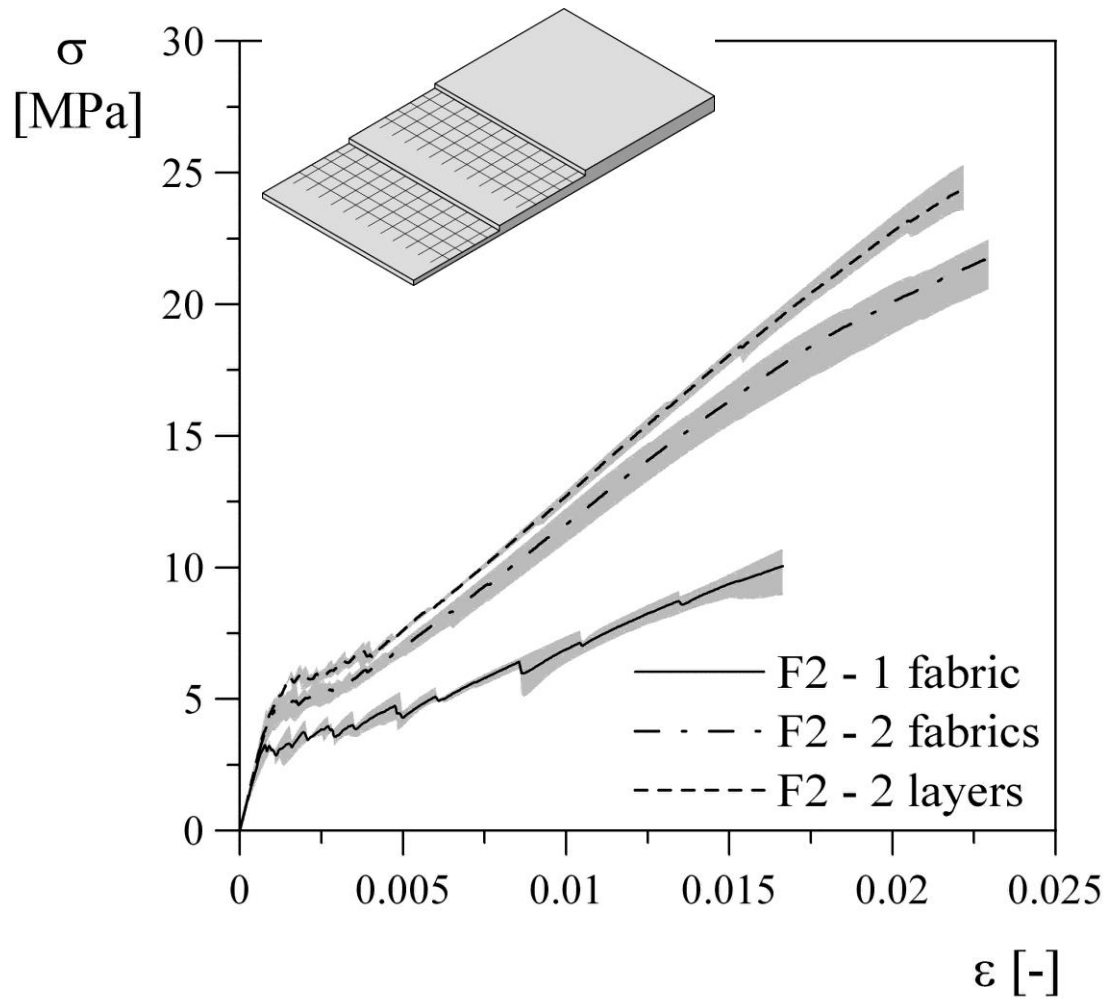
Size effect

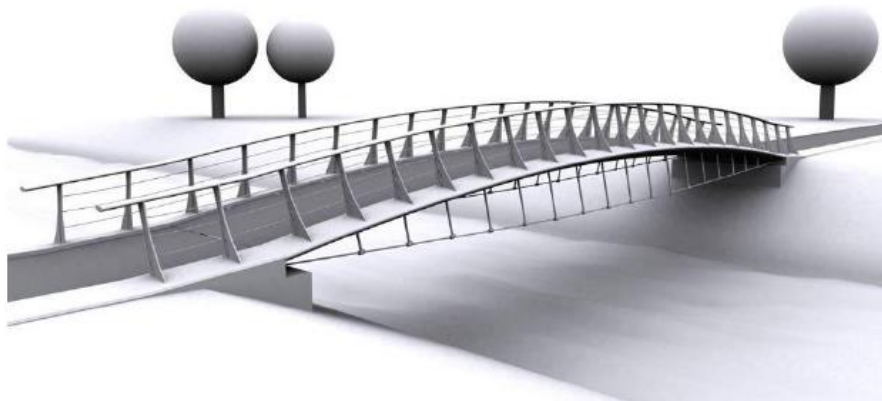


Residual stress after thermal damage

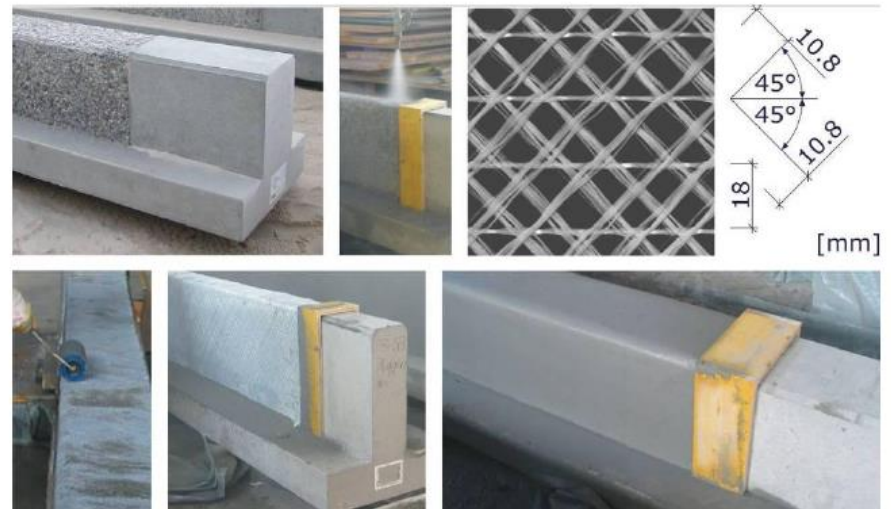


TRC: the use of non metallic AR glass fabrics

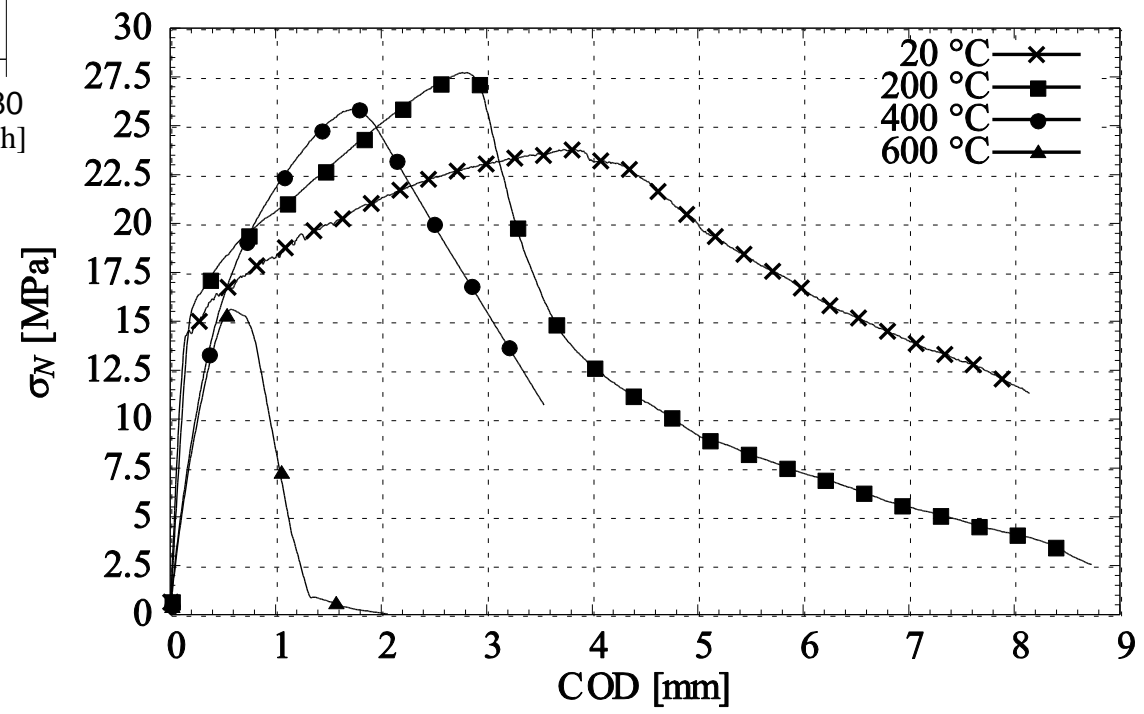
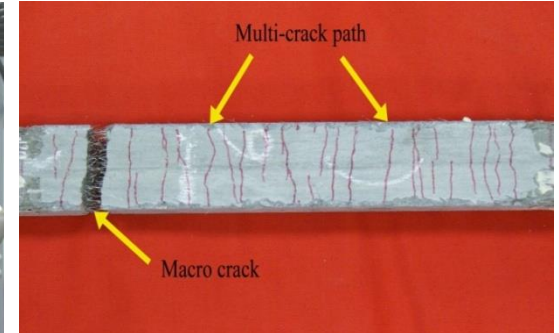
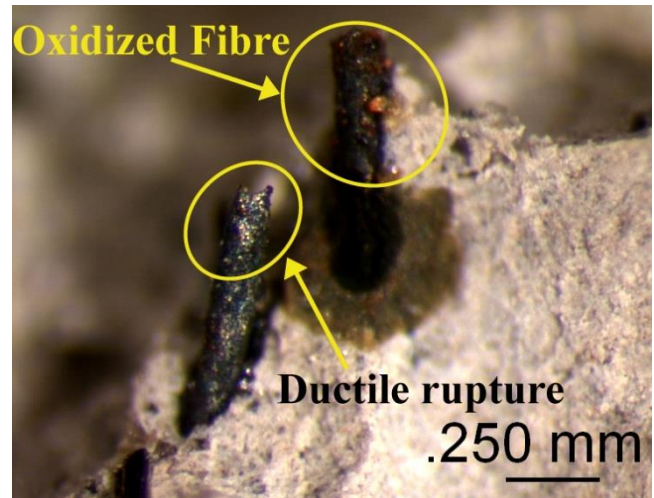
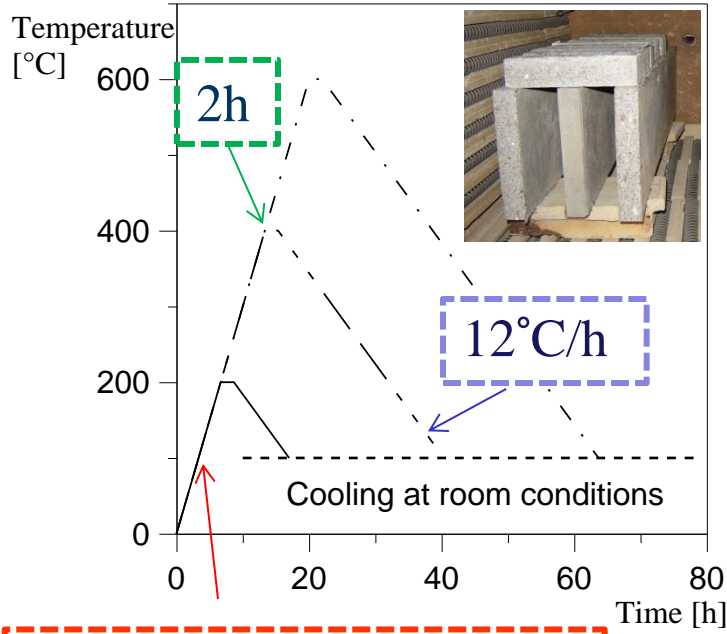


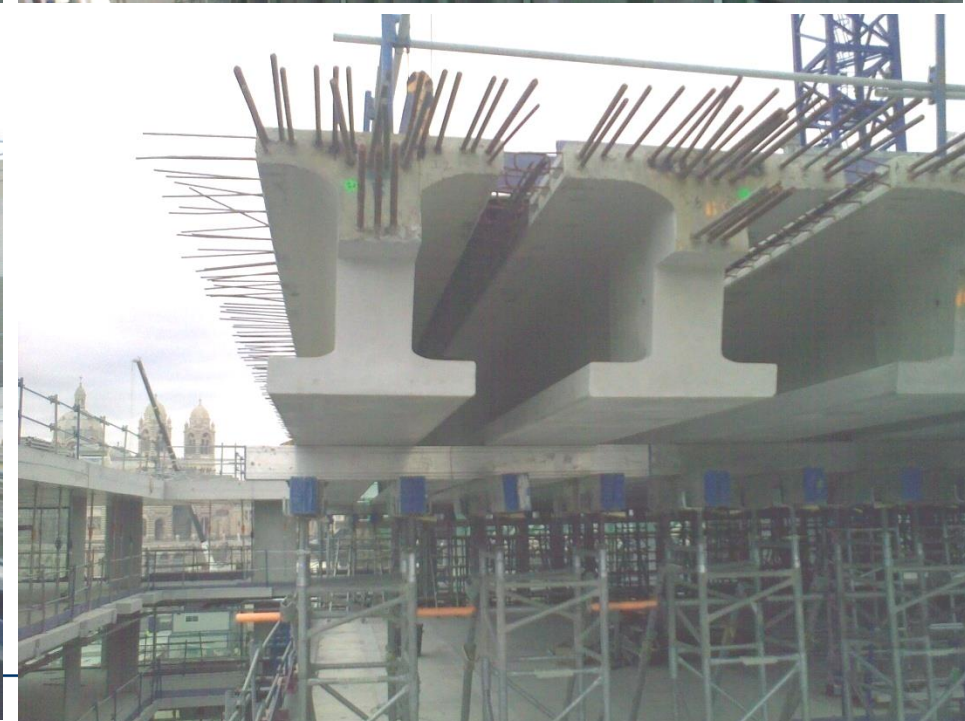


by Manfred Curbach and Silke Sheerer, 2011

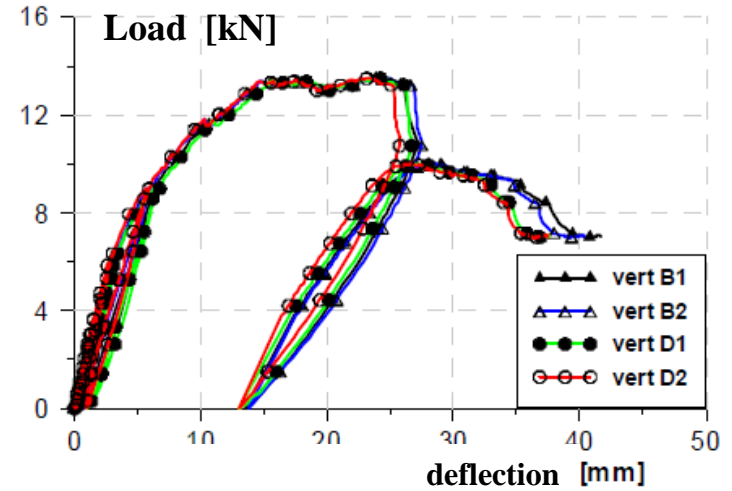
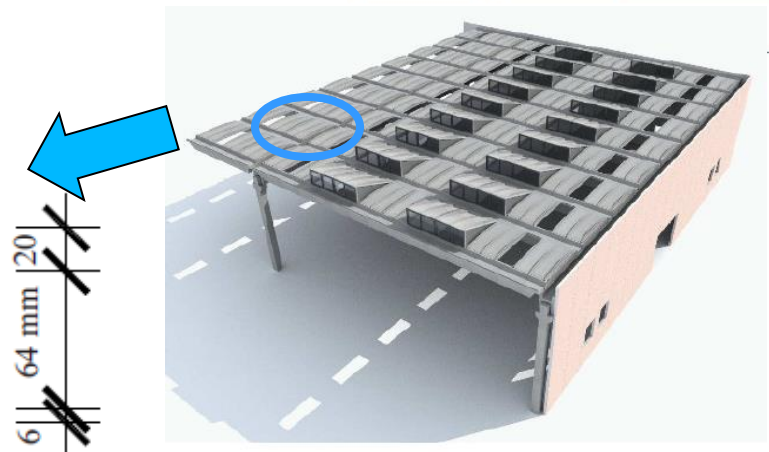
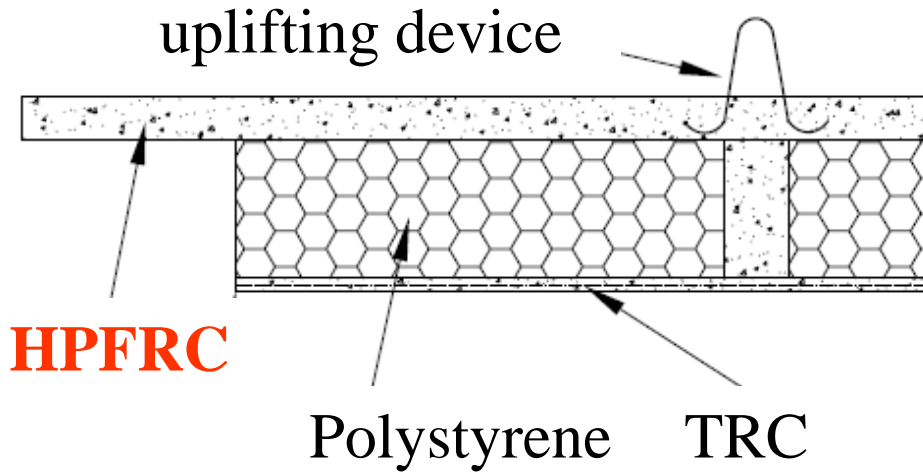


UHPFRC: fire resistant advanced material

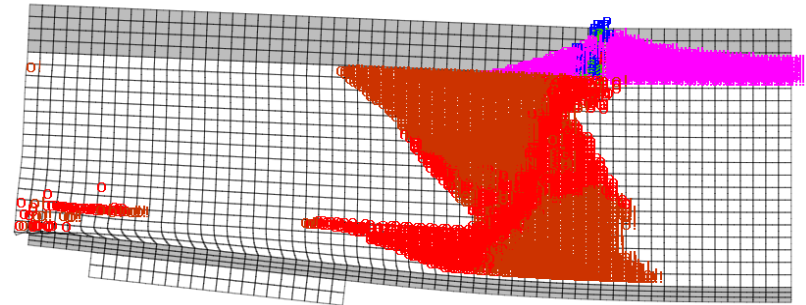
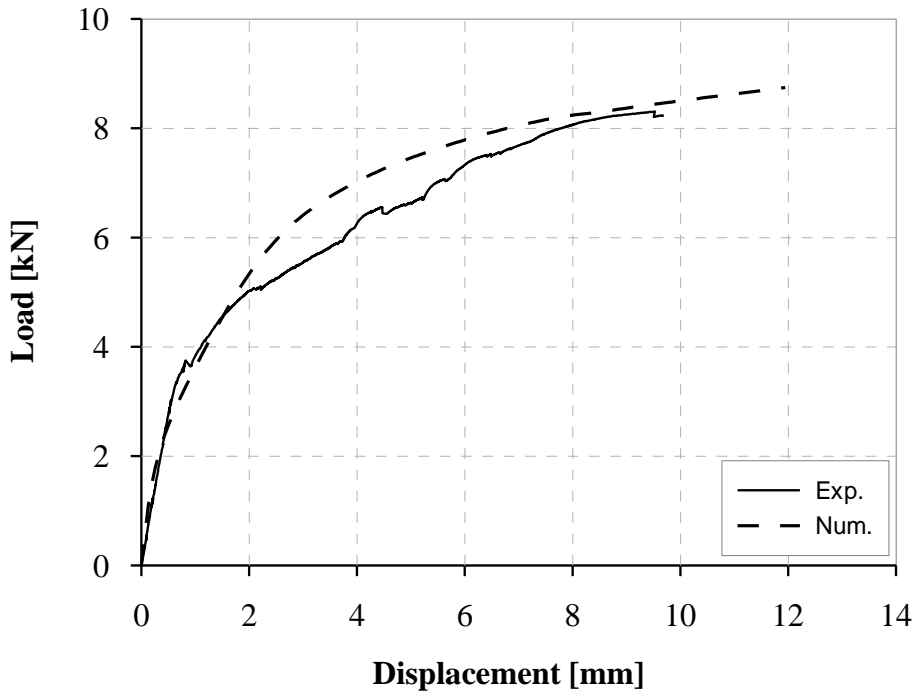
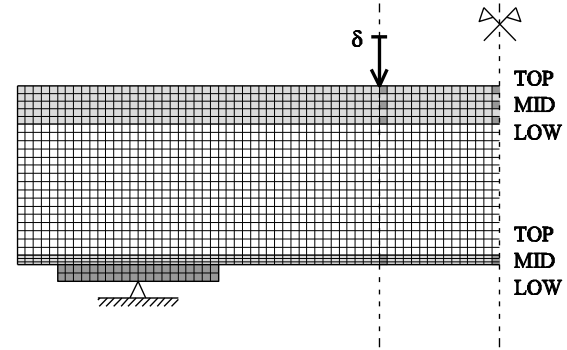
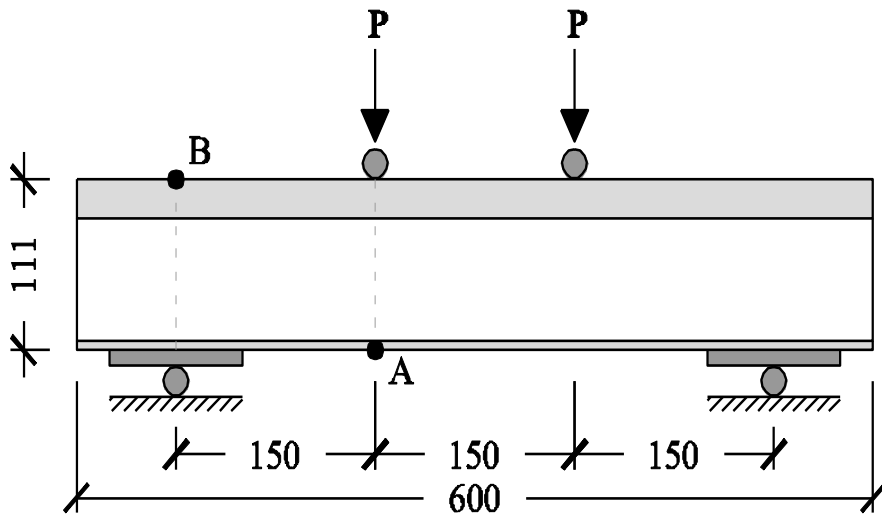




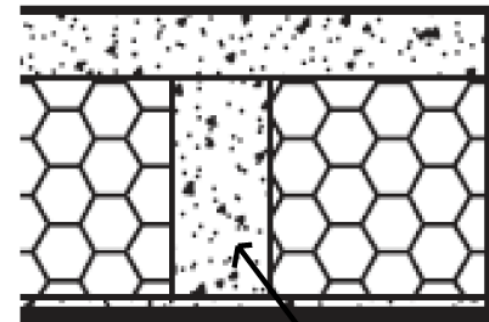
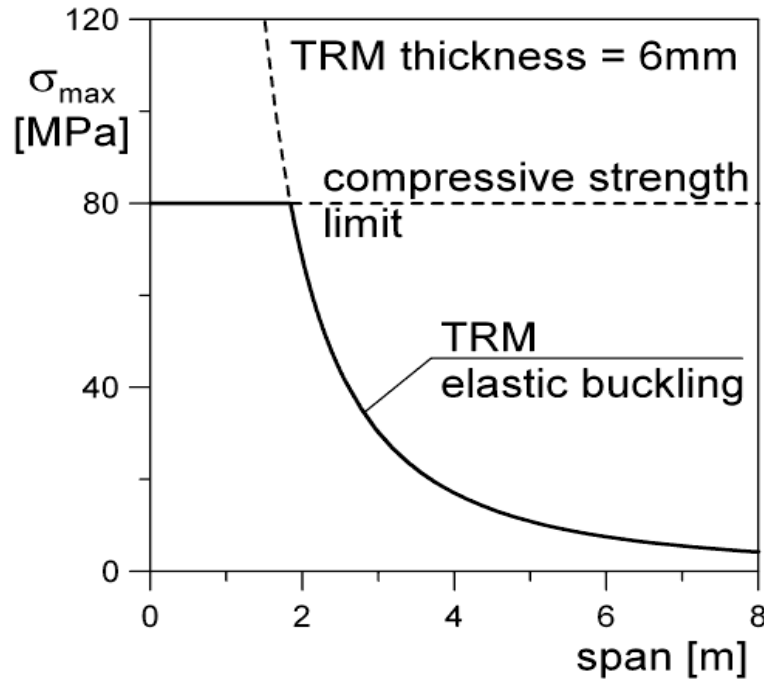
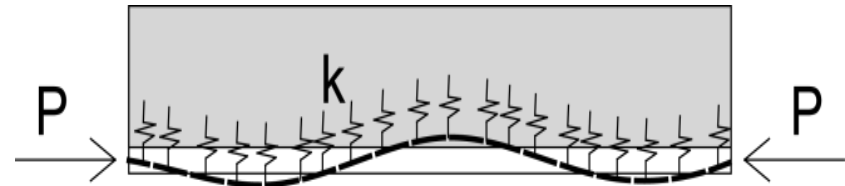
Thin layers for composite structure



No.	Failure mode		
A	tension failure of the reinforcement		
B	compression failure of the core at the point of load application		
C	local bending failure of the upper facing		
D	local shear failure of the upper facing		
E	shear failure of the core and delamination of core and facings		
F	longitudinal shear failure of the bond between the core and the upper facing (at one or both ends)		
G	compression failure of the core at the supports (at one or both ends)		

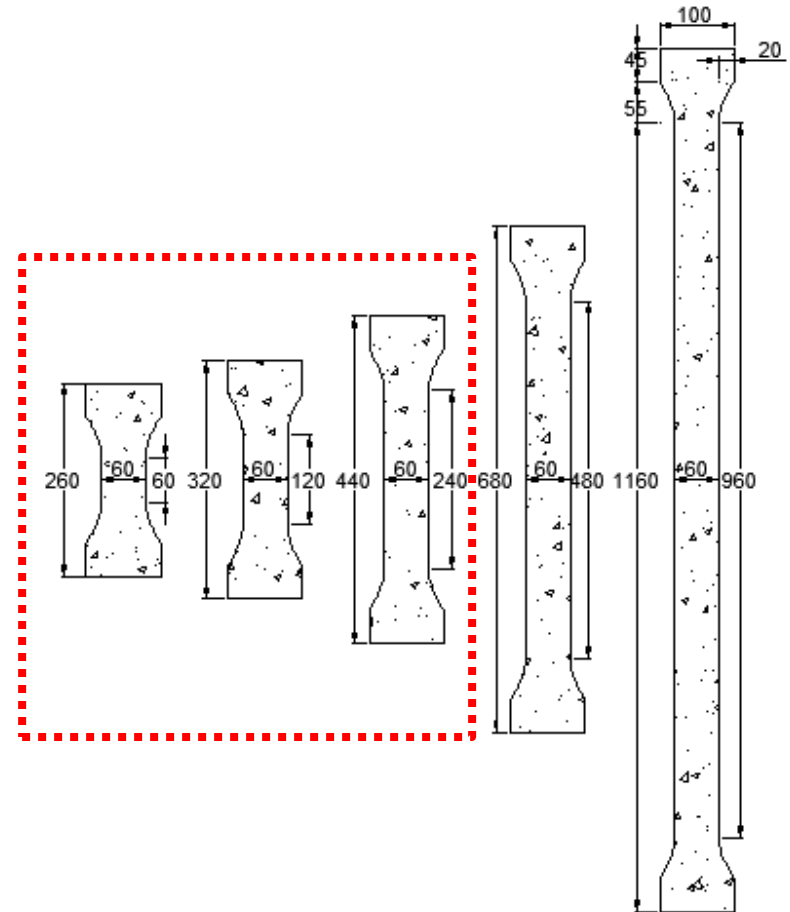
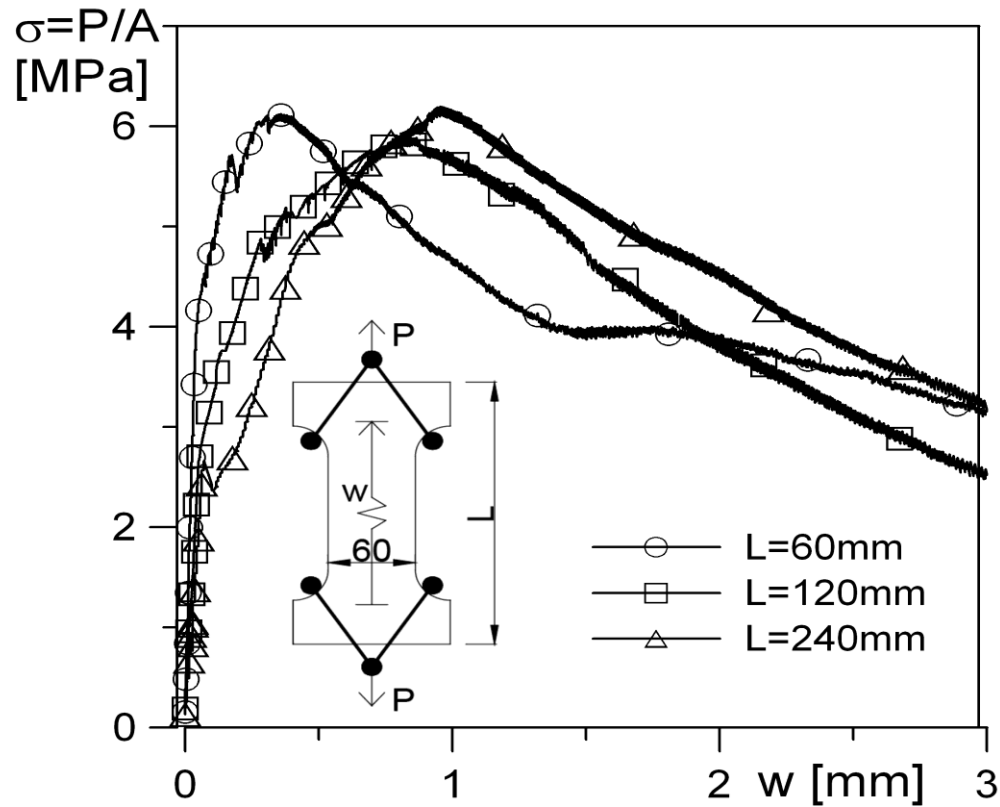


Buckling of TRM layer

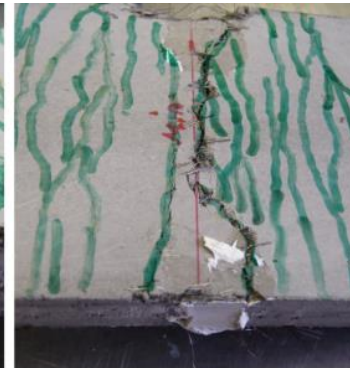
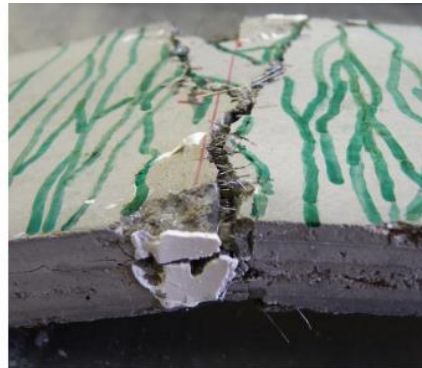
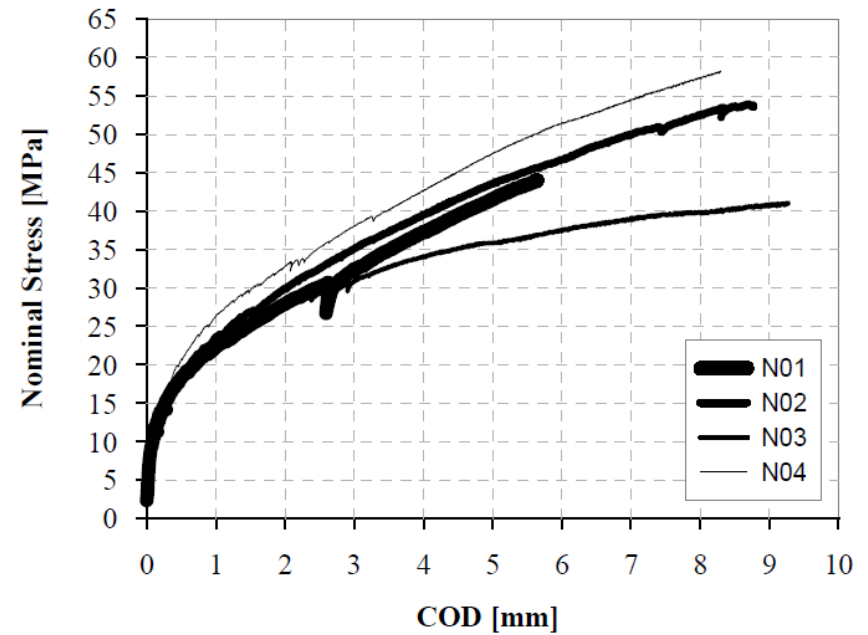
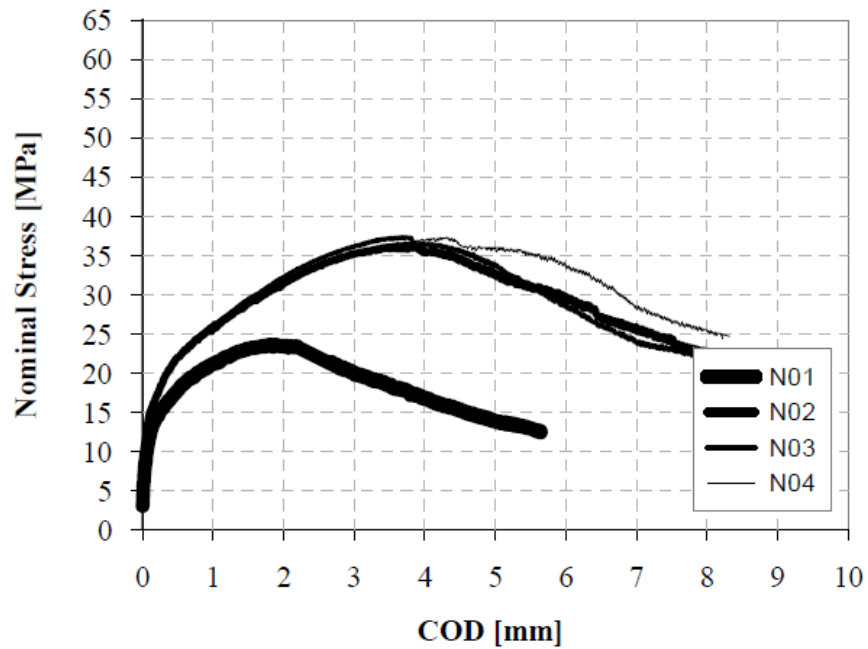


Link between layers

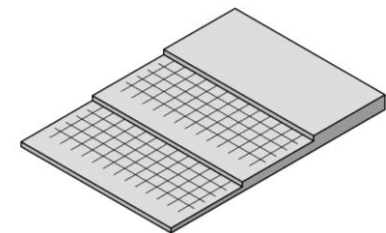
Size effect in uniaxial tension



TRC and UHPFRC: a significant synergistic behaviour

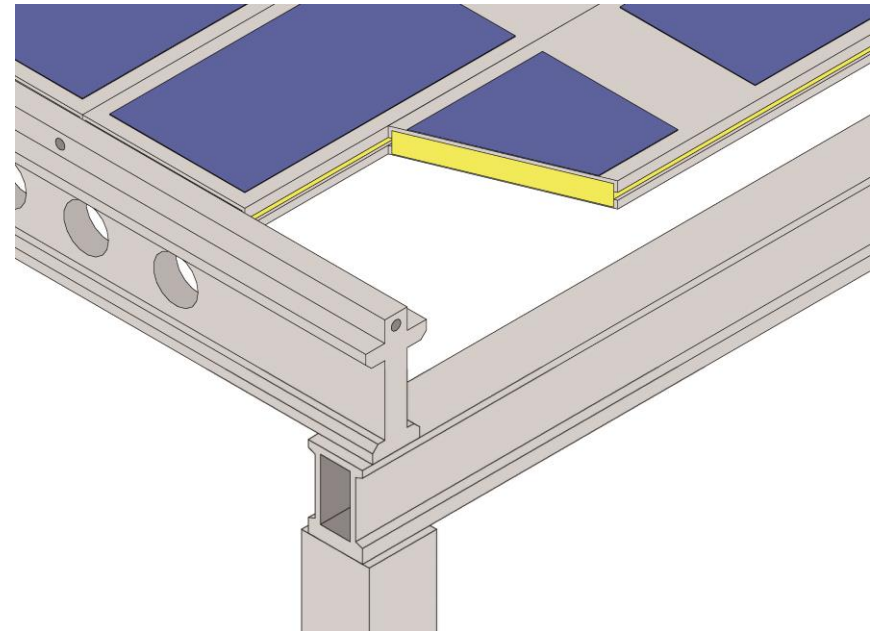


2 layers



Challenges

- ✓ insulating material: thermal and mechanical performance
- ✓ compatibility with photovoltaic panels
- ✓ light structures to reduce the seismic loads and for a sustainable construction
- ✓ durable & dismantlable constructions
- ✓ fire resistant



Concluding remarks

- ✓ Thin walled structures represent the future of many solutions for retrofitting and design of roofing and façade systems, due to their ability to reduce the dead weight and to be used in engineered technical solutions aimed at solving at the same time safety, insulation, fire resistance and energy caption
- ✓ Need of “structural” specimens for characterization. The mechanical is not homogeneous and isotropic. If this assumption is forced, a suitable k factor has to be used, especially for local check of safety.
- ✓ The conceptual design requires a global ductile behaviour: if specific bending or axial response is softening, a careful prevision of self-stresses due to shrinkage, thermal loads and boundary conditions must be computed, because if their combination can induce cracking, the crack opening regarded as limit values by Codes can easily be exceeded due to crack opening localization
- ✓ the addition of a suitable reinforcement as AR glass fabric can simplify the design, guaranteeing a hardening behaviour both in uniaxial tension and in bending. **A special attention to robustness is also absolutely required**

- ✓ the designer has to pay attention to instability and deformability as for steel structures: when precast elements are designed, a special care has to be paid to deformability in the cross section plane, because the shape loss of the cross section can strongly reduce the bearing capacity
- ✓ In multi-layered solutions a connection between the layers is suggested to prevent the detachment consequent to the buckling of the compressed layer.
- ✓ The in-plane load diffusion can cause a brittle failure in the D-regions, but no needs to reduce the uniaxial compressive force is required if FRC respects the minimum toughness performance requirements expressed in terms of minimum SLS and ULS residual strengths
- ✓ size effect requires further research: the results obtained highlight a weaker size effect dependency of residual strengths even if first cracking strength of FRC seems to be affected as plain concrete. Hybrid solutions with micro-fibres can mitigate also this brittleness effect.
- ✓ A mechanical characterization made at room temperature after a high temp. exposure can give the residual strength variation with temperature, allowing the designer a full fire resistance computation. HPFRCC can represent an interesting solution for fire resistance due to their impressive bending strength up to 400°C.

*Thank you
for your attention*

